

# Imaging Atmospheric Telescopes: Detection Principles

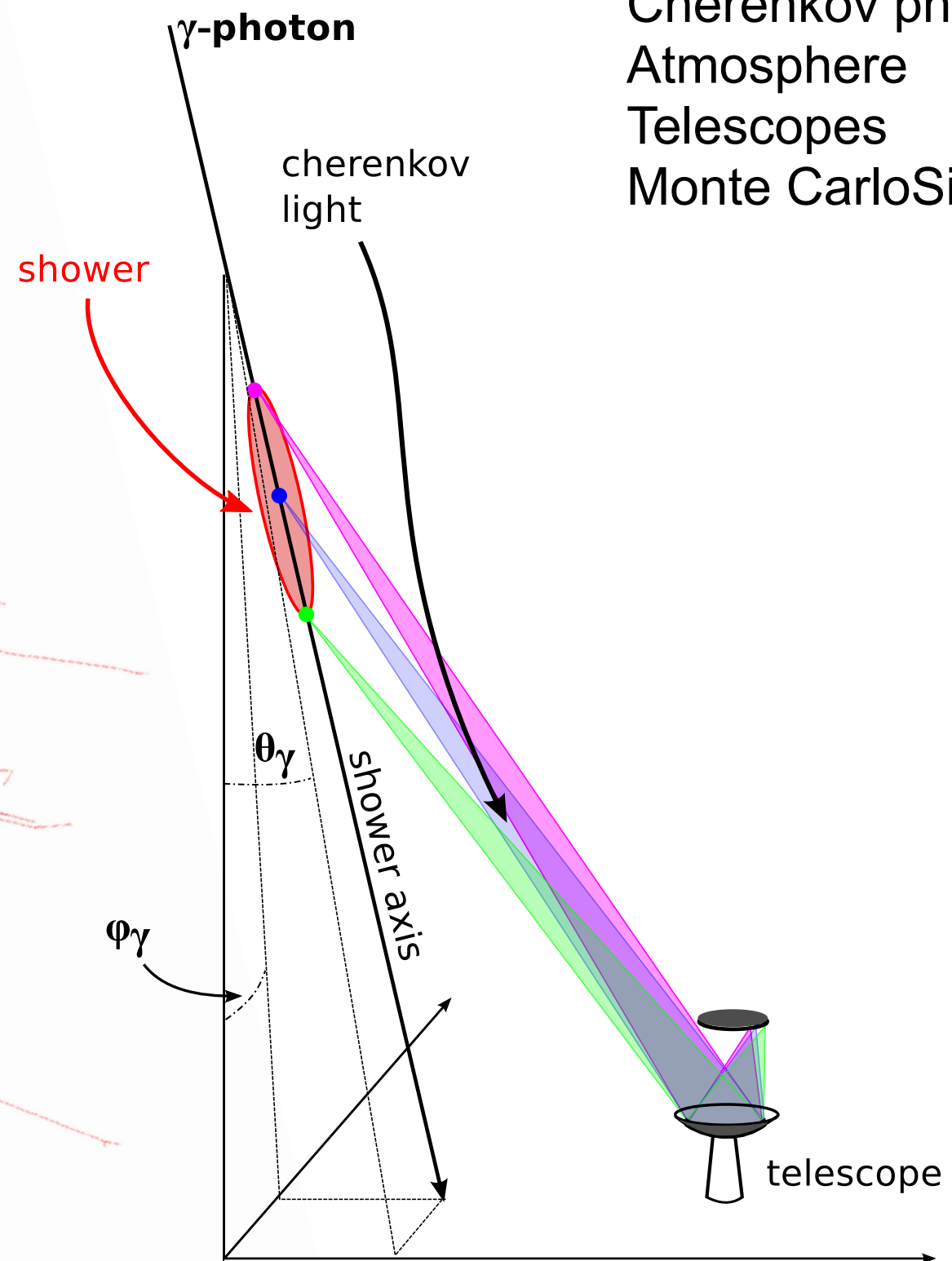
CTAO School 2025

Gernot Maier



# Outline.

Extensive air showers  
Cherenkov photons  
Atmosphere  
Telescopes  
Monte Carlo Simulations





# What we want to measure.

- For each event.
  - identification (probability that it is a gamma ray)
  - energy
  - direction
  - time
  - (do not measure photon polarization)
- (obviously we want to maximize number of events & precision)
- (replace "gamma ray" by the particle of interest)

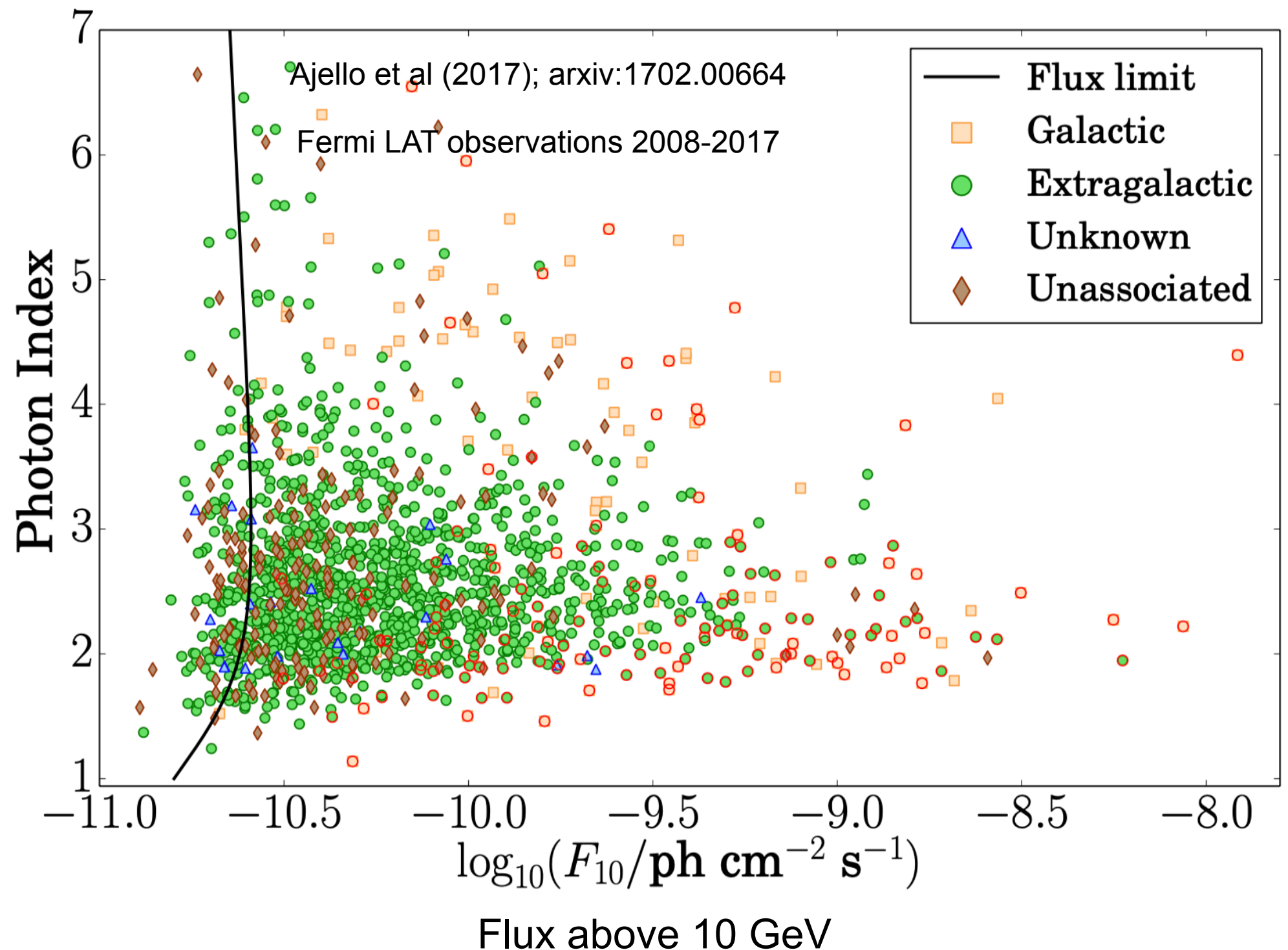
# Fluxes and spectra.

.. in general:

- low fluxes ( $10^{-10}$  photons/cm<sup>2</sup>/s)
- spectra with power-law like shape

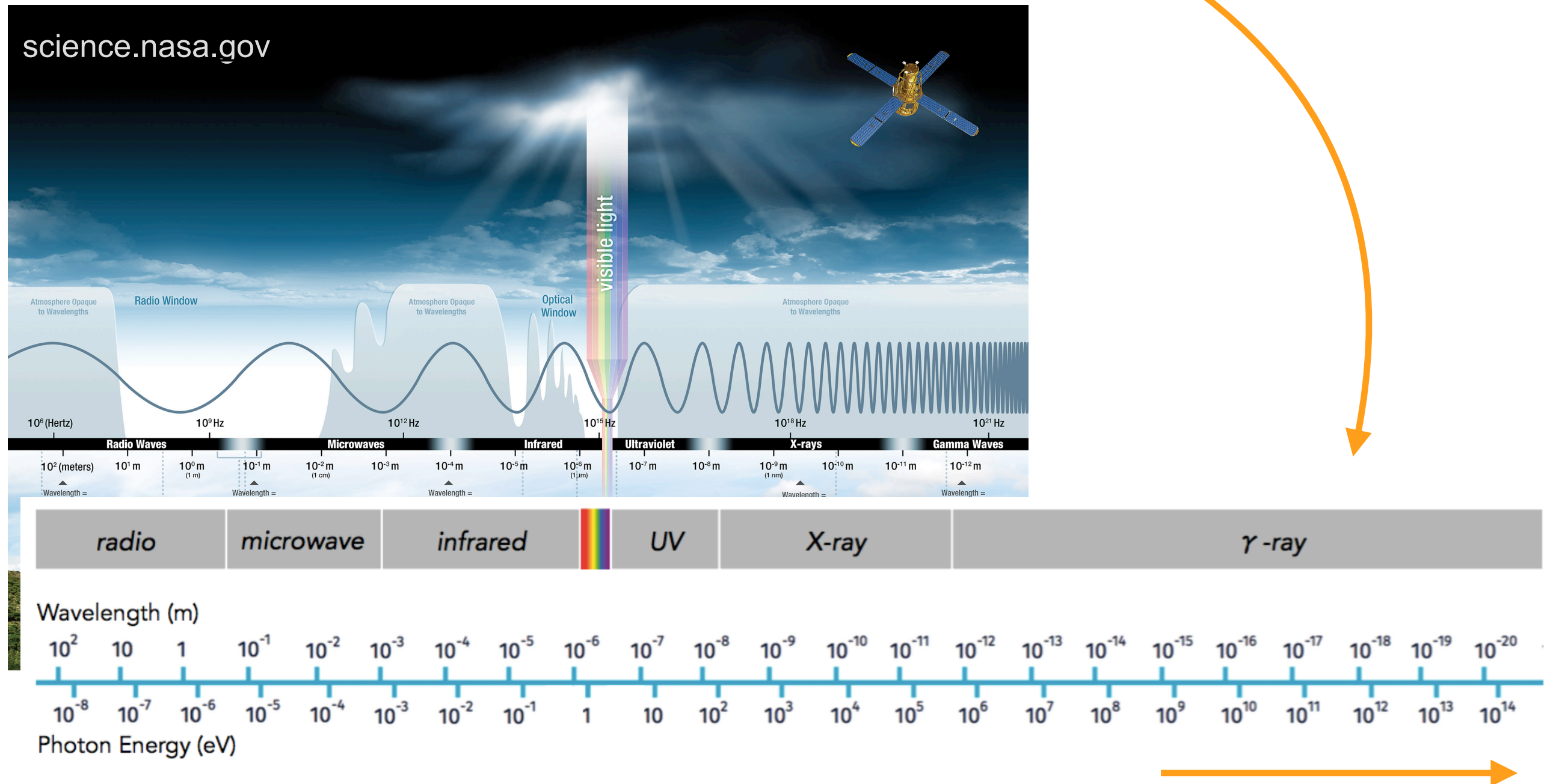
$$\frac{dN}{dE} \propto E^{-\gamma}$$

Fermi LAT  
~1 m<sup>2</sup> of effective area



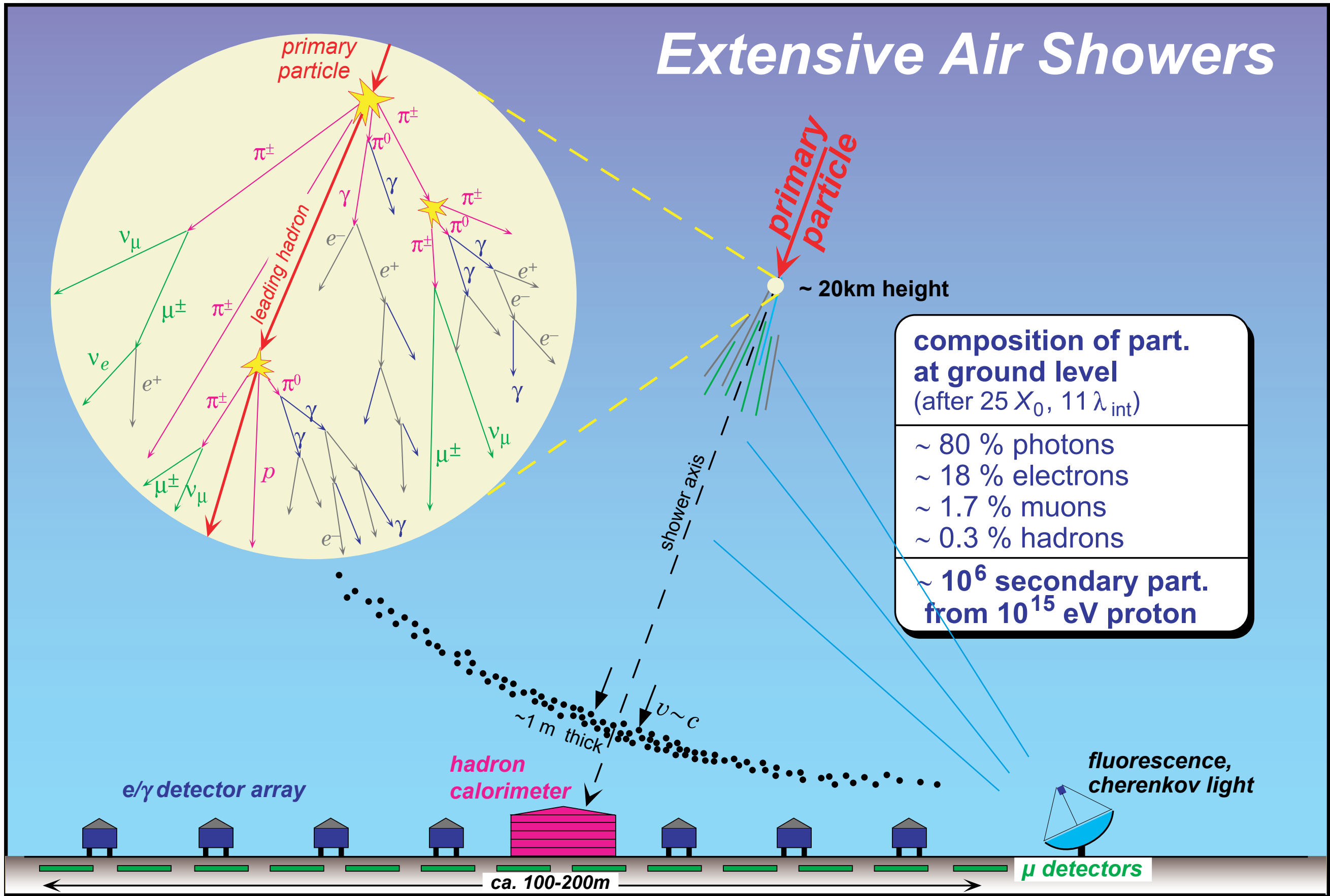


# Very-High Energy Gamma-ray Astronomy.

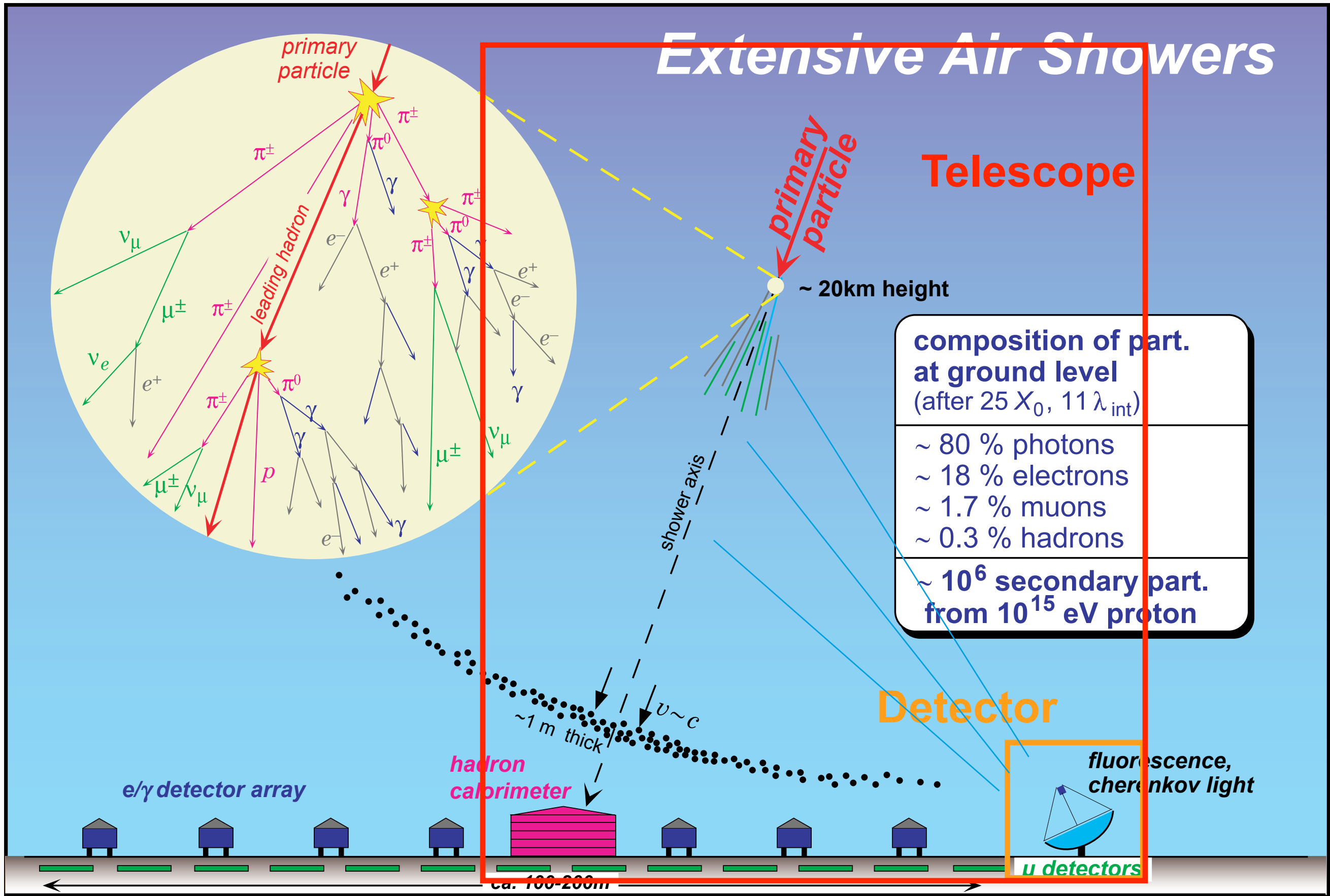


GeV ...PeV  
 $10^9 - 10^{15}$  eV

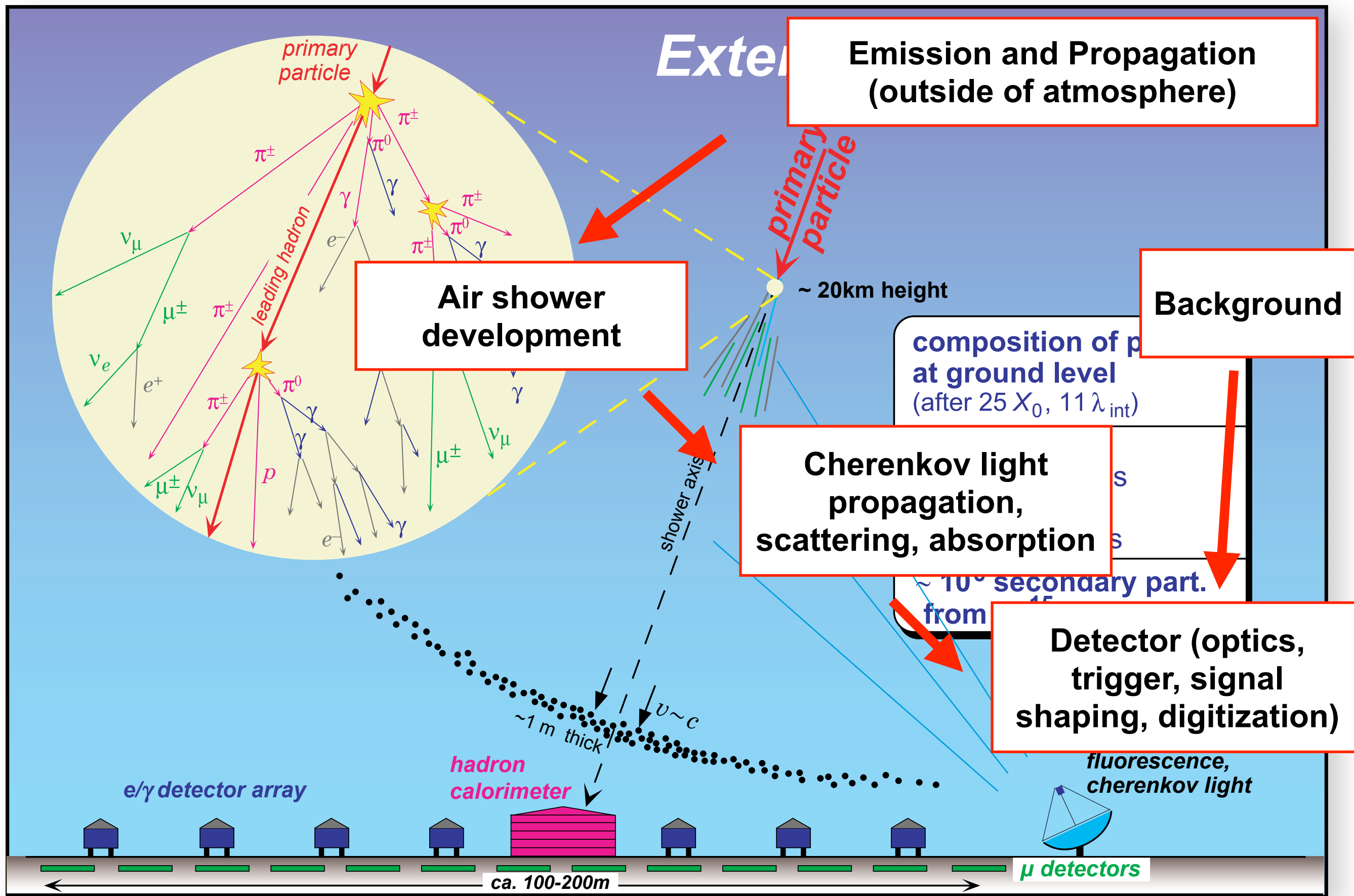
# Extensive Air Showers



# Extensive Air Showers







Air showers are complicated: use Monte Carlo simulations.

**Atmosphere.**

**Nature's calorimeter.**

# Atmosphere.

Tomorrow: detailed view on  
the atmosphere

- composition: 78% N<sub>2</sub>, 21% O<sub>2</sub>, 0.9% Ar.
- density (isothermal approximation):

$$\rho_{\text{atm}}(h) \approx \rho_0 e^{-h/h_0}$$

$$\rho_0 \approx 1.225 \text{ kg/m}^3 \quad \text{scale height: } h_0 = RT/(\mu g) \approx 8.4 \text{ km}$$

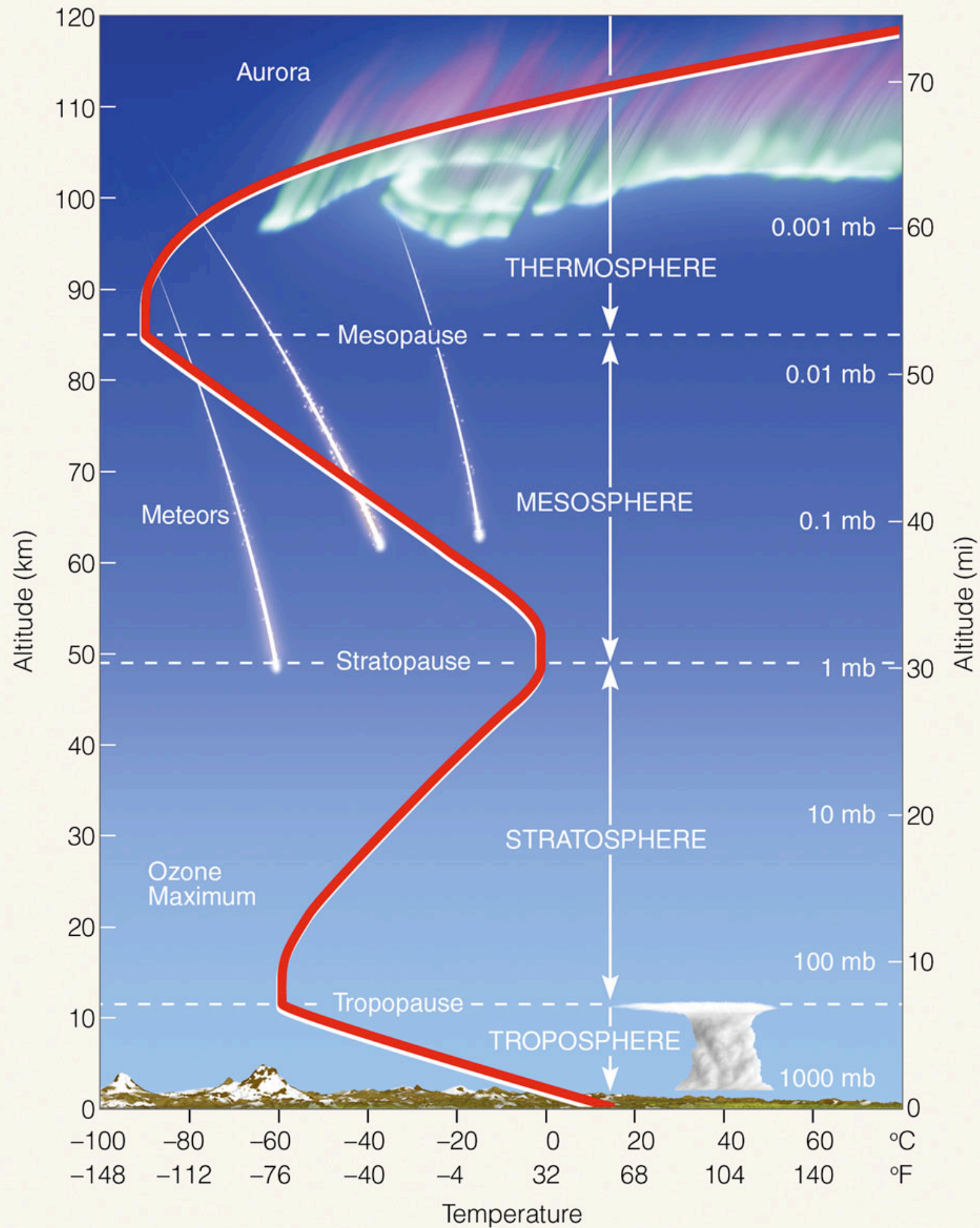
- (for air shower simulations: need to be better than isothermal approximation)
- actual matter traversed by air shower: slant depth / thickness

$$X_v(h) = \int_h^\infty \rho_{\text{atm}}(z) \, dz$$



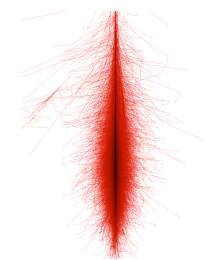
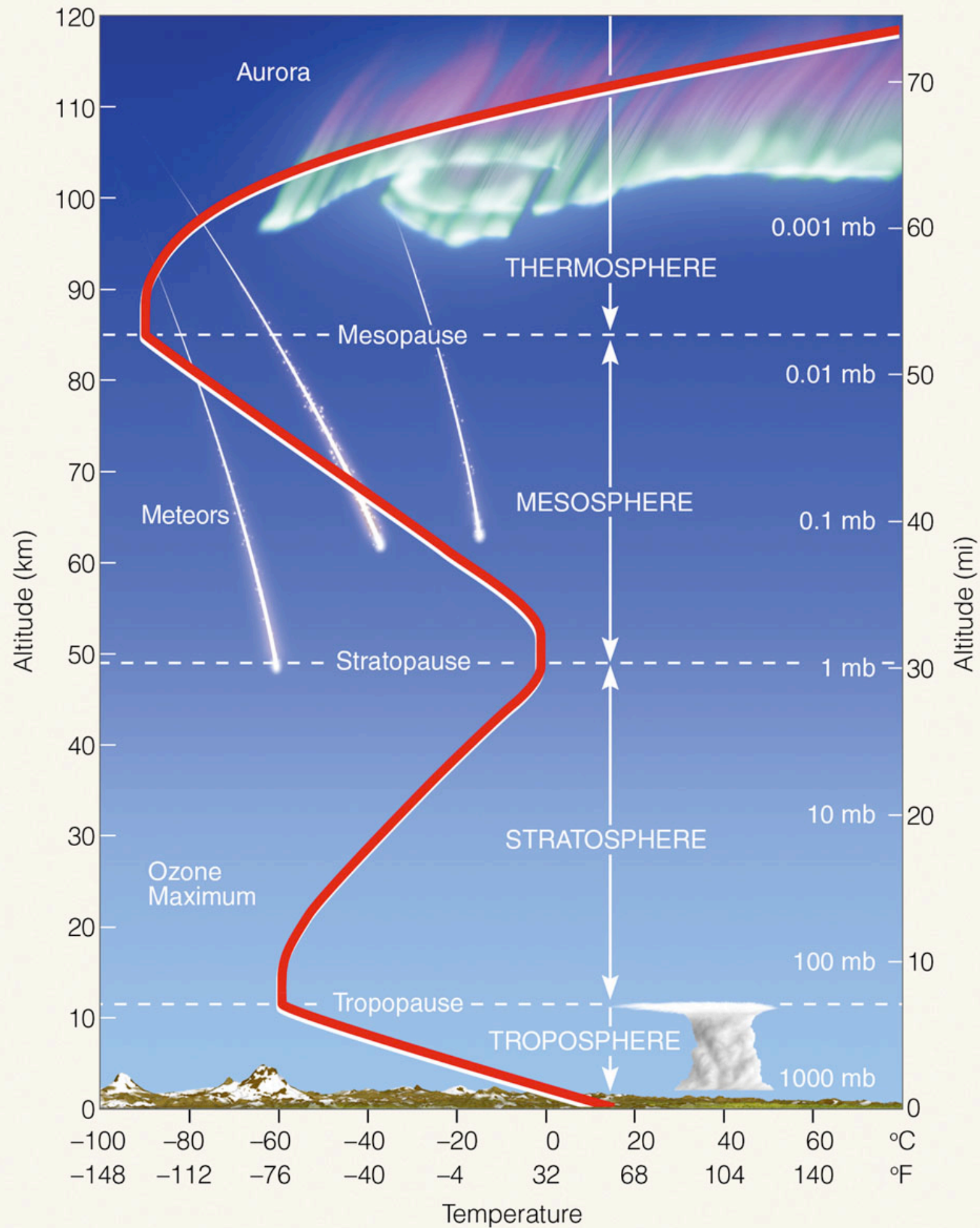
# Atmosp

<https://ghsearch.weebly.com/atmosphere.html>



# Atmosp

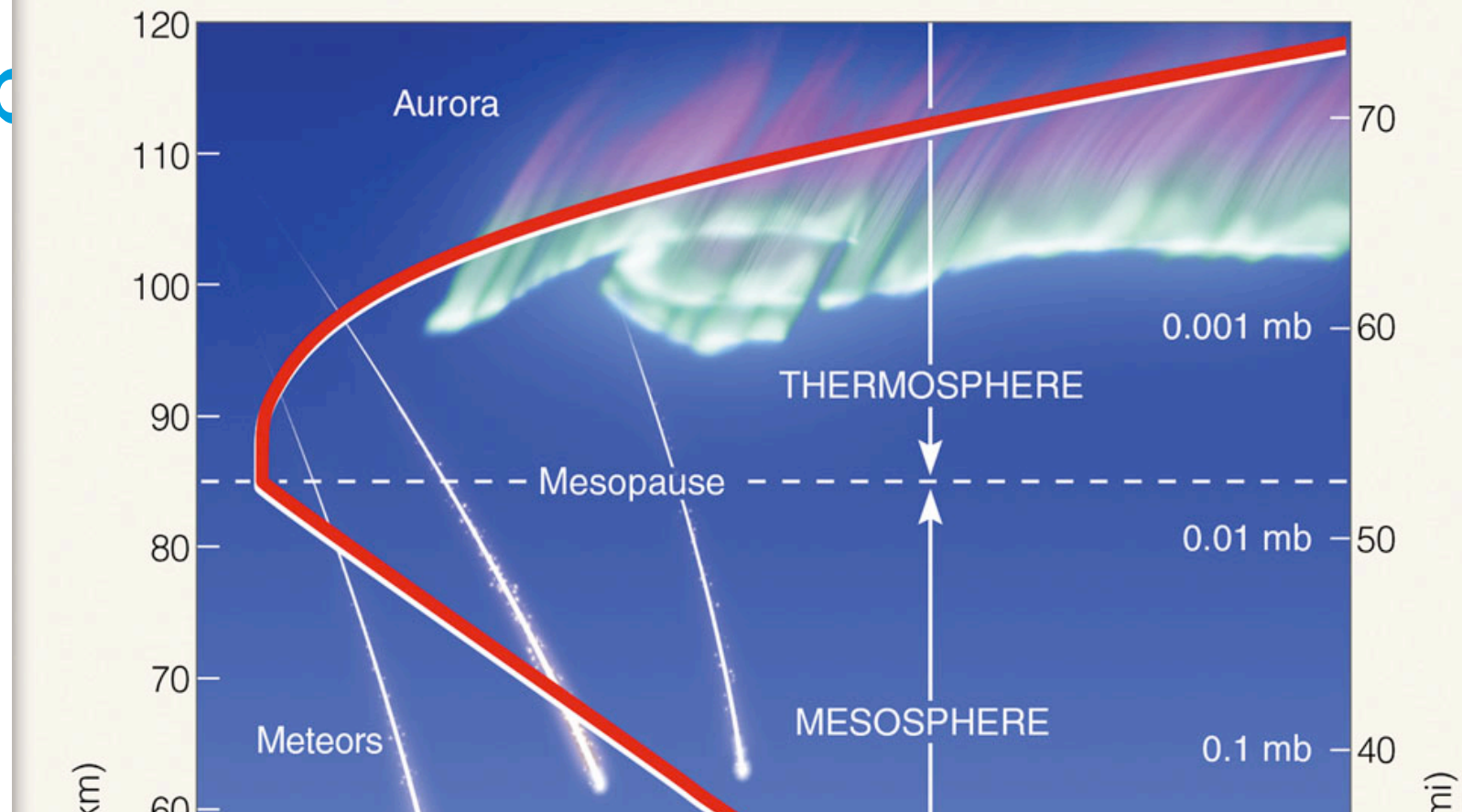
<https://ghsearch.weebly.com/atmosphere.html>



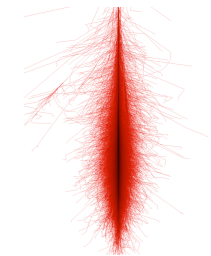
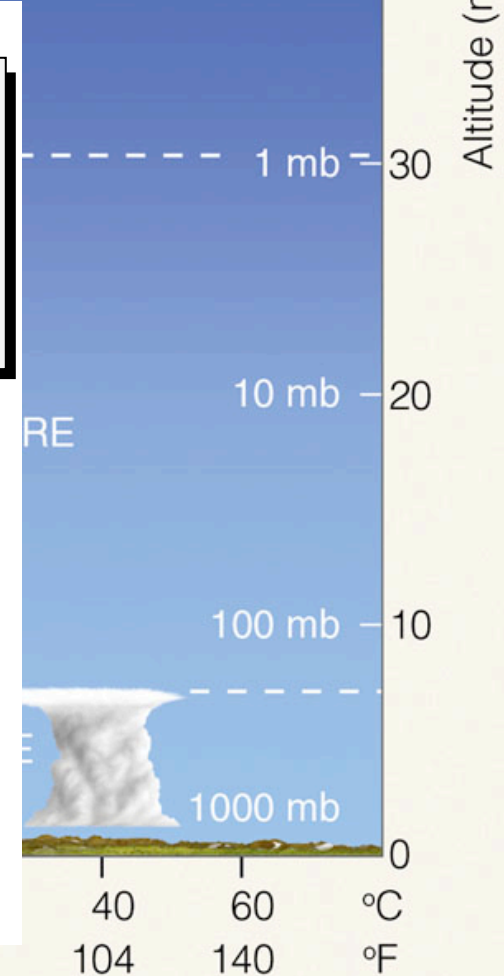
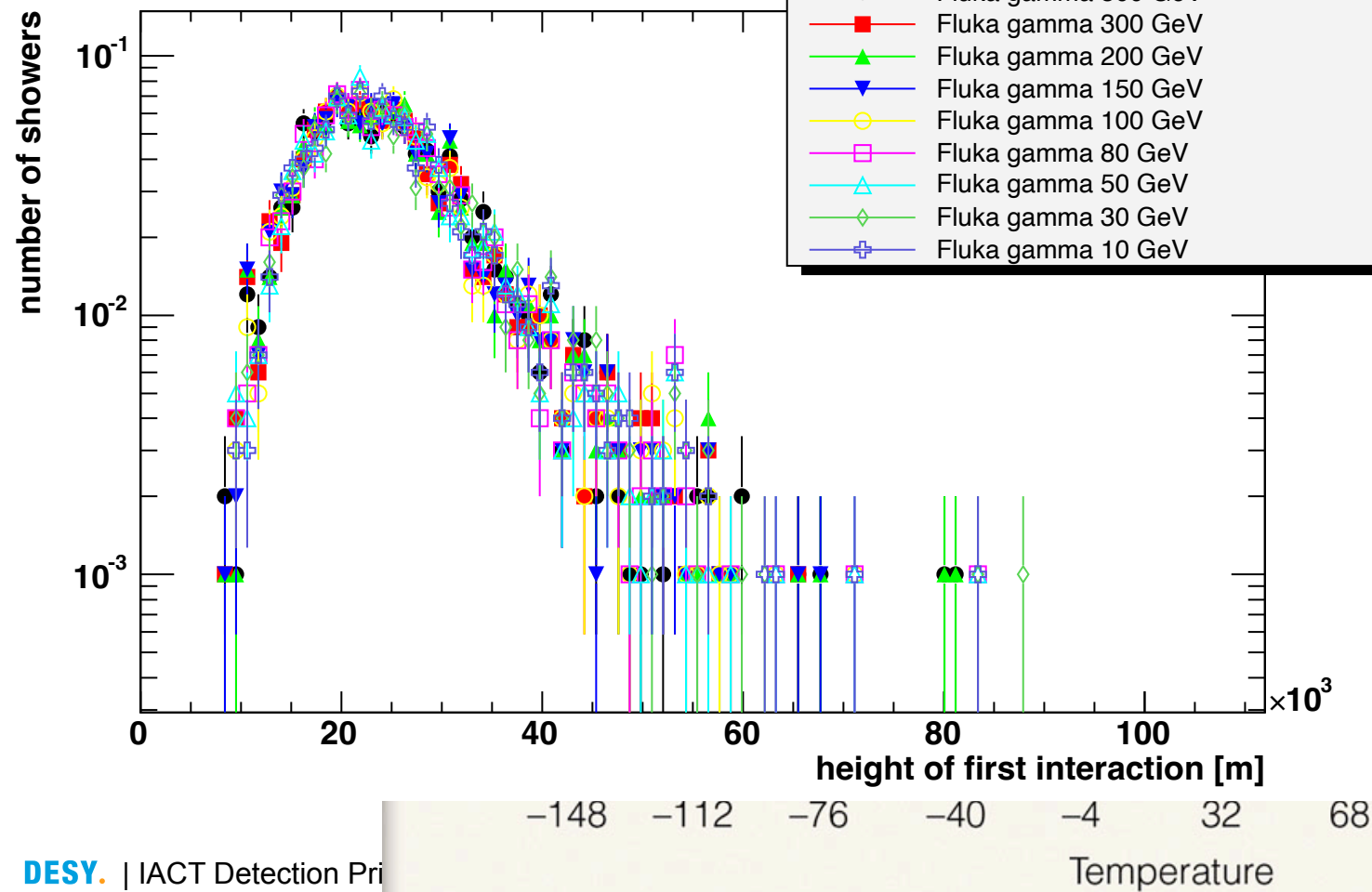


# Atmosphere

sphere.html



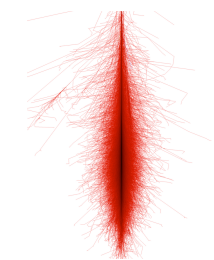
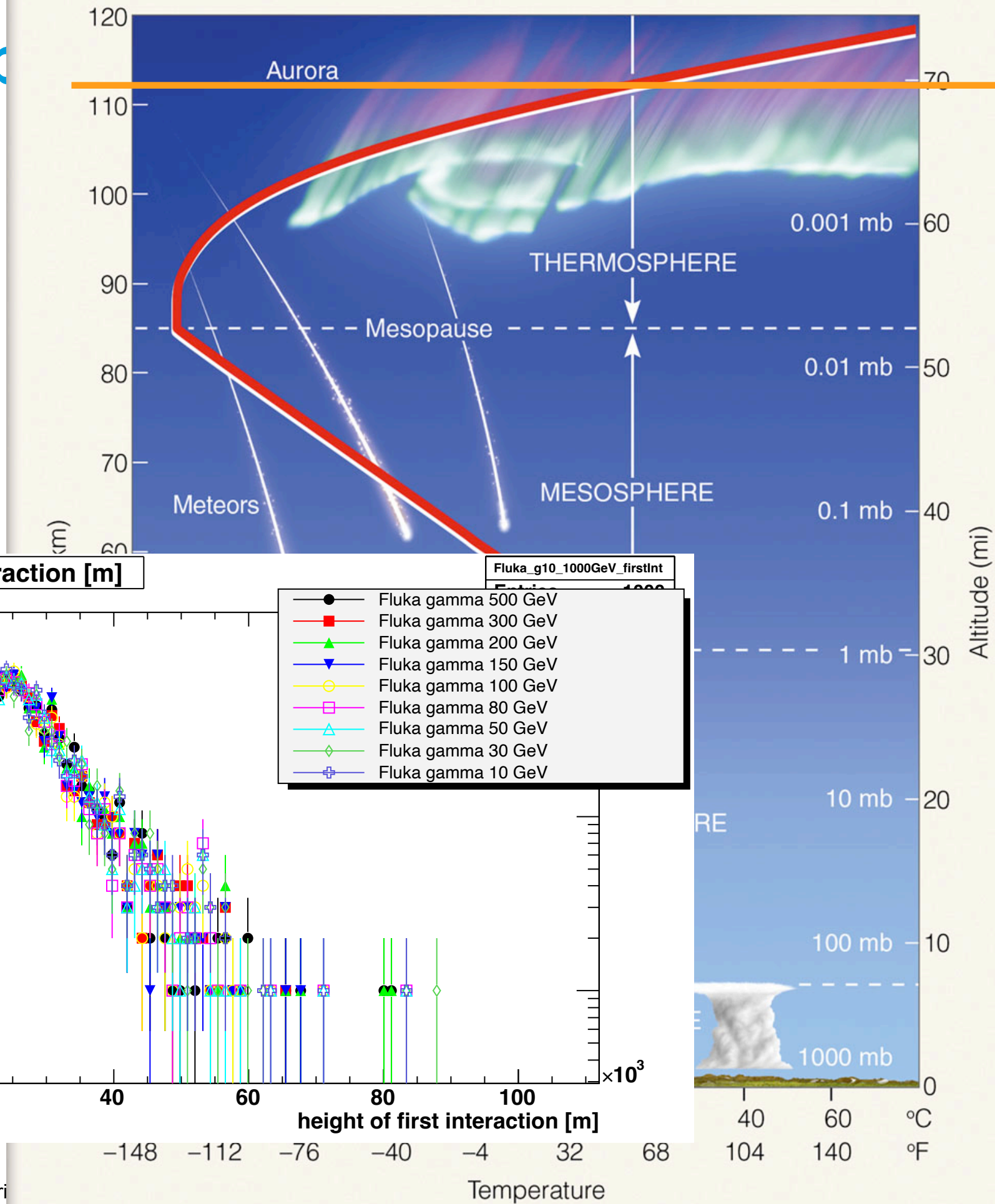
height of first interaction [m]



# Atmosp

Shower simulations  
(CORSIKA)  
Top of atmosphere  
112.8 km

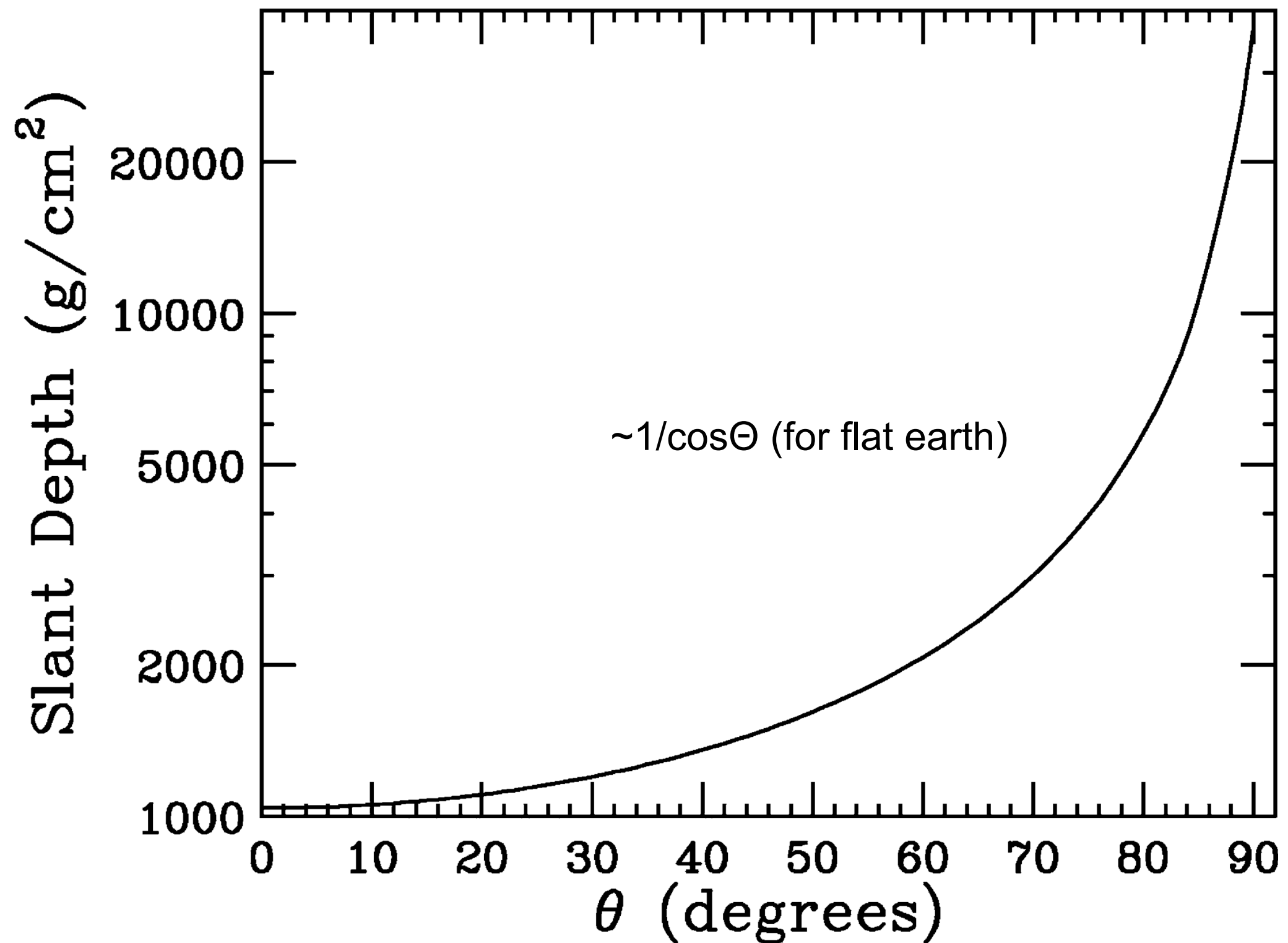
sphere.html





# Thickness vs zenith angle.

Anchordoqui et al. 2004



# Flat earth.

Bernlöhr 2000

~4% difference in thickness at 80 deg for curved atmosphere

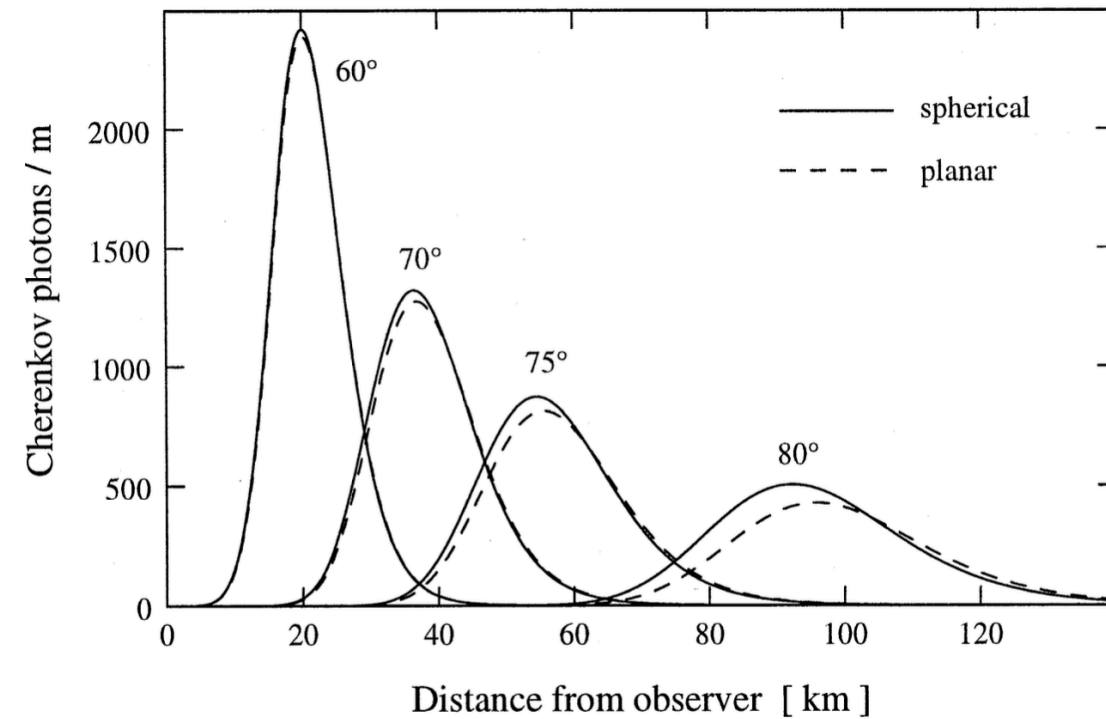
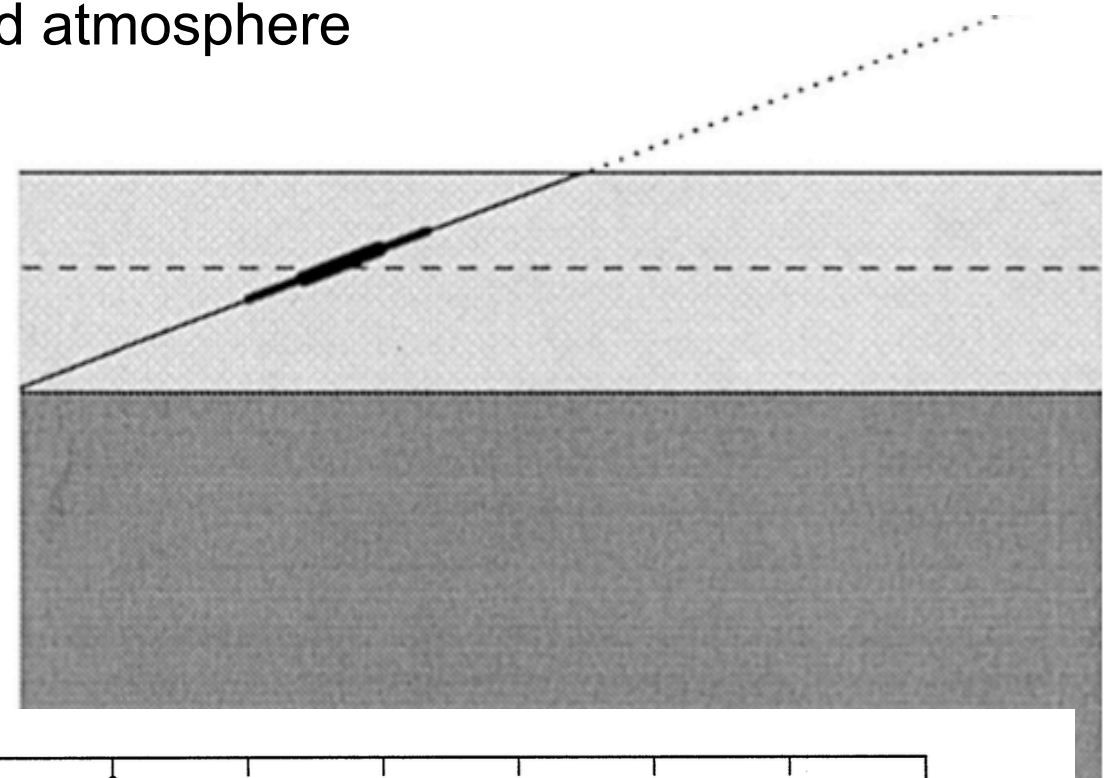
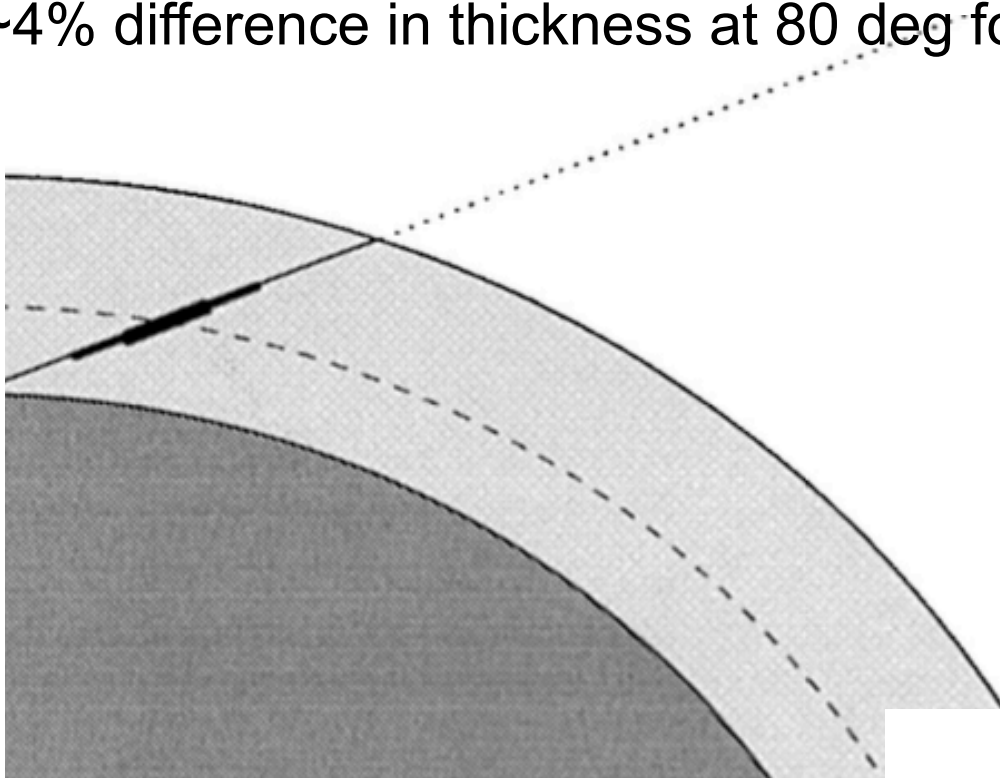
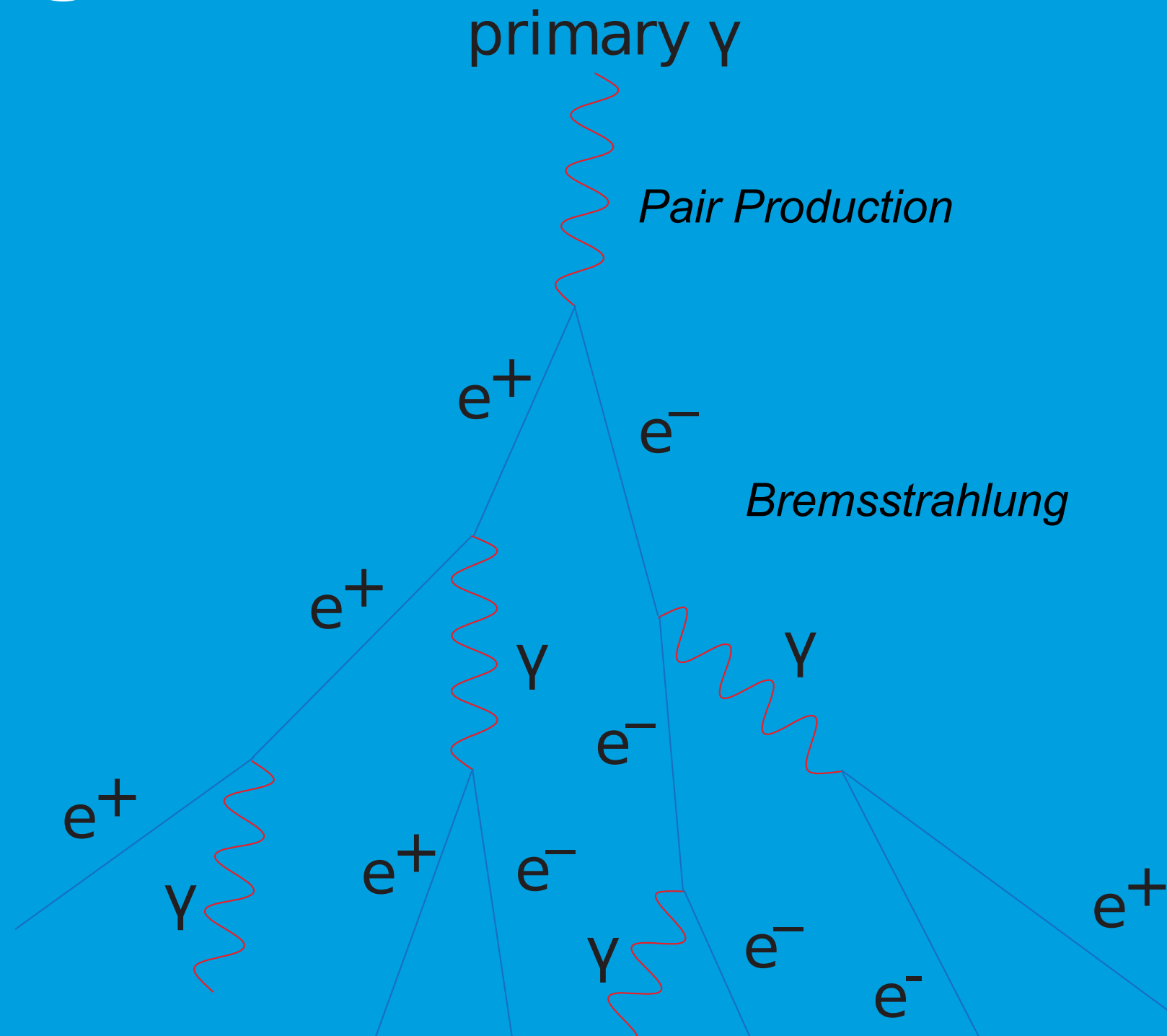


Fig.14. The average longitudinal Cherenkov emission profile as a function of distance from the observer (Cherenkov photons emitted in the wavelength range 300–600 nm per meter along the

# Air showers.

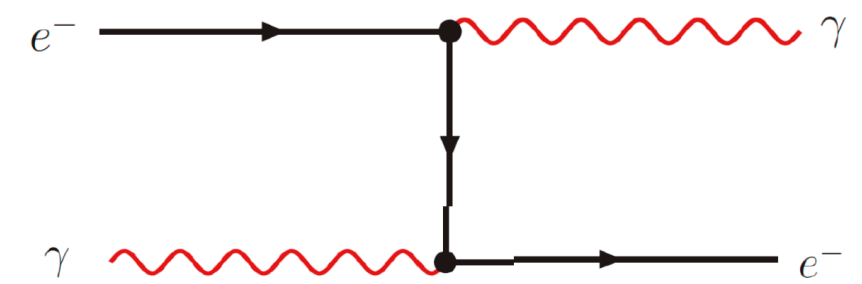
## Primary Gamma.



# Bremsstrahlung.

$$e + Z \rightarrow e + \gamma + Z$$

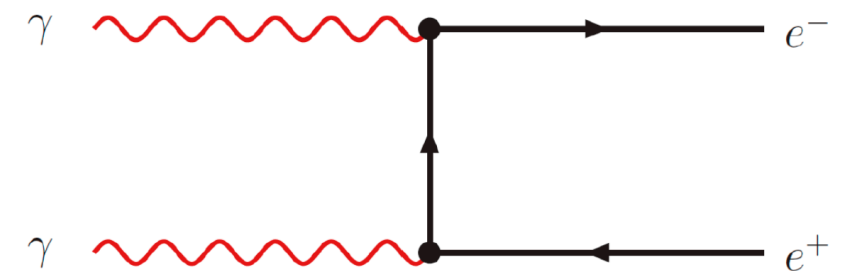
$$e + \gamma_{\text{virtual}} \rightarrow e + \gamma$$



# Pair production.

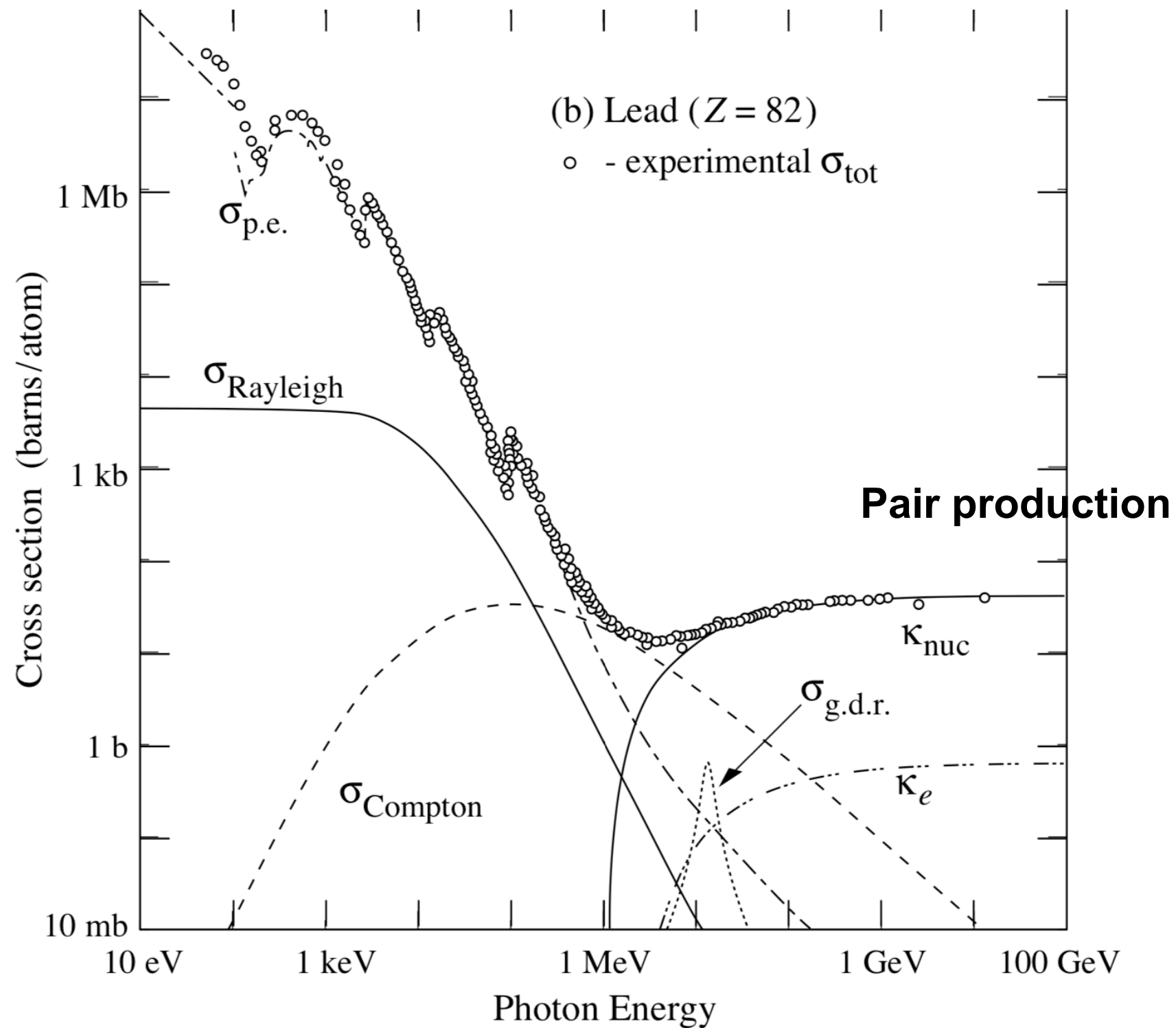
$$\gamma + Z \rightarrow e^+ + e^- + Z$$

$$\gamma + \gamma_{\text{virtual}} \rightarrow e^+ + e^-$$



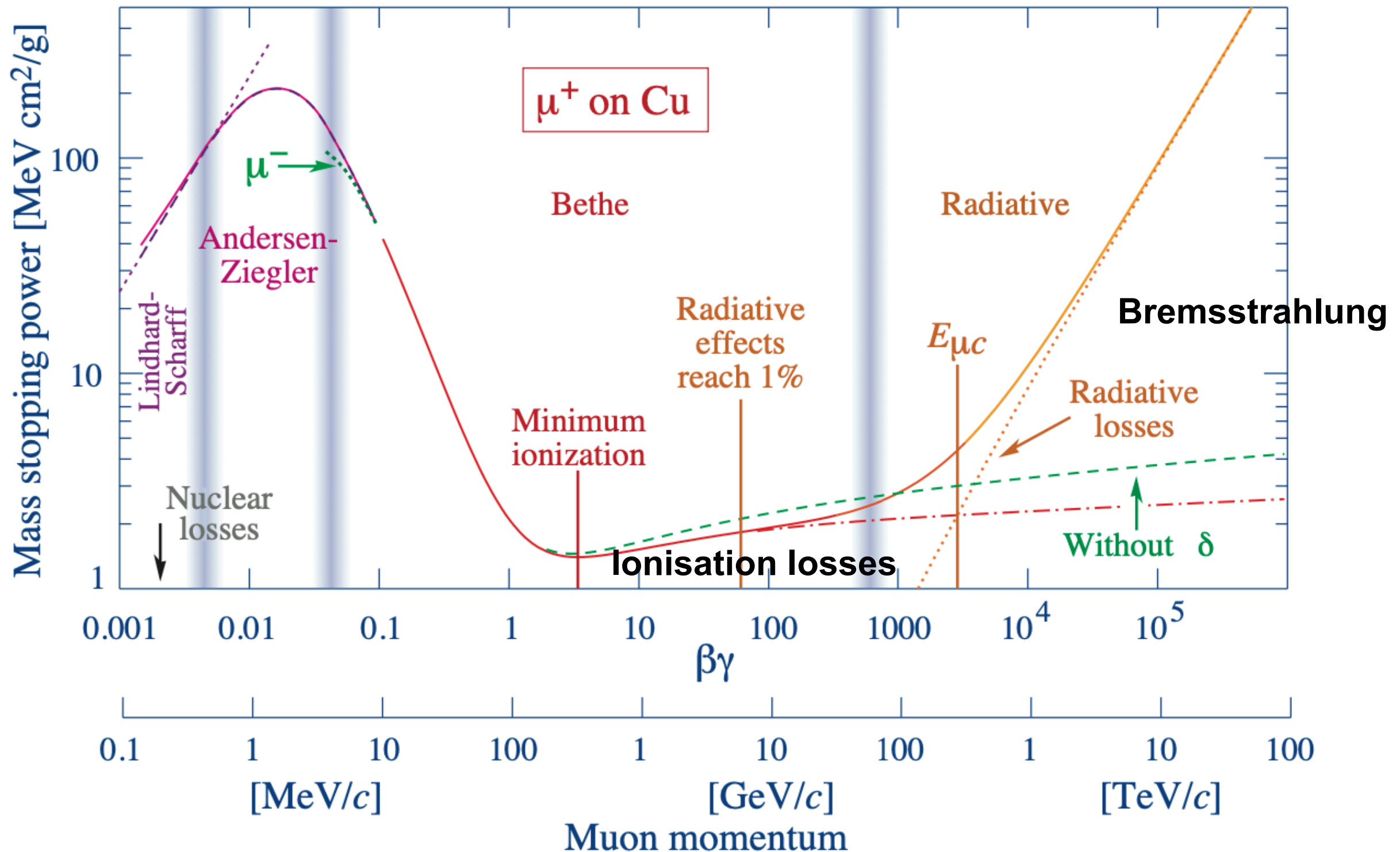


# Photon interaction.



Particle Physics Review

# Energy losses electrons / muons.



Particle Physics Review

# Radiation length.

characteristic amount of matter traversed by  
electrons/positrons or photons

mean distances over which a  
high-energy electron reduces its  
energy by a factor  $1/e$

7/9th of the mean free path for  
pair production for a high-energy  
photon

From fit to data (Dahl):

$$X_0 = \frac{716.4 \text{ g cm}^{-2} A}{Z(Z+1) \ln(287/\sqrt{Z})}$$

mixtures:

$$1/X_0 = \sum w_j / X_j$$

$w_j$ : fraction by weight

$$\text{Air: } X_0 \approx 37 \text{ g/cm}^2$$

Scale variable frequently used:

$$t = x/X_0,$$

# Radiation length vs “Pair length”

Physical Meaning of the “Radiation Length”

$$\langle E_e(X) \rangle = E_e(0) e^{-X/\lambda_{\text{rad}}}$$

Physical Meaning of the “Pair Length”

$$N_\gamma(X) = N(0) e^{-X/\lambda_{\text{pair}}}$$

$$\lambda_{\text{rad}}^{\text{air}} \simeq 37 \frac{\text{g}}{\text{cm}^2}$$

$$\lambda_{\text{pair}} \simeq \frac{9}{7} \lambda_{\text{rad}}$$



# Radiation vs ionization losses - Critical energy.

$$dE/dX = -\alpha(E) - E/X_0$$

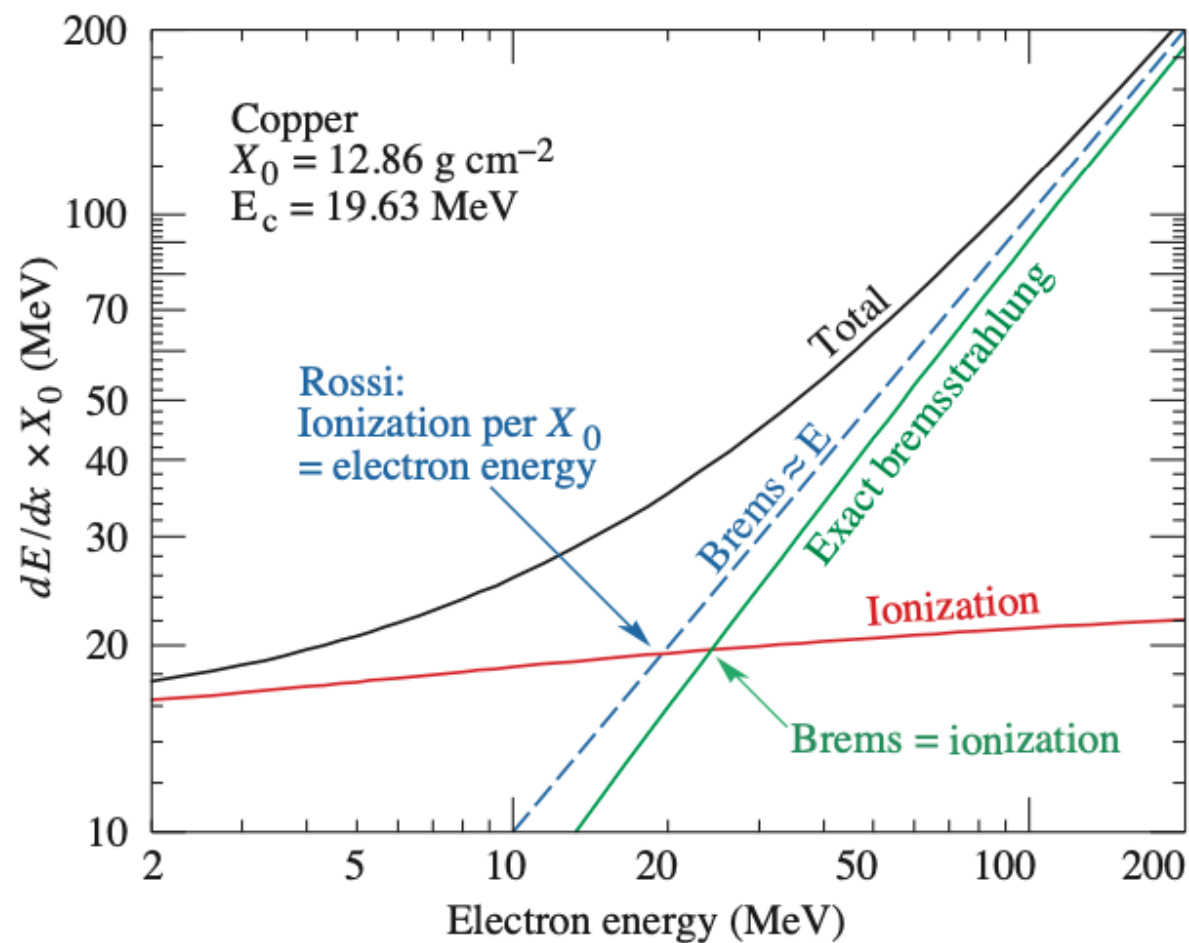


Figure 34.13: Two definitions of the critical energy  $E_c$ .

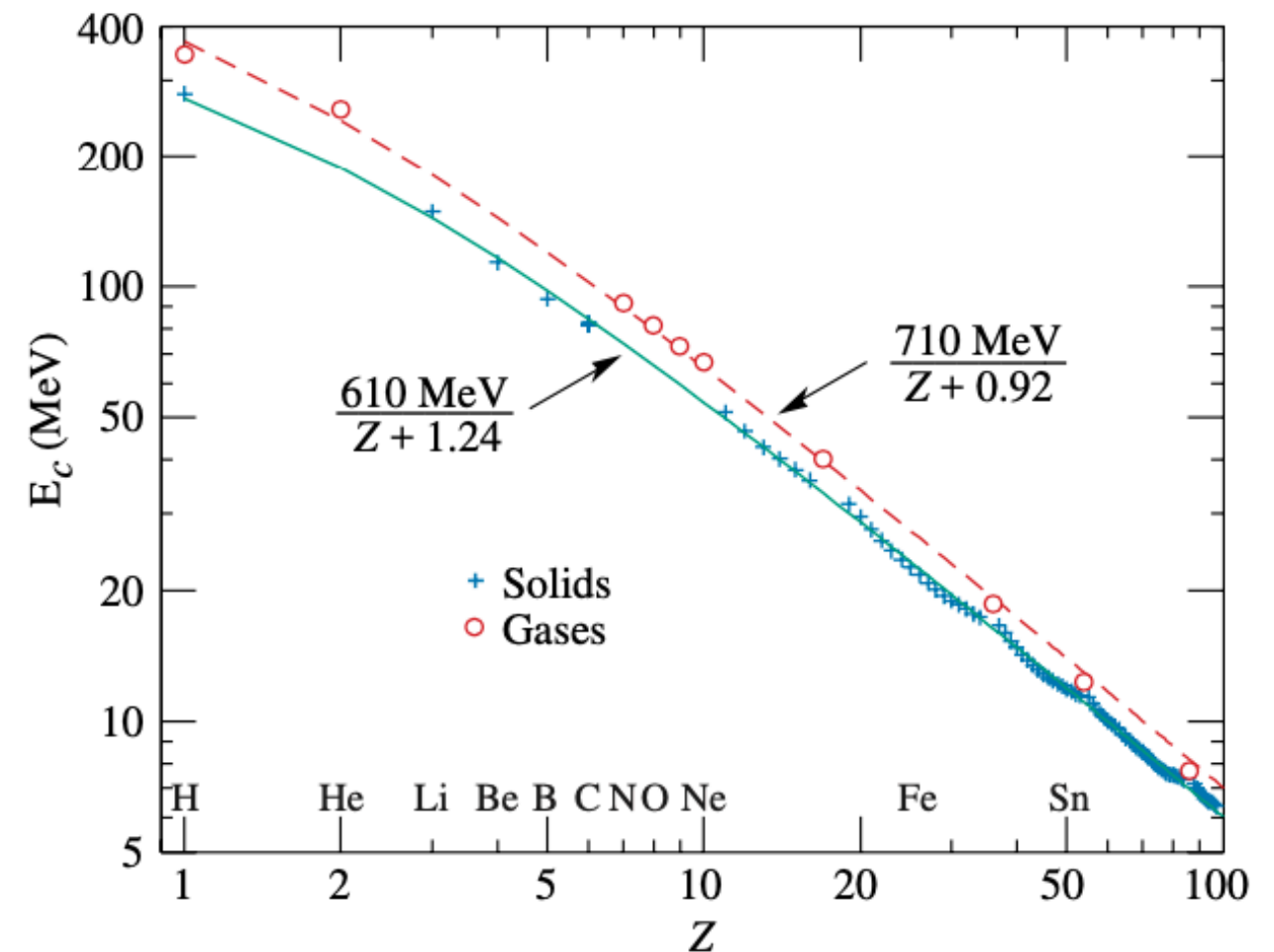
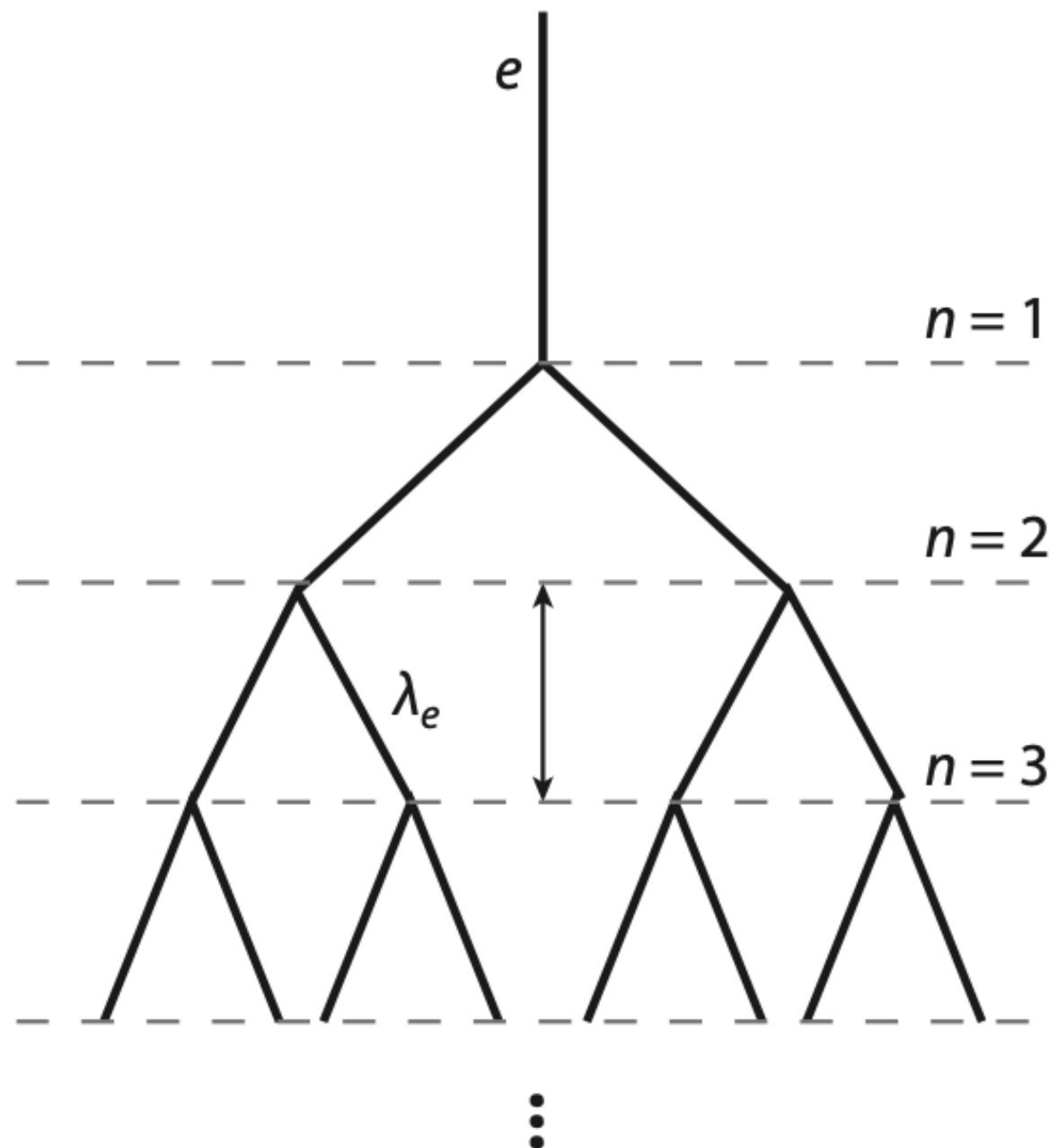


Figure 34.14: Electron critical energy for the chemical elements, using Rossi's definition [2]. The fits shown are for solids and liquids (solid line) and gases (dashed line). The rms deviation is 2.2% for the solids and 4.0% for the gases.

Air:  $E_c \approx 85 \text{ MeV}$

# Heitler model.

(introduced by Carlson & Oppenheimer 1937)

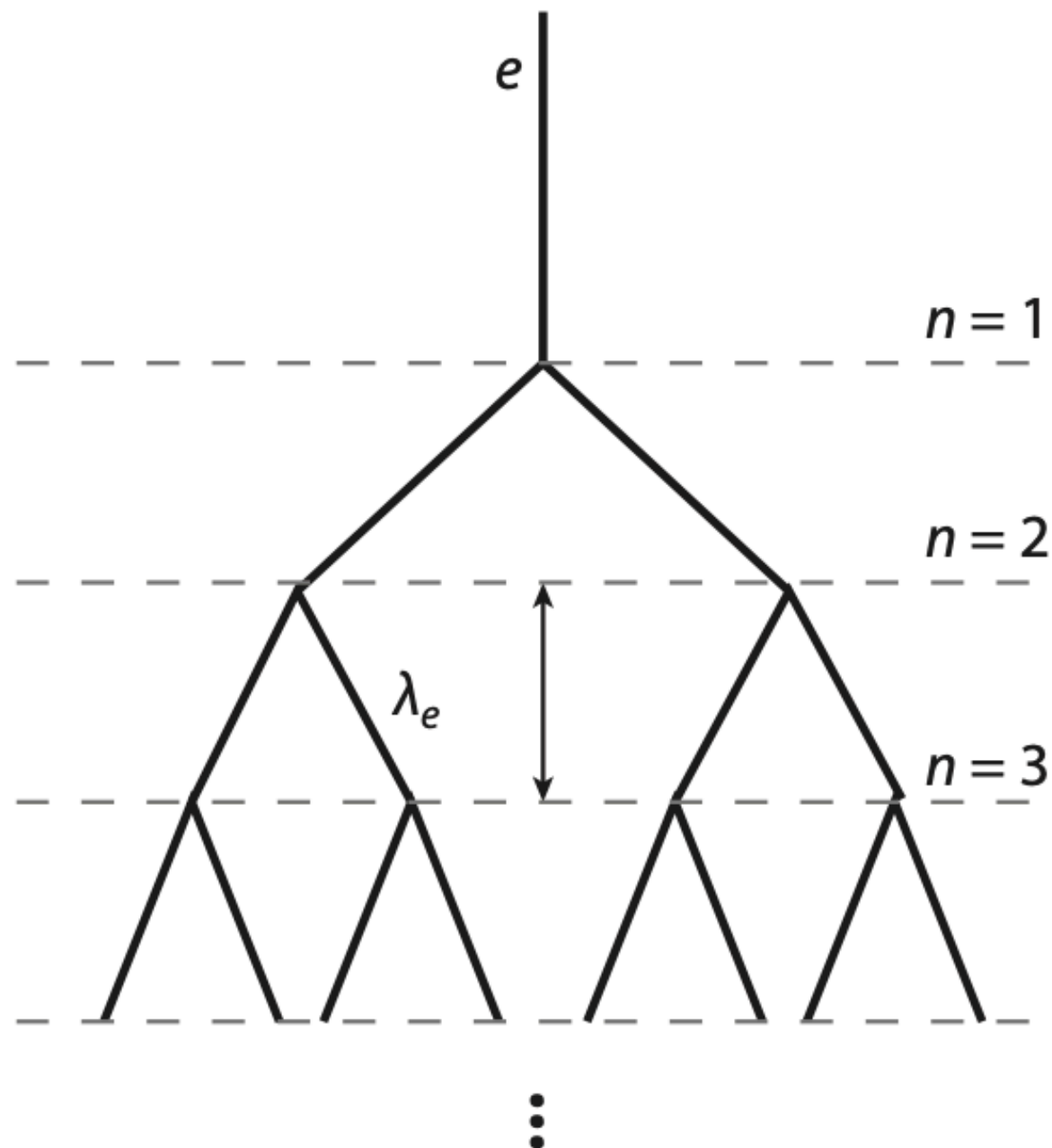


## Simplification:

- one "electron-photon" particle
- initial energy  $E$
- any interaction leads to two new particles of energy  $E/2$
- characteristic splitting length  $X_0$
- critical energy  $E_c$

# Heitler model.

(introduced by Carlson & Oppenheimer 1937)



Shower development stops at

$$\frac{E}{2^n} = E_c$$

Maximum number of particles

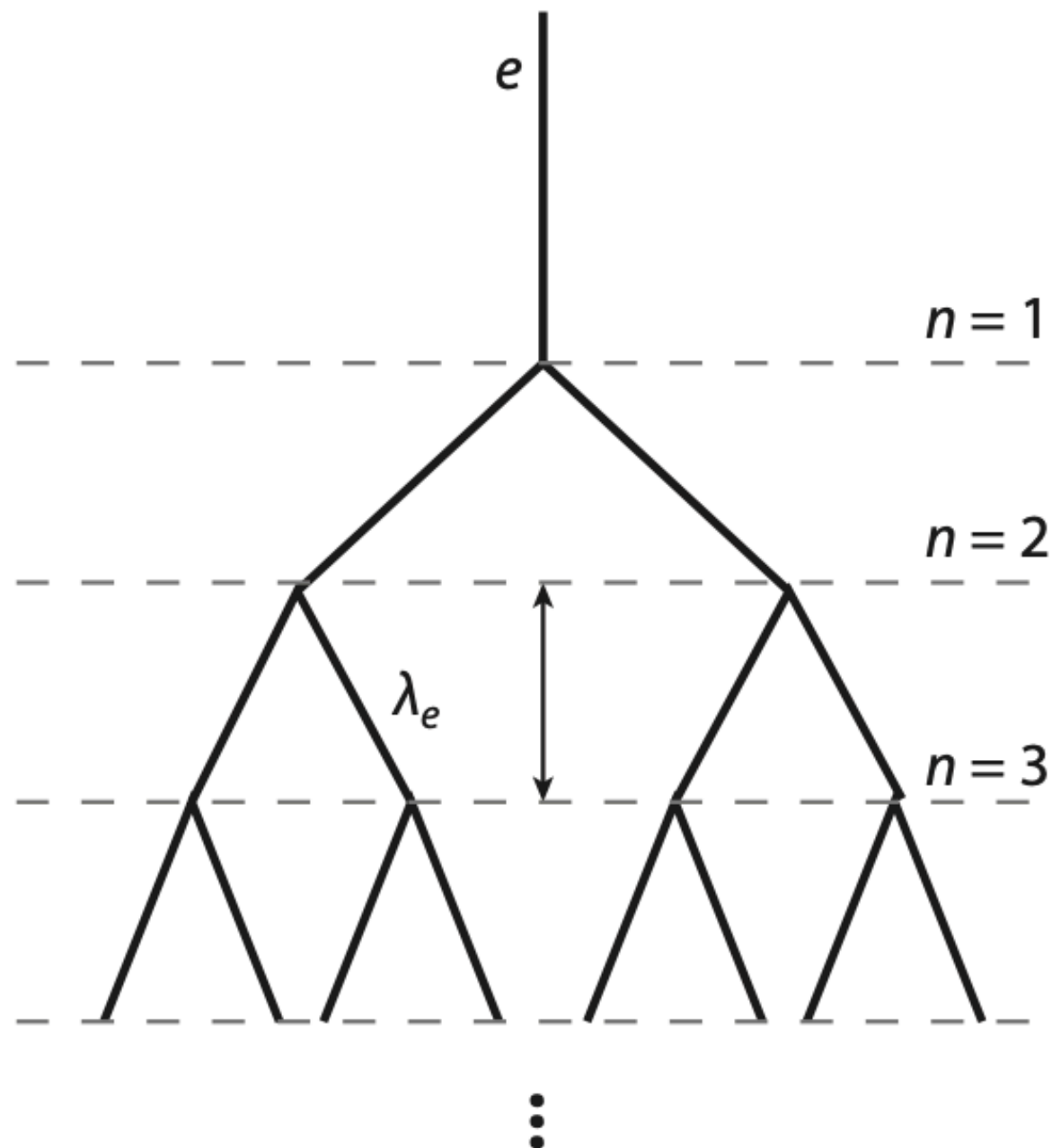
$$\begin{aligned} N_{max} &= 2^n \\ &= 2^{\log_2 E/E_c} \\ &= E/E_c \end{aligned}$$

Shower maximum at

$$X_{max} \propto X_0 \log \frac{E}{E_C}$$

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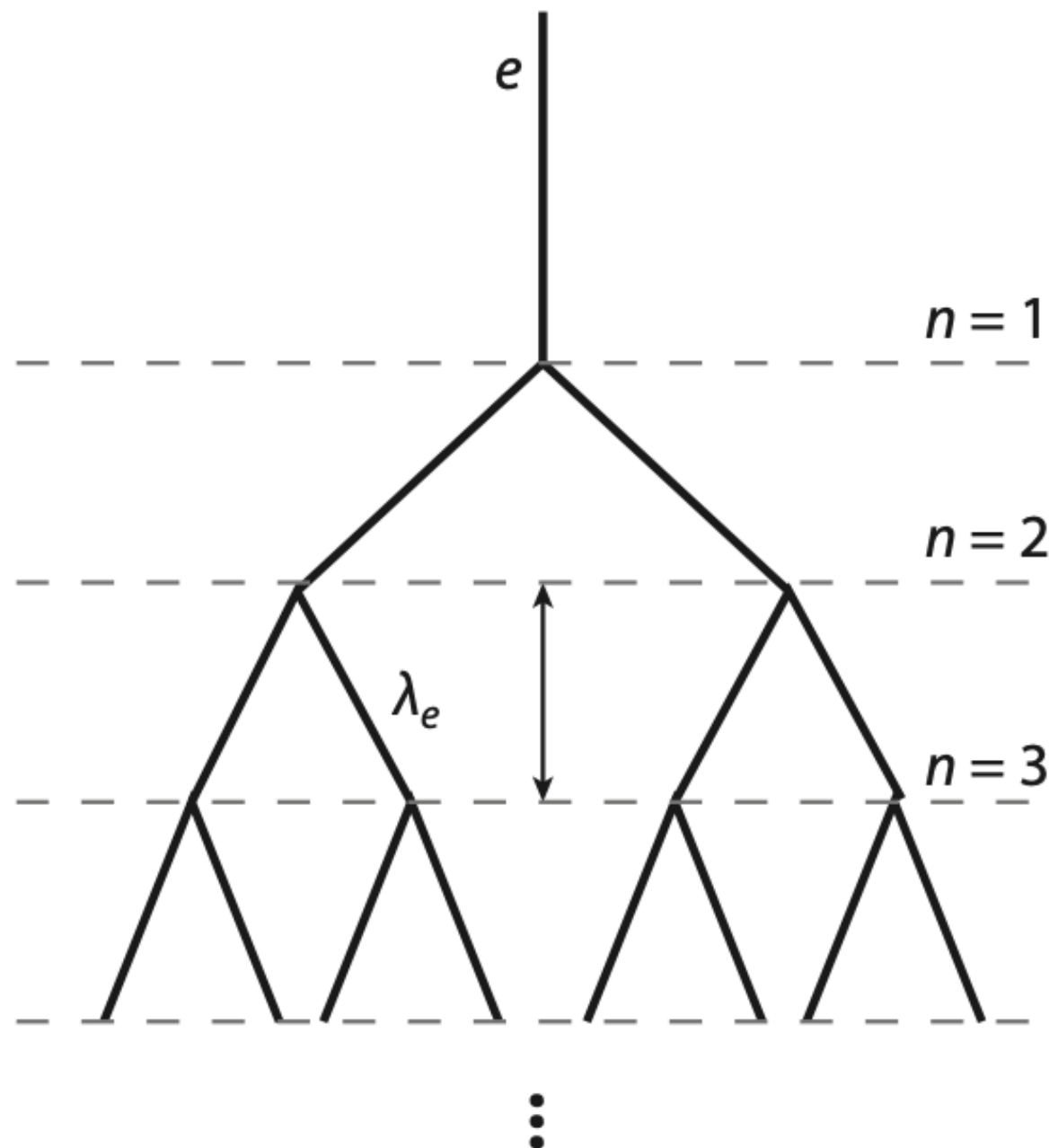
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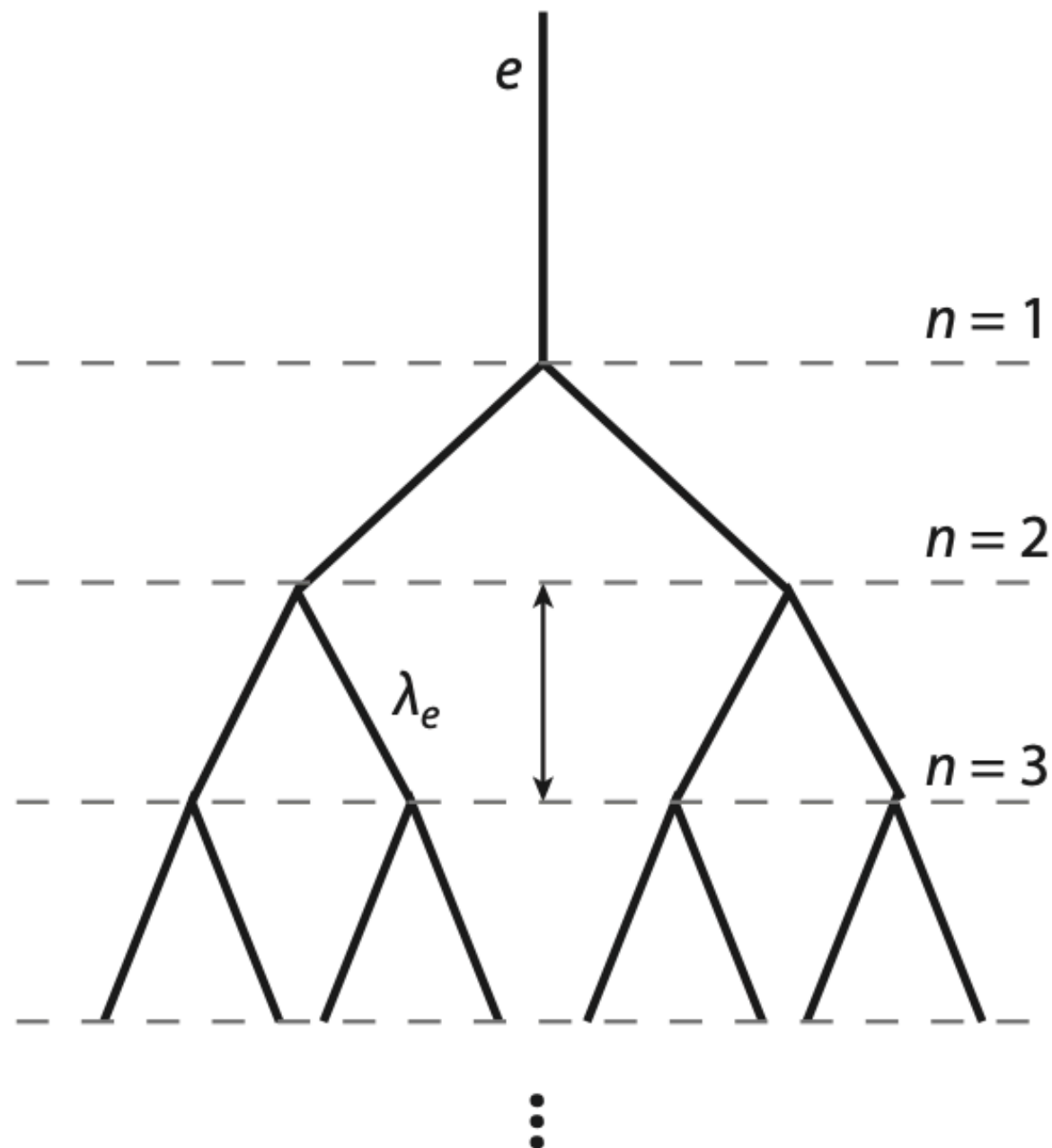
Surprisingly good:

- $X_{\max}$  predictions quite good
- $e/\gamma$  assumed to be 2, in reality closer to  $1/6$

Why is it a simplification?

# Heitler model.

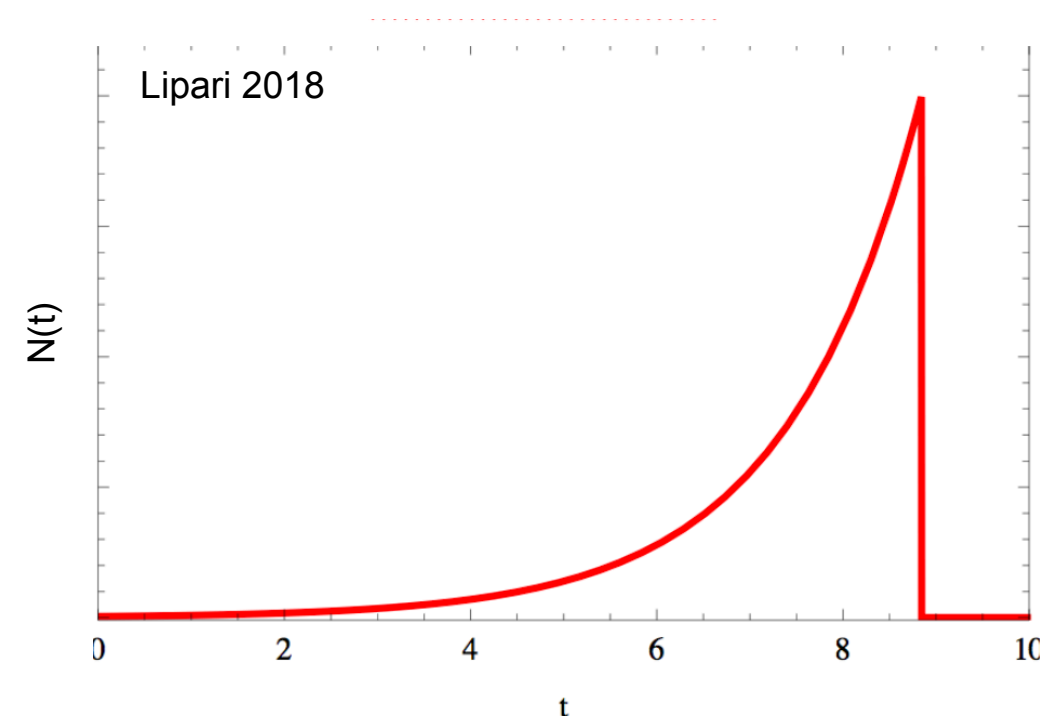
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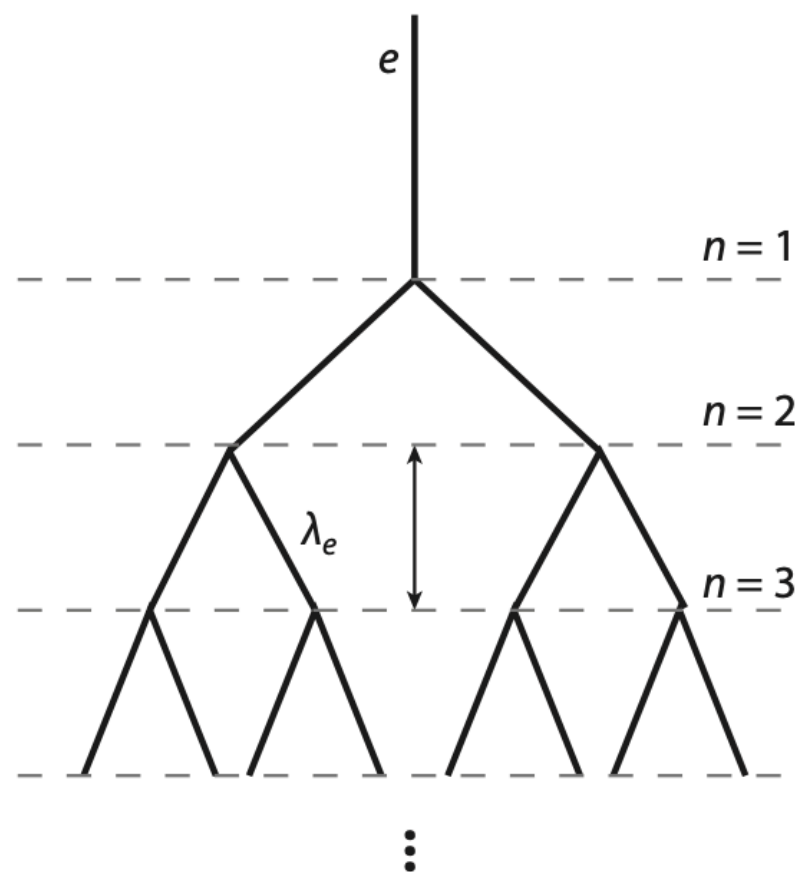
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- initial energy  $E$
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- characteristic splitting length  $X_0$
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Why is it a simplification?



# Heitler model. Simplifications.

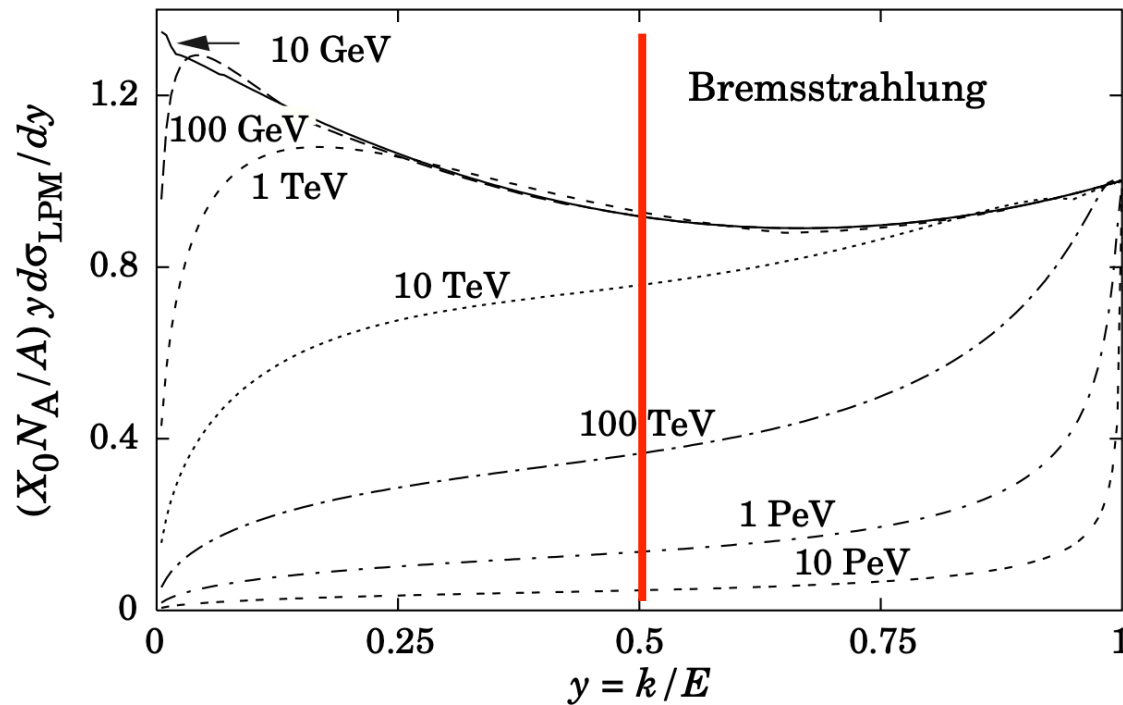
- particle interactions are stochastic processes
- atmosphere is complicated (e.g., density profile)
- analytical solutions insufficient -> Monte Carlo Methods



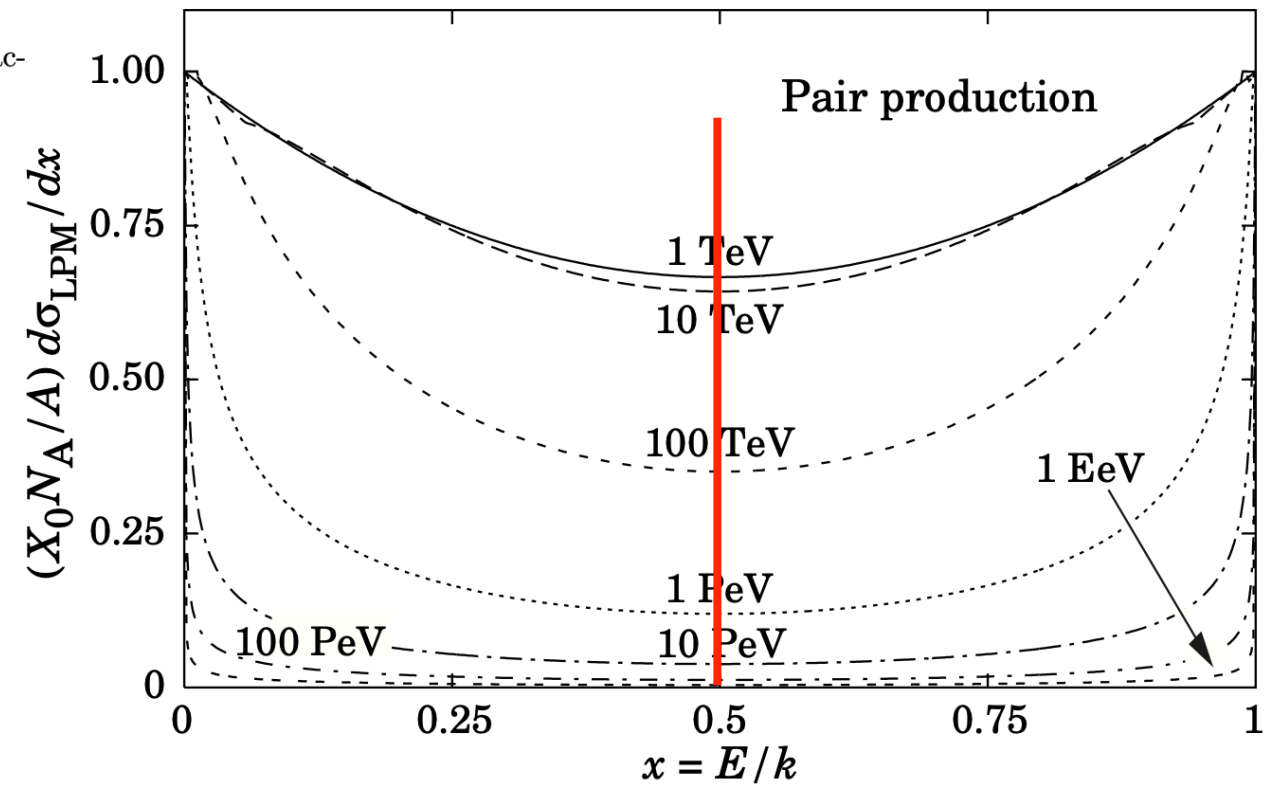
## Simplification (what is wrong):

- ✗ one "electron-photon" particle
- ✓ initial energy  $E$
- ✗ any interaction leads to two new particles of energy  $E/2$
- ✗ characteristic splitting length  $X_0$
- ✗ critical energy  $E_c$

# Any interaction leads to two new particles with $E/2$ ?

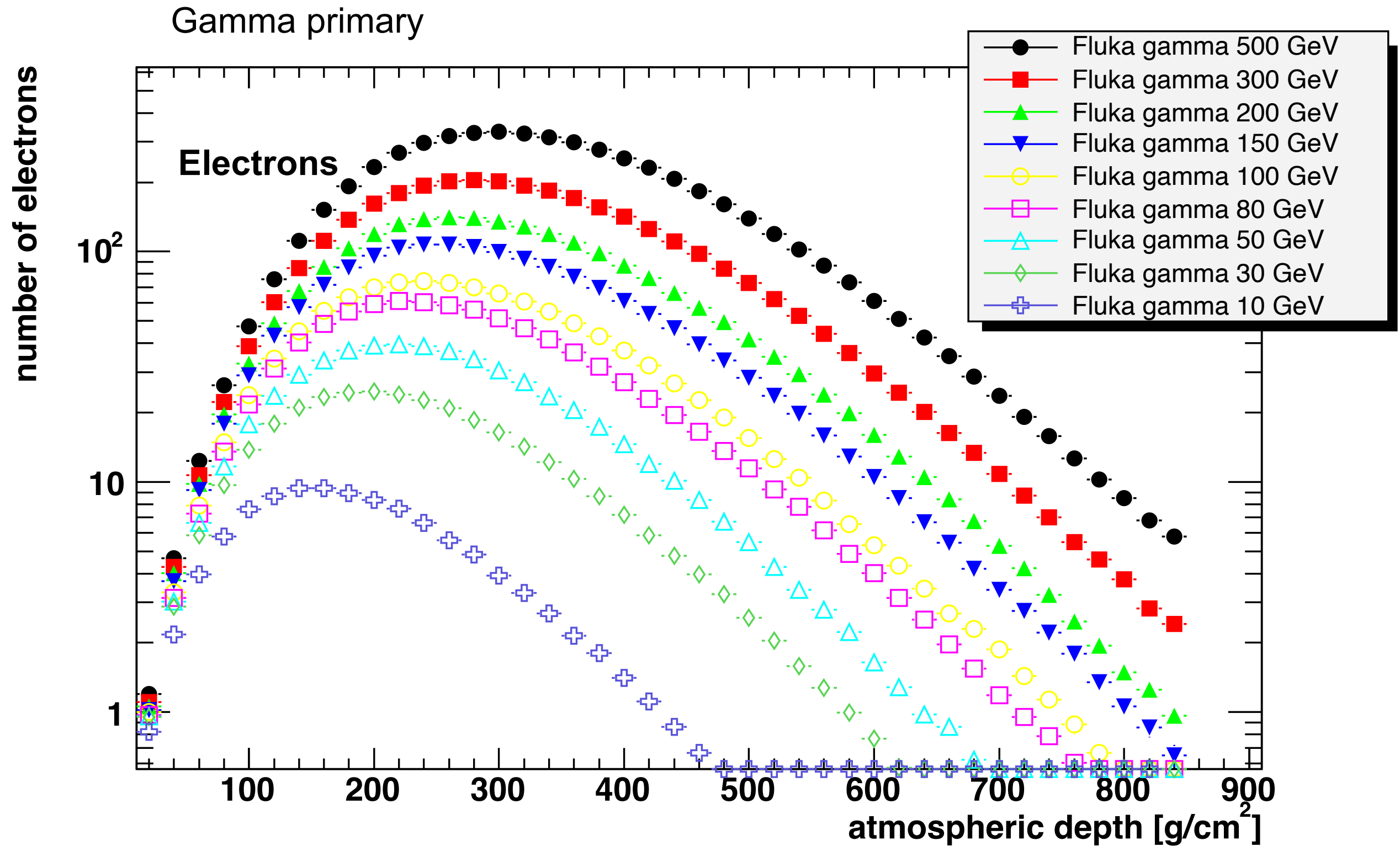


**Figure 34.12:** The normalized bremsstrahlung cross section  $k d\sigma_{LPM}/dk$  in lead versus the fractional photon energy  $y = k/E$ . The vertical axis has units of photons per radiation length.



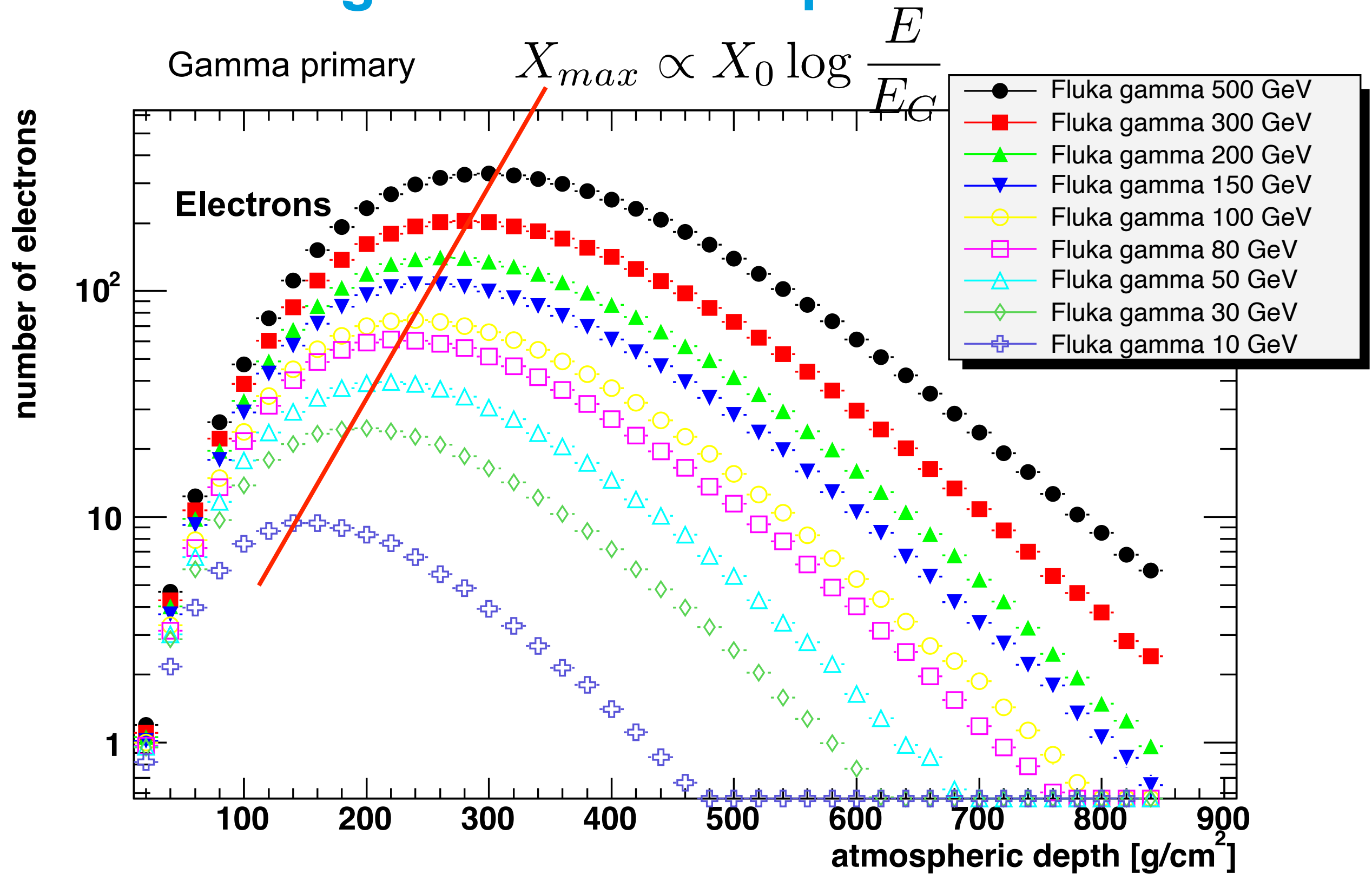
**Figure 34.18:** The normalized pair production cross section  $d\sigma_{LPM}/dx$ , versus fractional electron energy  $x = E/k$ .

# Electron longitudinal development.

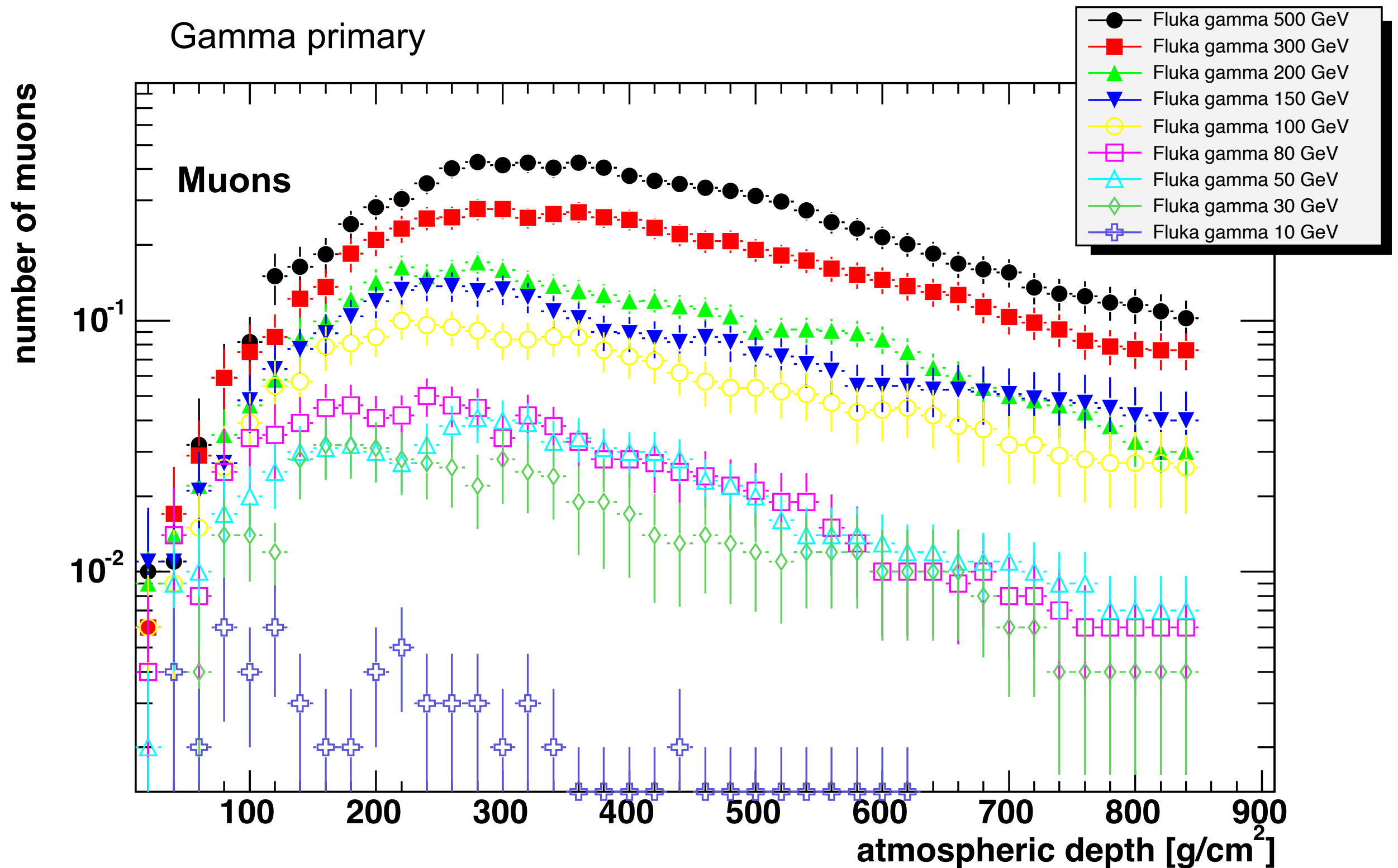




# Electron longitudinal development.



# Non-EM particles in gamma-ray showers.



Pair production cross section with  $1/\text{m}^2$  term.

# Air showers. Primary Hadrons.

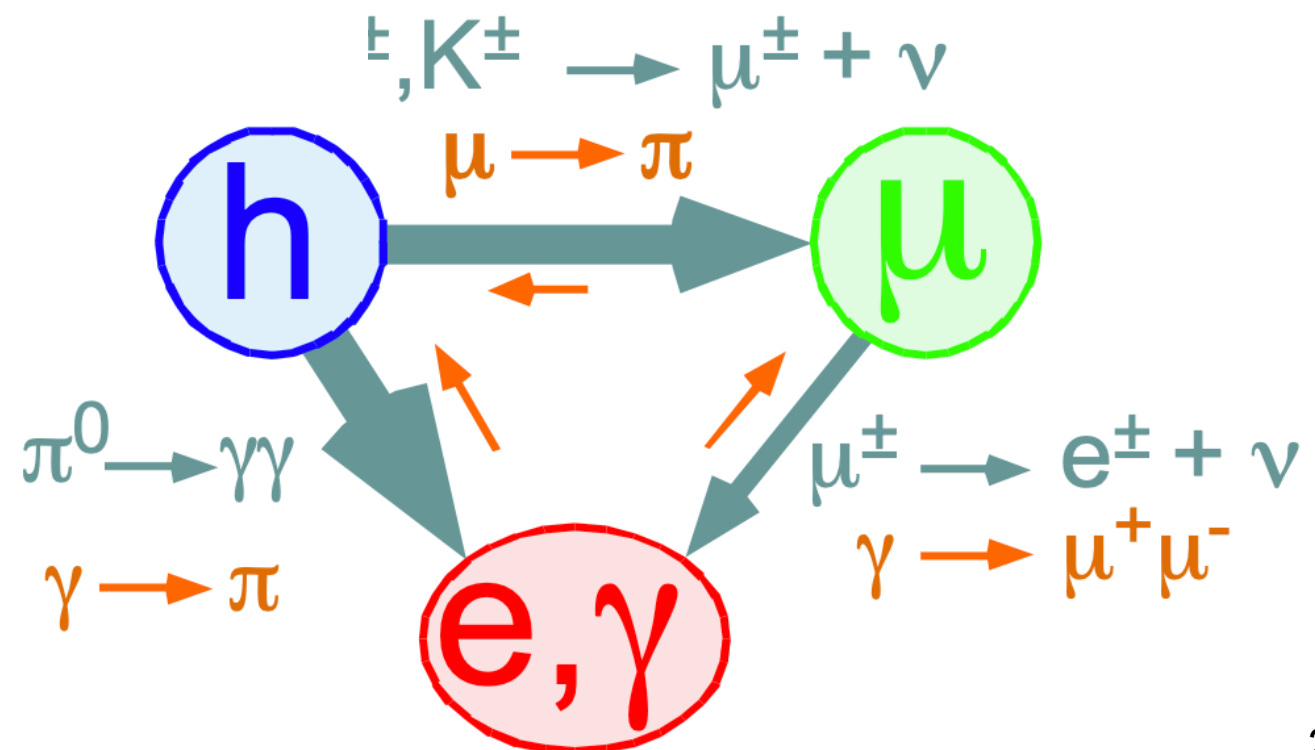
Why do we care?

# Hadronic showers.

- different secondaries, transverse momentum, resonances, QCD color flows, string fragmentation, jet production, pomerons, parton densities, ... this is complicated...
  - absolute necessity of good models (LHC!).
  - QGSJet, Epos, Sibyl, FLUKA, URQMD, ...
- basic picture from simplified model:
  - produce pions, muons,  $e^-/e^+$ ,  $\gamma$ 's

Energy flow.

J.Knapp 2017

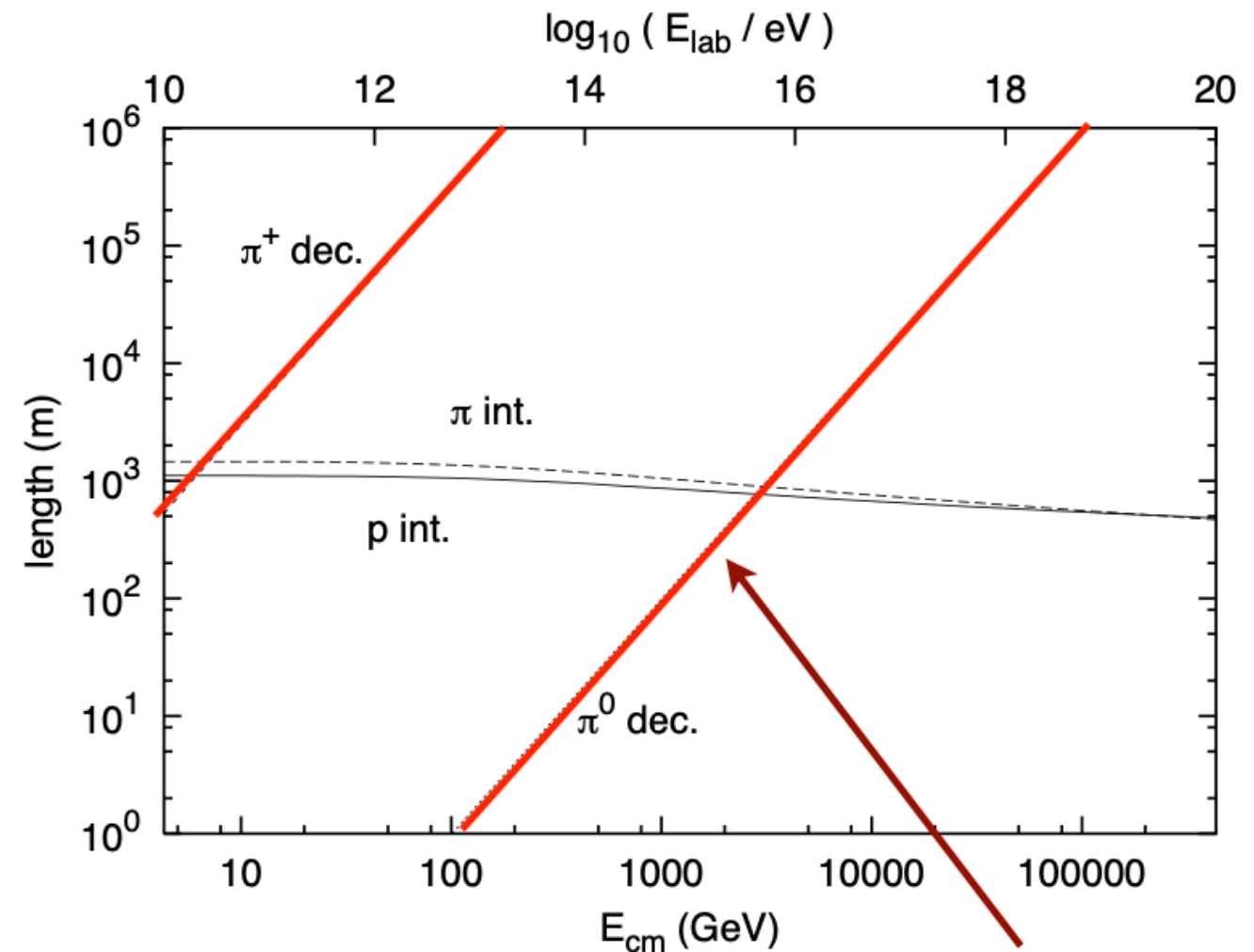


# Pions - decay vs interaction.

Slide from Ralph Engel (2008)

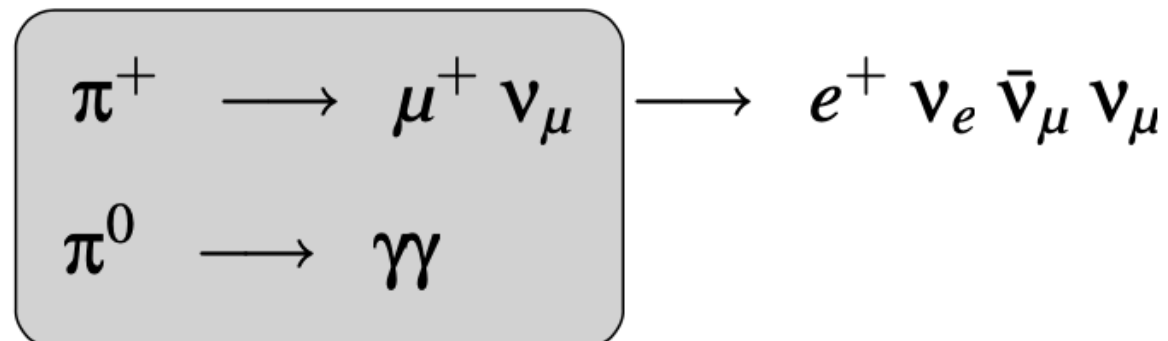
Comparison at sea level

$$\lambda_{\text{int}} = \frac{\langle m \rangle}{\sigma_{\text{ine}}}$$



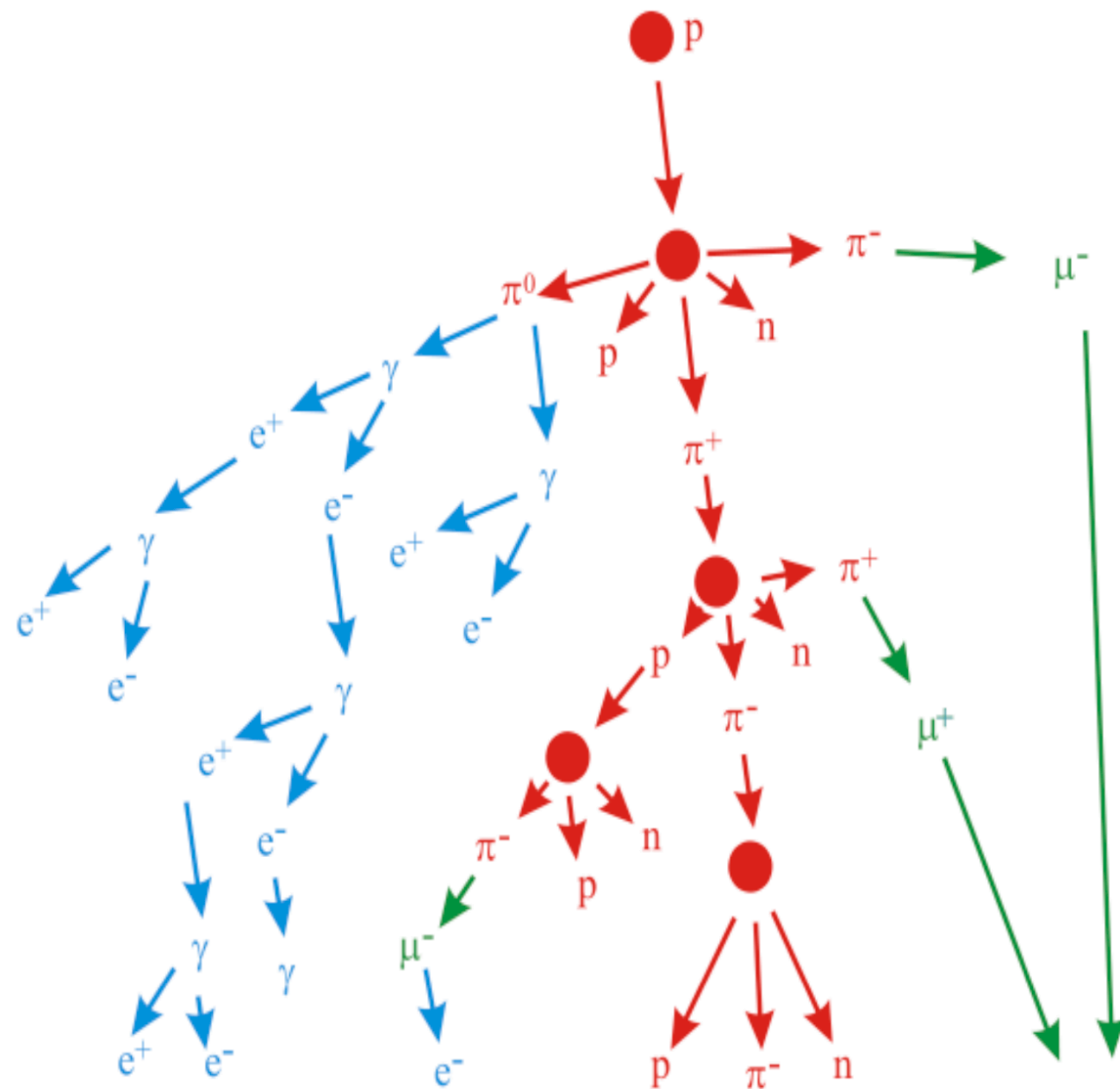
$$c\tau_{\pi^\pm} = 7.8 \text{ m}$$

$$c\tau_{\pi^0} = 25.1 \text{ ns}$$





# Heitler Matthews Model.



## Simplification:

- neutral pions decay immediately (initiate electromagnetic shower)
- charged pions interact and initiate secondary cascade
- cascade stops at  $E = E_{\text{decay}}$
- each charged pion produces one muon during decays
- muons don't interact

Can get some basic predictions, e.g.

$$N_{\mu} = \left( \frac{E_0}{\xi_{\pi}^{\pi}} \right)^{\beta} \approx 10^4 \left( \frac{E_0}{1 \text{ PeV}} \right)^{0.85}$$

$$\frac{E_{\text{em}}}{E_0} = \frac{E_0 - N_{\mu} \xi_{\pi}^{\pi}}{E_0} = 1 - \left( \frac{E_0}{\xi_{\pi}^{\pi}} \right)^{\beta-1}$$

~ 70% (at energies relevant for CTA)

from Cazon 2018

# Superposition model.

Proton-induced shower

$$N_{\max} = E_0/E_c$$

$$X_{\max} \sim \lambda_{\text{eff}} \ln(E_0)$$

$$N_{\mu} = \left( \frac{E_0}{E_{\text{dec}}} \right)^{\alpha} \quad \alpha \approx 0.9$$

**Assumption:** nucleus of mass  $A$  and energy  $E_0$  corresponds to  $A$  nucleons (protons) of energy  $E_n = E_0/A$

$$N_{\max}^A = A \left( \frac{E_0}{AE_c} \right) = N_{\max}$$

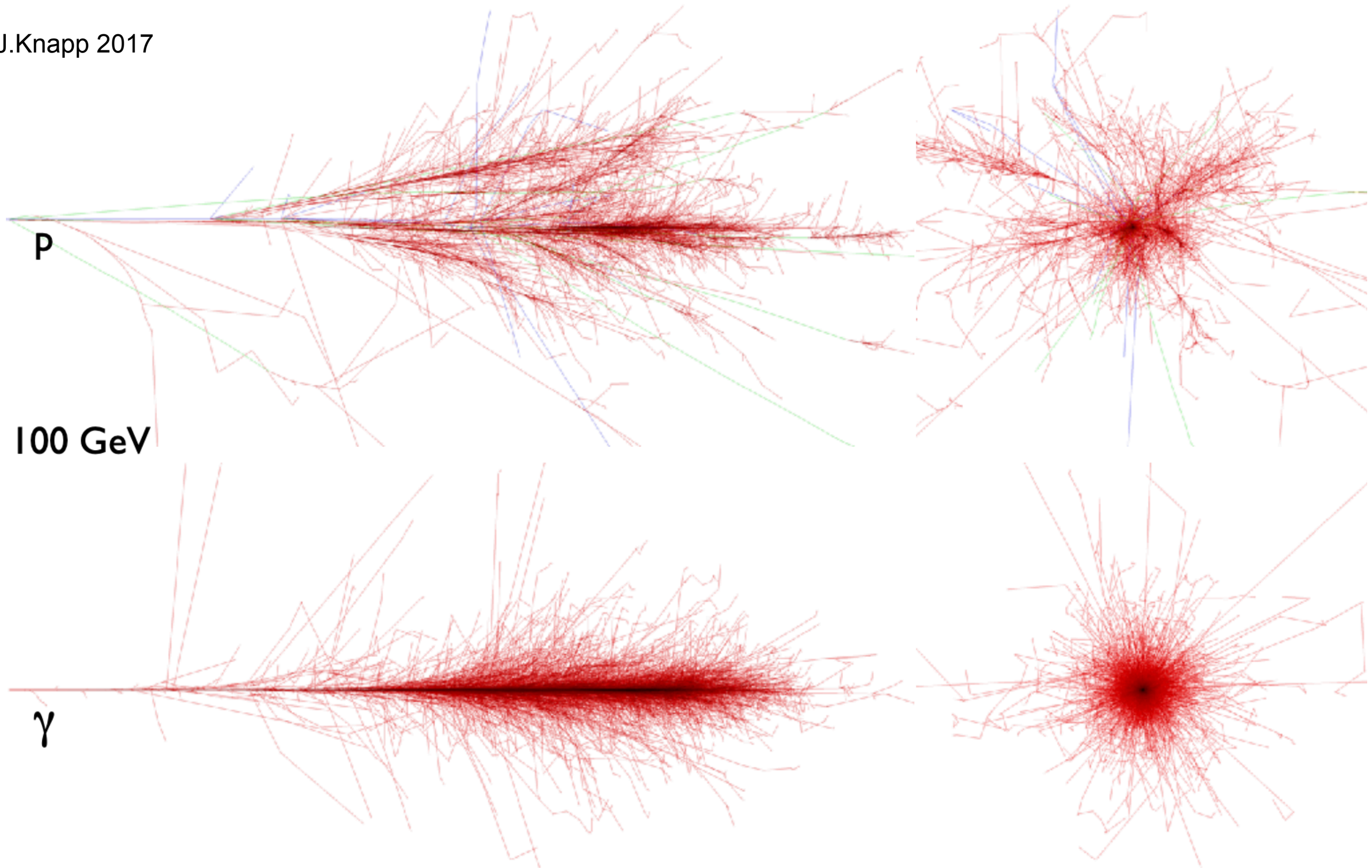
$$X_{\max}^A \sim \lambda_{\text{eff}} \ln(E_0/A)$$

$$N_{\mu}^A = A \left( \frac{E_0}{AE_{\text{dec}}} \right)^{\alpha} = A^{1-\alpha} N_{\mu}$$

Many more muons compared to protons: He: 3.5x; Fe 37x

# Gamma vs protons.

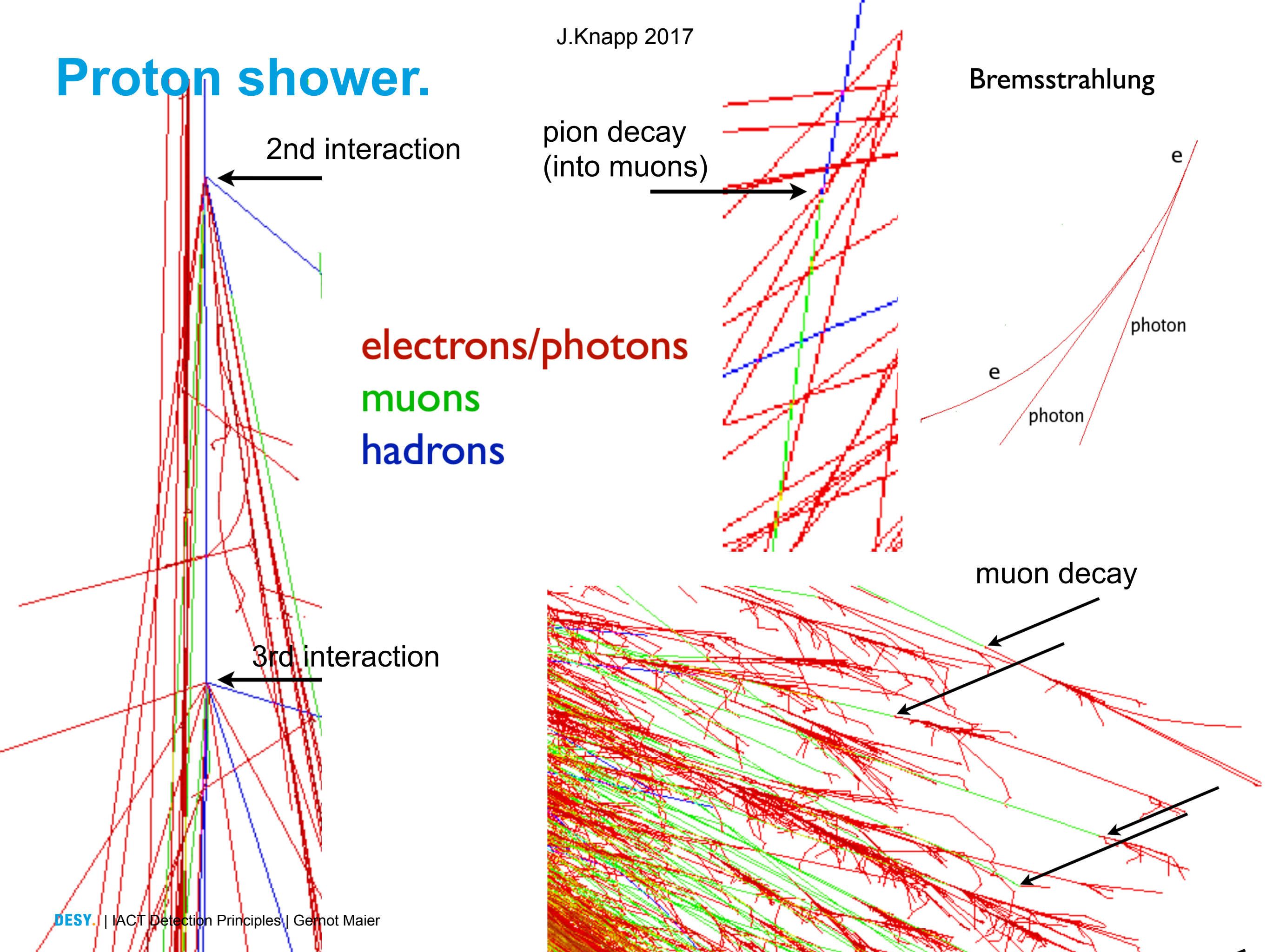
J.Knapp 2017

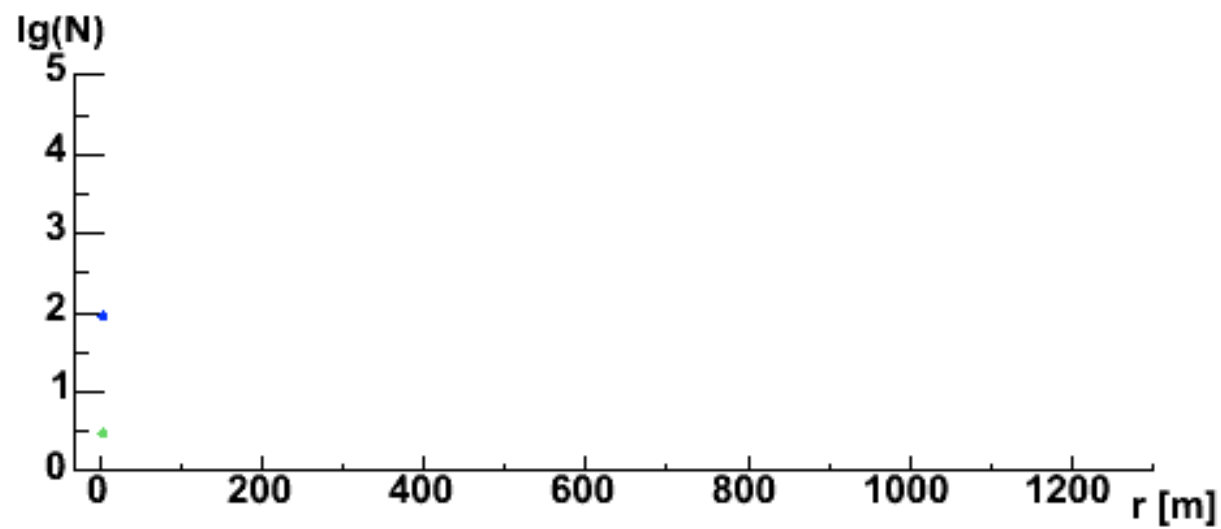
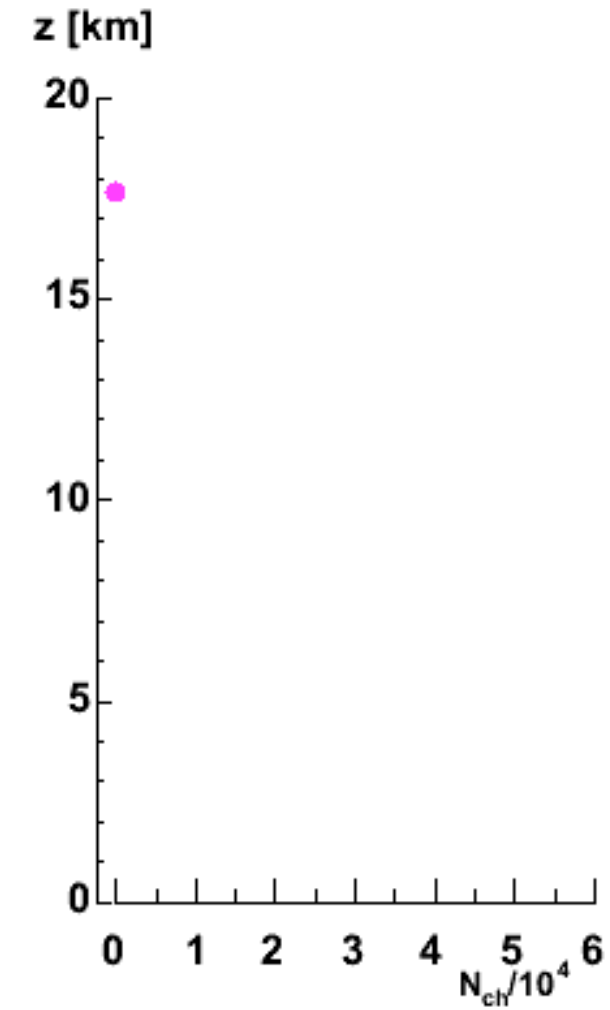
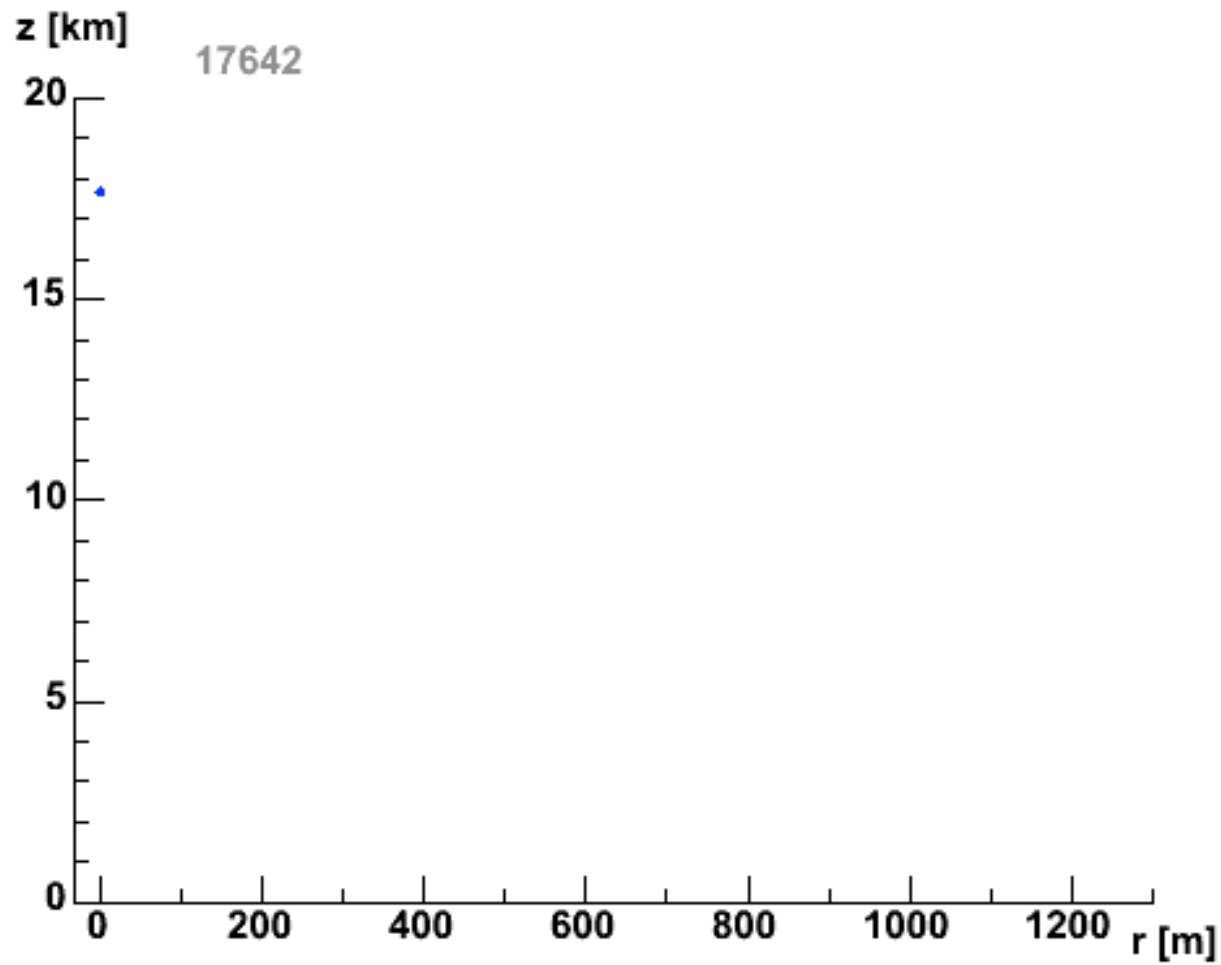




# Proton shower.

J.Knapp 2017





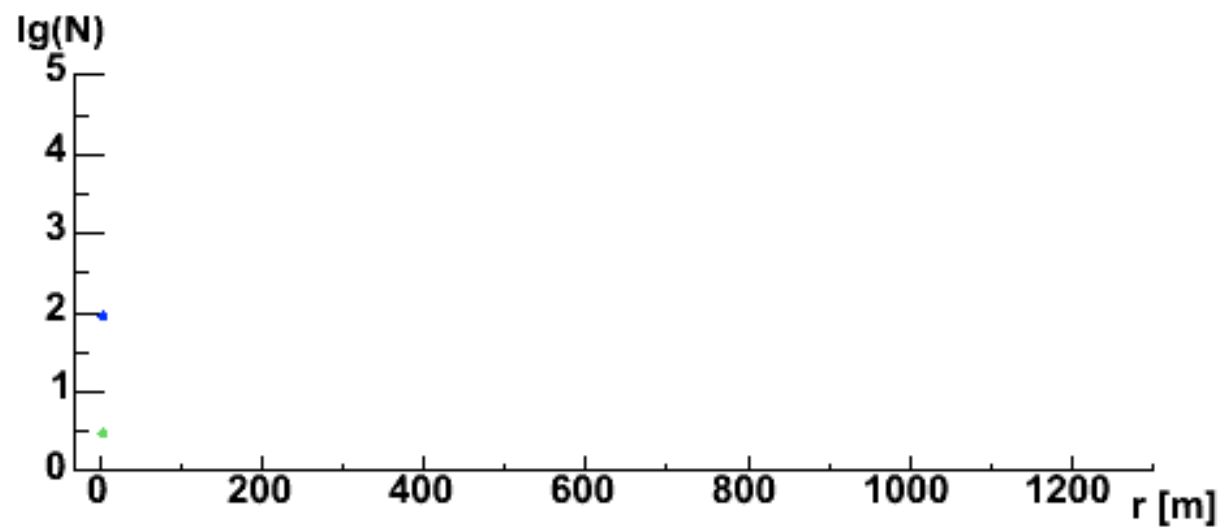
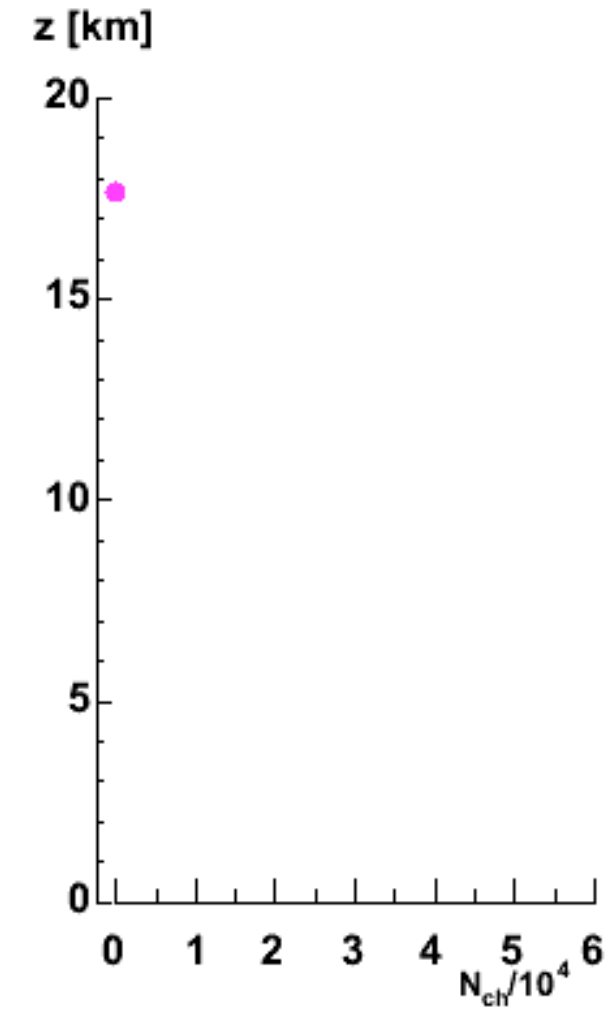
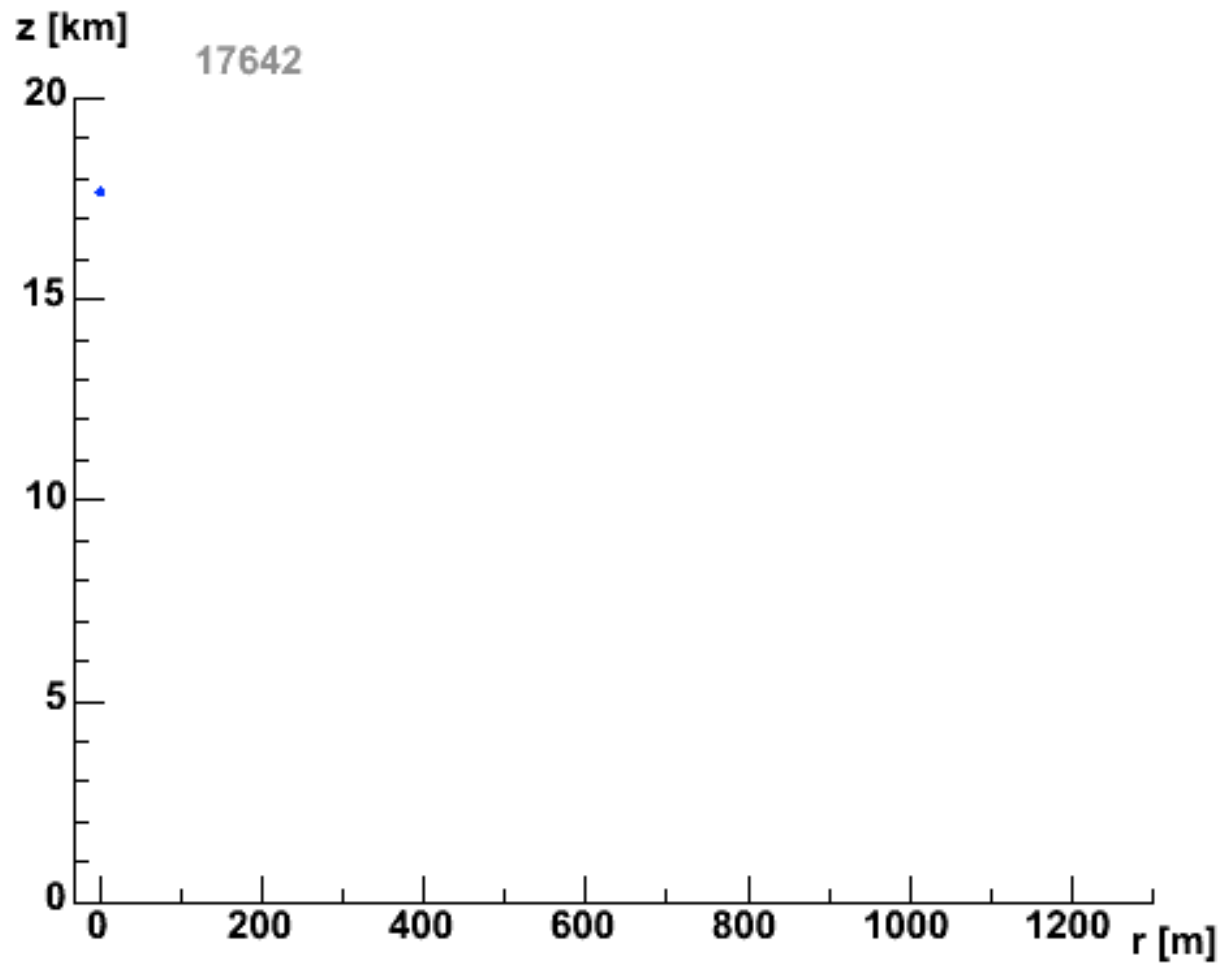
**Proton  $10^{14}$  eV**

$h^{1st} = 17642$  m

hadrons    muons

neutrons    electrs

J.Oehlschlaeger,R.Engel,FZKarlsruhe



**Proton  $10^{14}$  eV**

$h^{1st} = 17642$  m

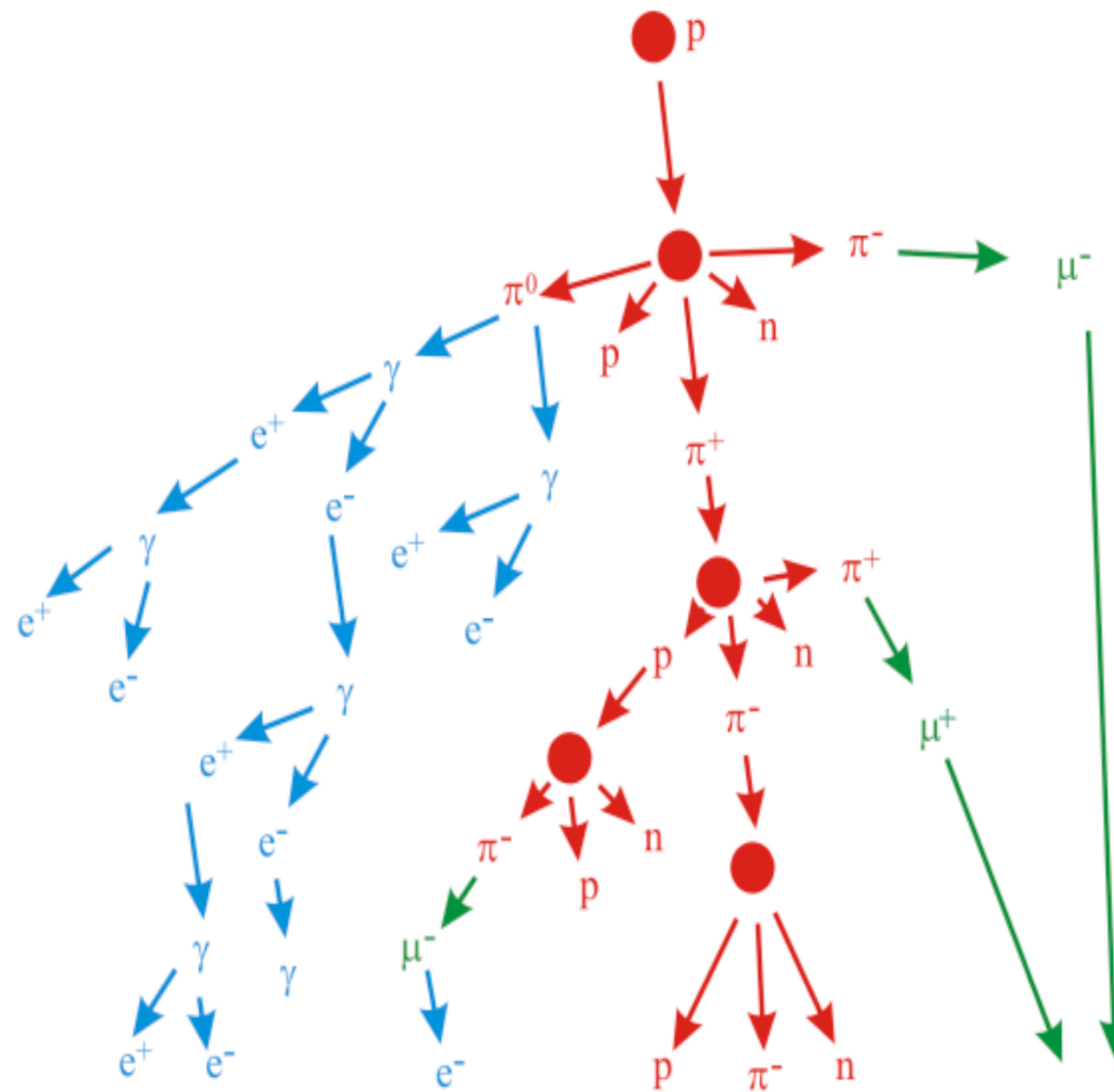
hadrons    muons

neutrons    electrs

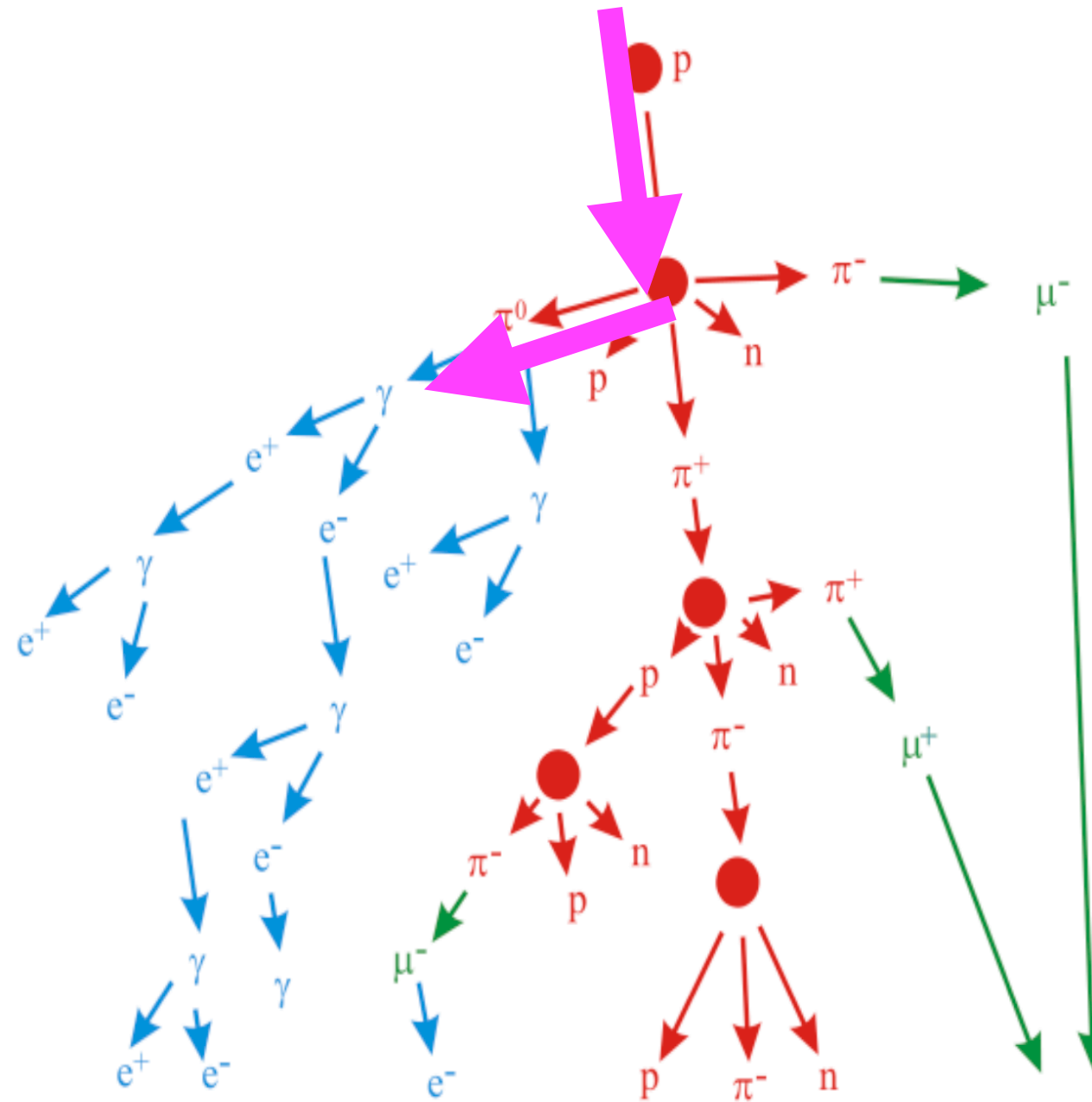
J.Oehlschlaeger,R.Engel,FZKarlsruhe



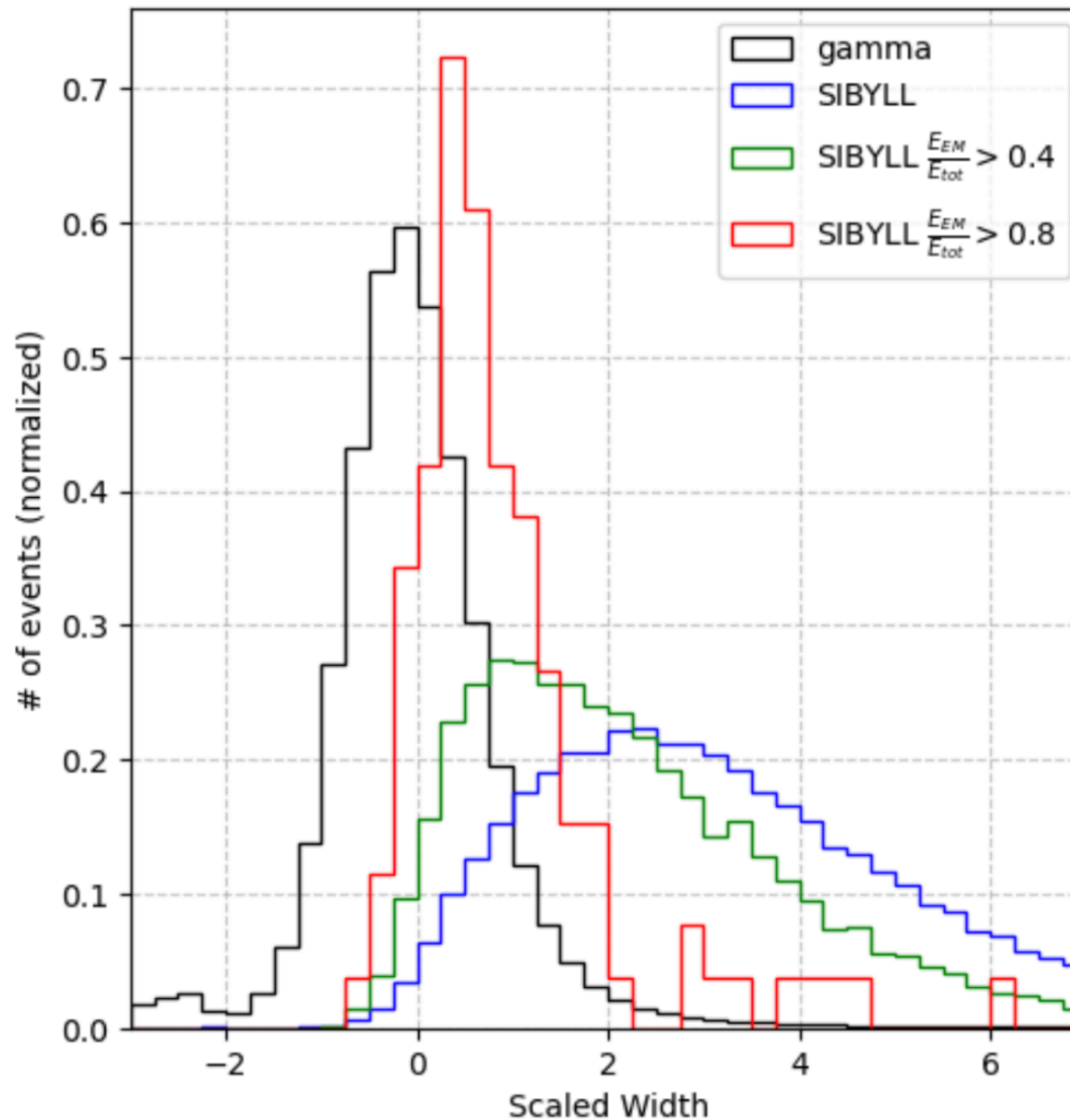
# Irreducible background from hadronic showers?



# Irreducible background from hadronic showers?



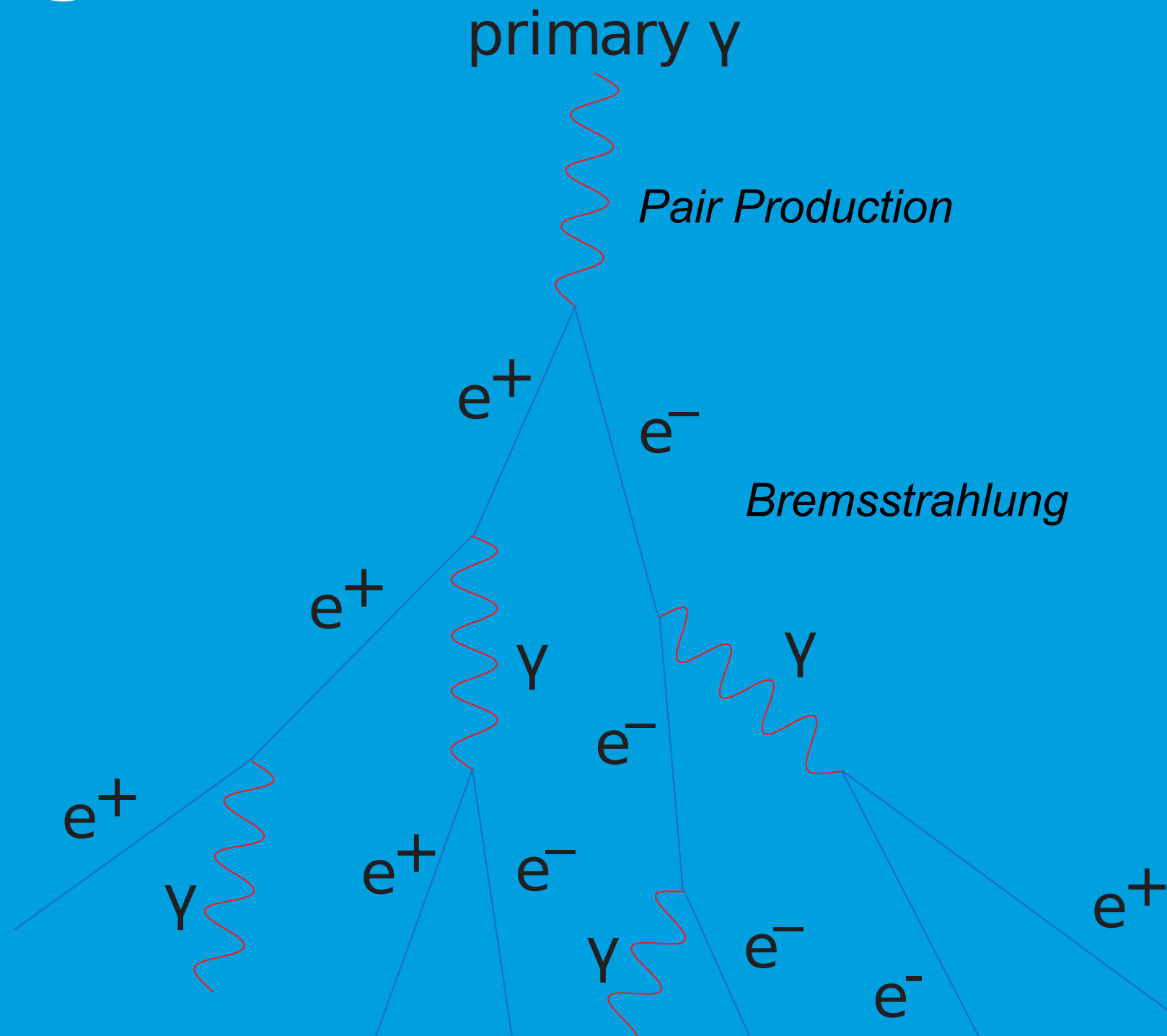
# Single Pion Dominated Events.



Dan Parsons  
(see also Maier & Knapp 2007)

# Air showers.

## Primary Electrons.



**Air showers.**

**Lateral extension.**



# Lateral extension of electromagnetic showers.

**determined by multiple Coulomb scattering**  
(and not opening angle of pair production / Bremsstrahlung)

**Scatter angle distribution not Gaussian** (as expected by central limit theorem)  
single scattering important, as cross section falls off too slowly with  $1/\theta^4$

$$\frac{d\sigma}{d\Omega}|_{Rutherford} = z^2 Z^2 \alpha^2 \hbar^2 \frac{1}{\beta^2 p^2} \frac{1}{4 \sin^4 \frac{\theta}{2}}$$

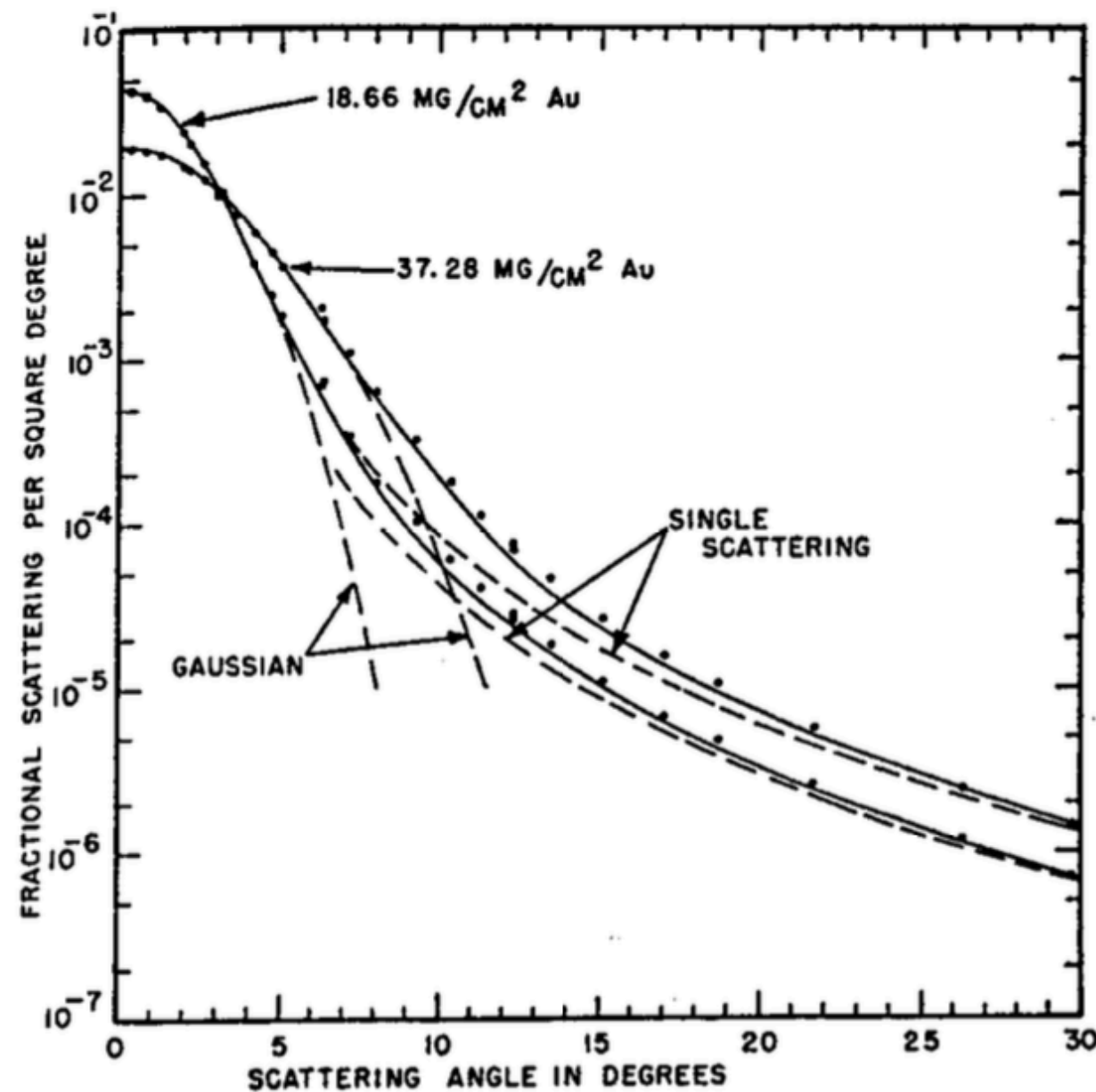
Molière's Theory for multiple scatter.

For air showers: Kamata & Nishimura (1959) and Greisen (1956)

Implementation in air shower codes non-trivial (check EGS manual on multiple scatter)

Note: different lateral distributions for each particle type (electrons, photons, ...)

# Multiple Scattering



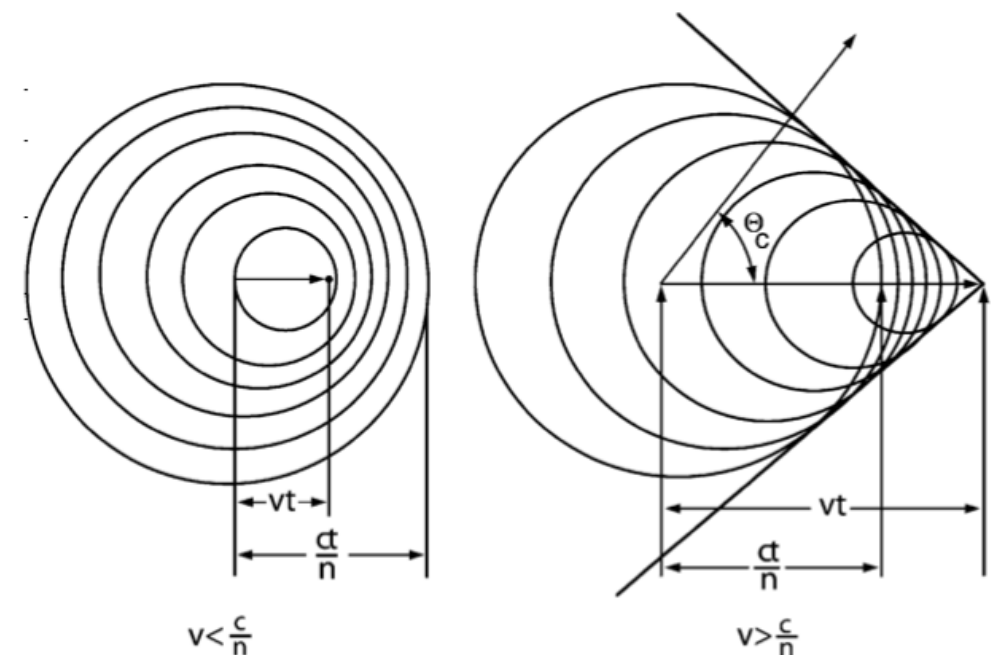
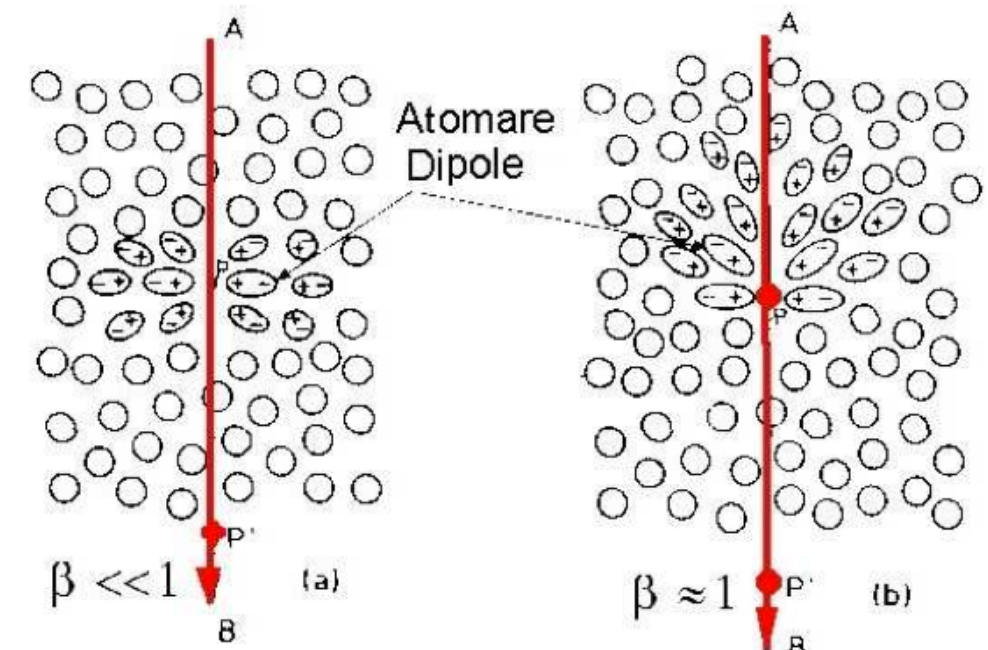
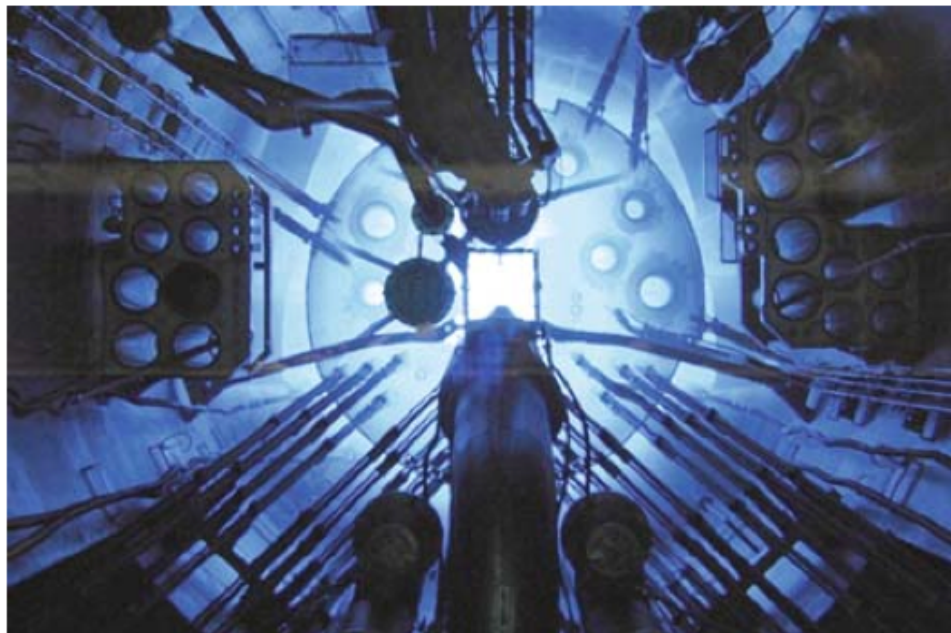
Hanson et al 1951

FIG. 3. Angular distribution of electrons from thick and thin gold foils from  $0^\circ$  to  $30^\circ$ . The solid line represents the theory of Molière extrapolated through the region where his small and large angle approximations give different values. The dotted lines at small angles represent the continuation of the gaussians of Fig. 1. At larger angles, the dotted line represents the single scattering contribution.

# Cherenkov light.

# Cherenkov Light.

- polarization of dielectric medium by charged particle
- constructive interference when particle is faster than the emitted radiation ( $c/n$ )
- emission in a cone with respect to the particle direction



Cherenkov condition:  $n\beta > 1$



# Cherenkov.

You can get a Nobel prize  
for your PhD...

arXiv > physics > arXiv:1101.4535

Physics > History and Philosophy of Physics

[Submitted on 24 Jan 2011]

## The Discovery of Cherenkov Radiation and its use in the detection of extensive air showers

A A Watson

Cascades of charged particles in the atmosphere: these 'extensive air showers' are a common feature of high-energy cosmic ray arrival direction distribution.

the intensity of radiation found using a technique, called 'quenching', in which the dark-adapted eye was used with a graded wedge to provide calibration of the light intensity. These were difficult and delicate experiments requiring high levels of both patience and experimental skill. Cherenkov discovered that light was emitted even when the vessel contained only sulphuric acid, the solvent for the uranyl salt. He went on to demonstrate that the light was observed in a range of different solvents. In a moving obituary [4], which mentions only briefly Cherenkov's considerable post-war contributions to accelerator physics, Chudakov writes "The phenomenon was not and probably could not have been discovered earlier by someone more experienced in physics than Cherenkov was in the 1930s. To determine the nature of the faint blue light produced in different liquids by gamma rays from a radioactive source seemed to require a young fellow from a rural area, inexperienced but with immense patience and vigour".

Observation of polarization was an important clue to the eventual interpretation but the critical breakthrough was Cherenkov's discovery in 1936 that the radiation was emitted asymmetrically only in the forward direction with respect to the direction of the incoming  $\gamma$ -ray beam [5], at an angle

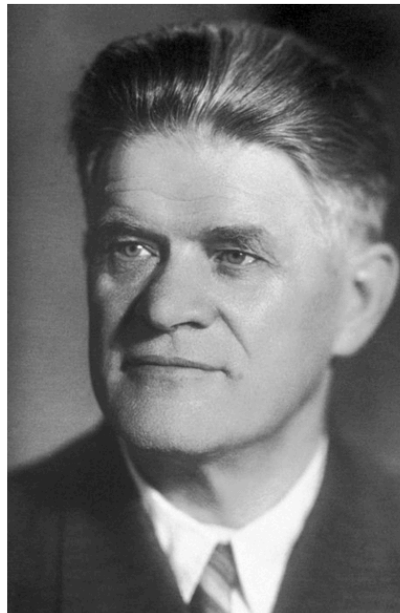


Photo from the Nobel Foundation archive.

Pavel Alekseyevich Cherenkov  
The Nobel Prize in Physics 1958

Born: 28 July 1904, Novaya Chigla, Russia

Died: 6 January 1990, USSR (now Russia)

Affiliation at the time of the award: P.N. Lebedev Physical Institute, Moscow, USSR (now Russia)

Prize motivation: "for the discovery and the interpretation of the Cherenkov effect"

Prize share: 1/3

# Cherenkov emission.

What you absolutely need to know.

Cherenkov condition:  $n\beta > 1$

light is emitted along a cone with half opening angle  $\theta$ :  $\cos \Theta = \frac{1}{n\beta}$

good approximation:  $\Theta_c \approx \sqrt{2(n-1)}$  radians

number of Cherenkov photons per path length  $x$ :

$$\frac{dN}{dx} = 2\pi\alpha z^2 \int_{\lambda_1}^{\lambda_2} \left(1 - \frac{1}{n^2\beta^2}\right) \frac{d\lambda}{\lambda^2} = 2\pi\alpha z^2 \int_{\lambda_1}^{\lambda_2} \sin^2 \Theta \frac{d\lambda}{\lambda^2}$$

$$\beta = v/c$$

$n$  = refractive index

$z$  = charge

$\lambda$  = wavelength

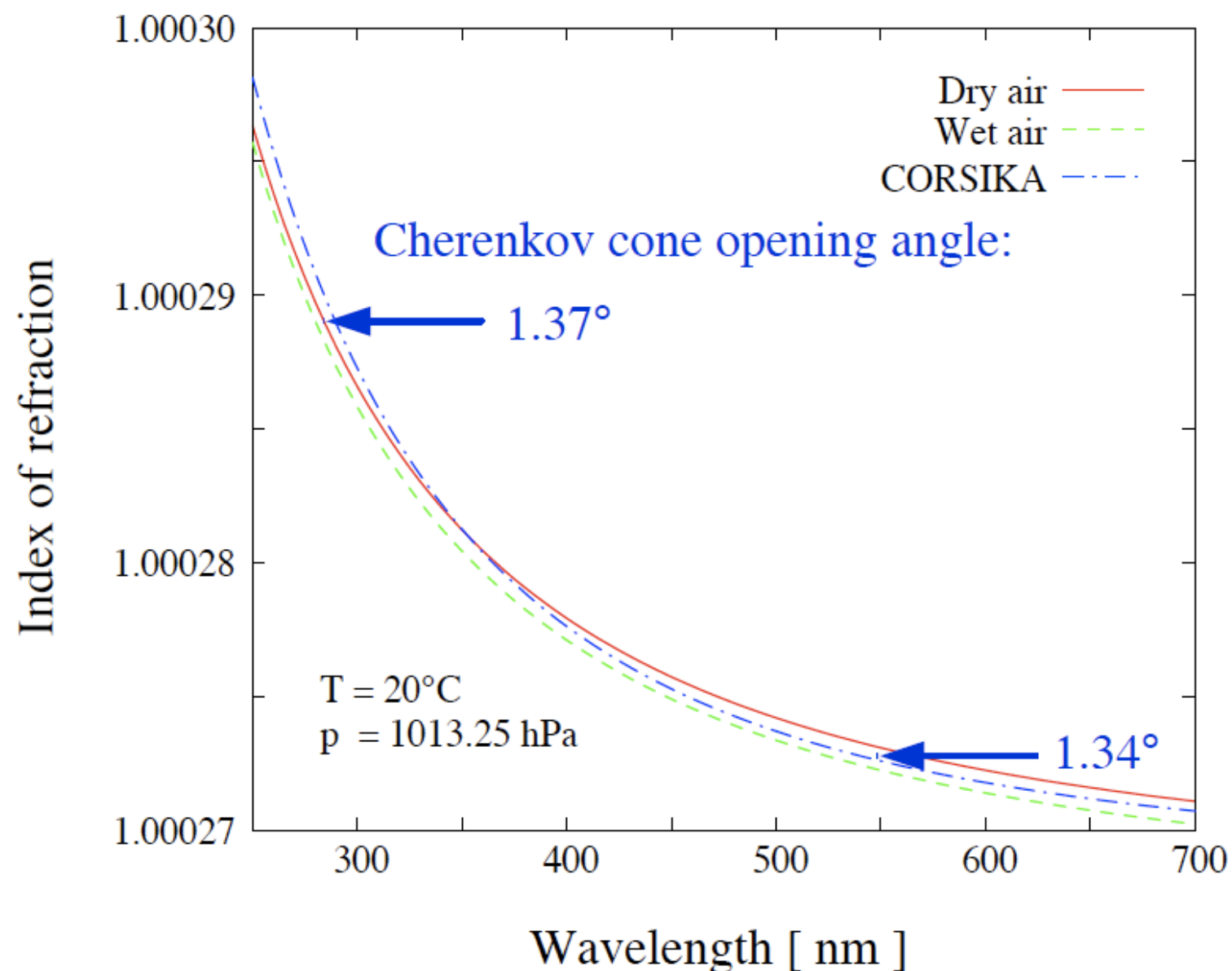
$$\alpha = 1/137$$



# Index of refraction.

refractive index in air scales with density:  $n = 1 + 0.000283 \rho(h)/\rho(0)$

(additional dependency on pressure, temperature, water vapor content)



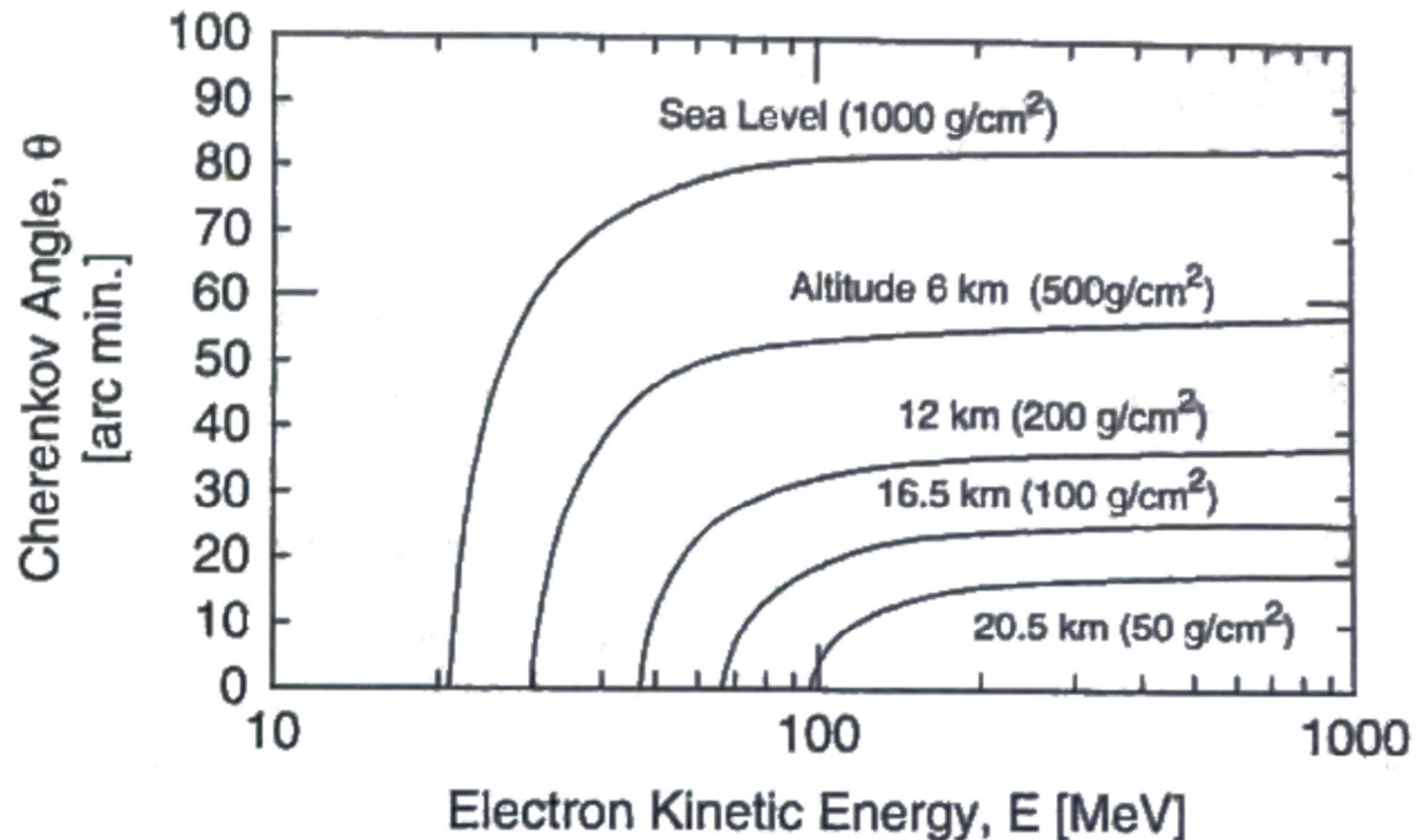
Current simulations use  $n(450 \text{ nm})$ .

# Cherenkov angle vs electron energy

Thresholds for Cherenkov emission:

Electrons: 20 MeV at sea level / 35 MeV at 10 km

Muons: 4.5 GeV at sea level / 8 GeV at 10 km

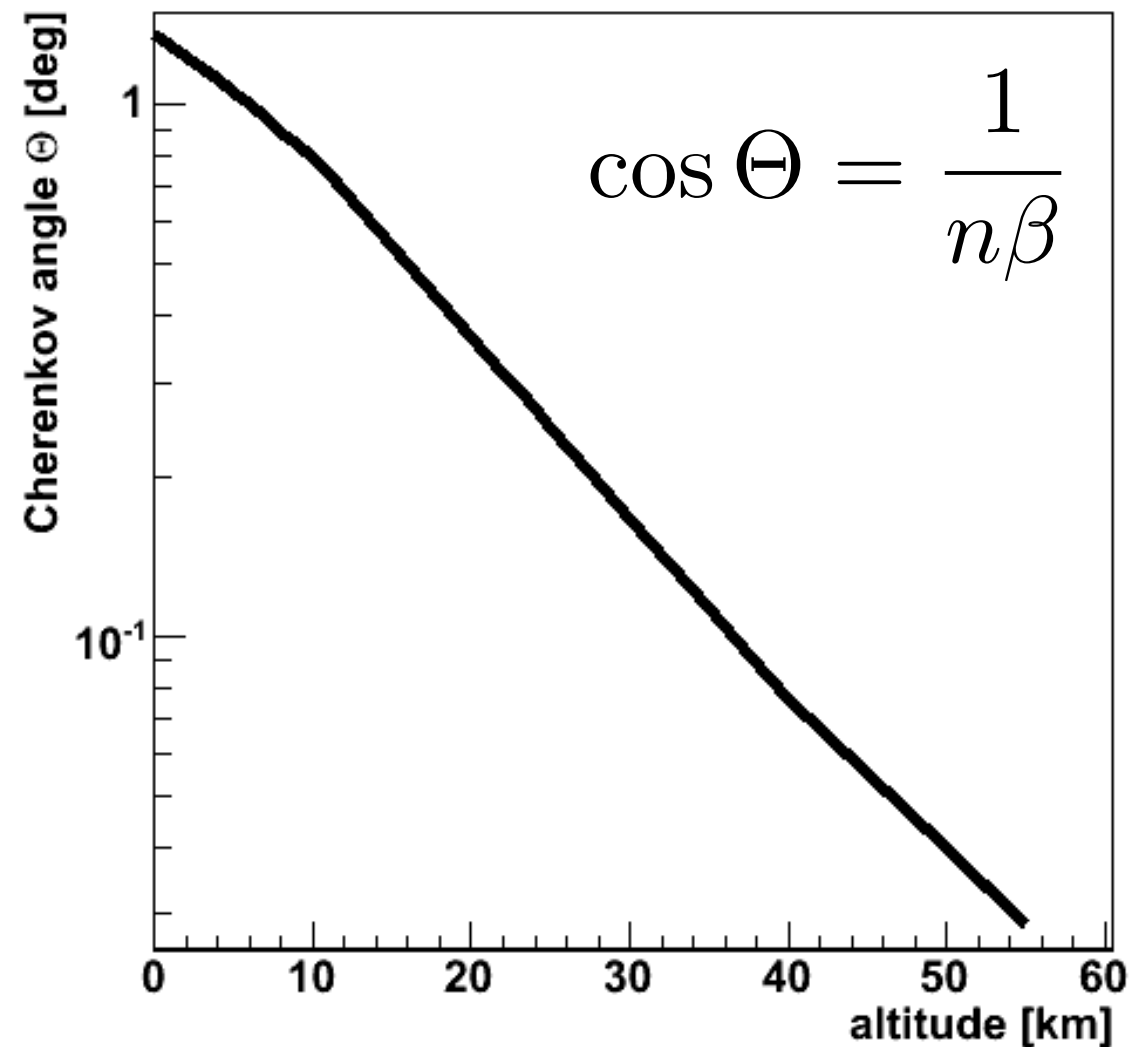
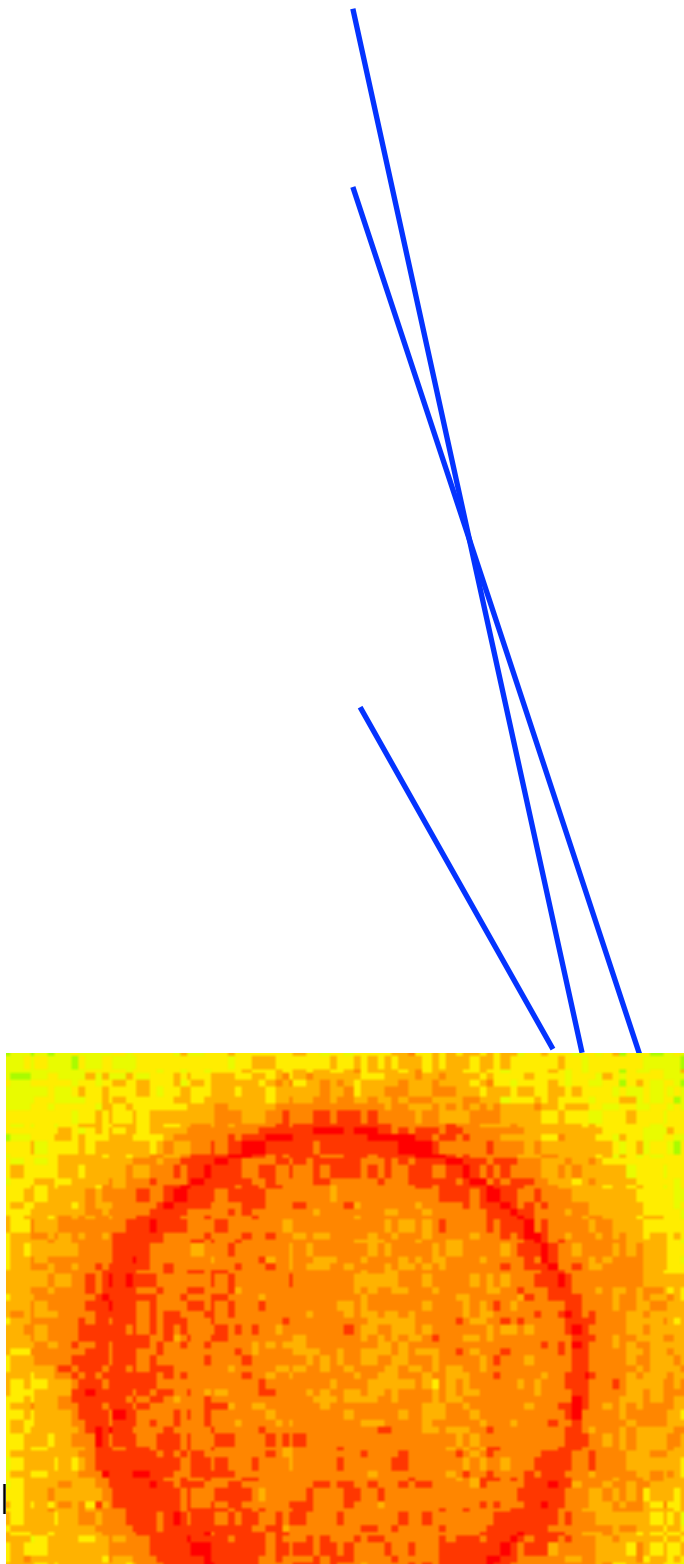


Grieder 2010.

# Cherenkov emission in the Atmosphere

refractive index in air scales with density

$$n = 1 + 0.000283 \rho(h)/\rho(0)$$

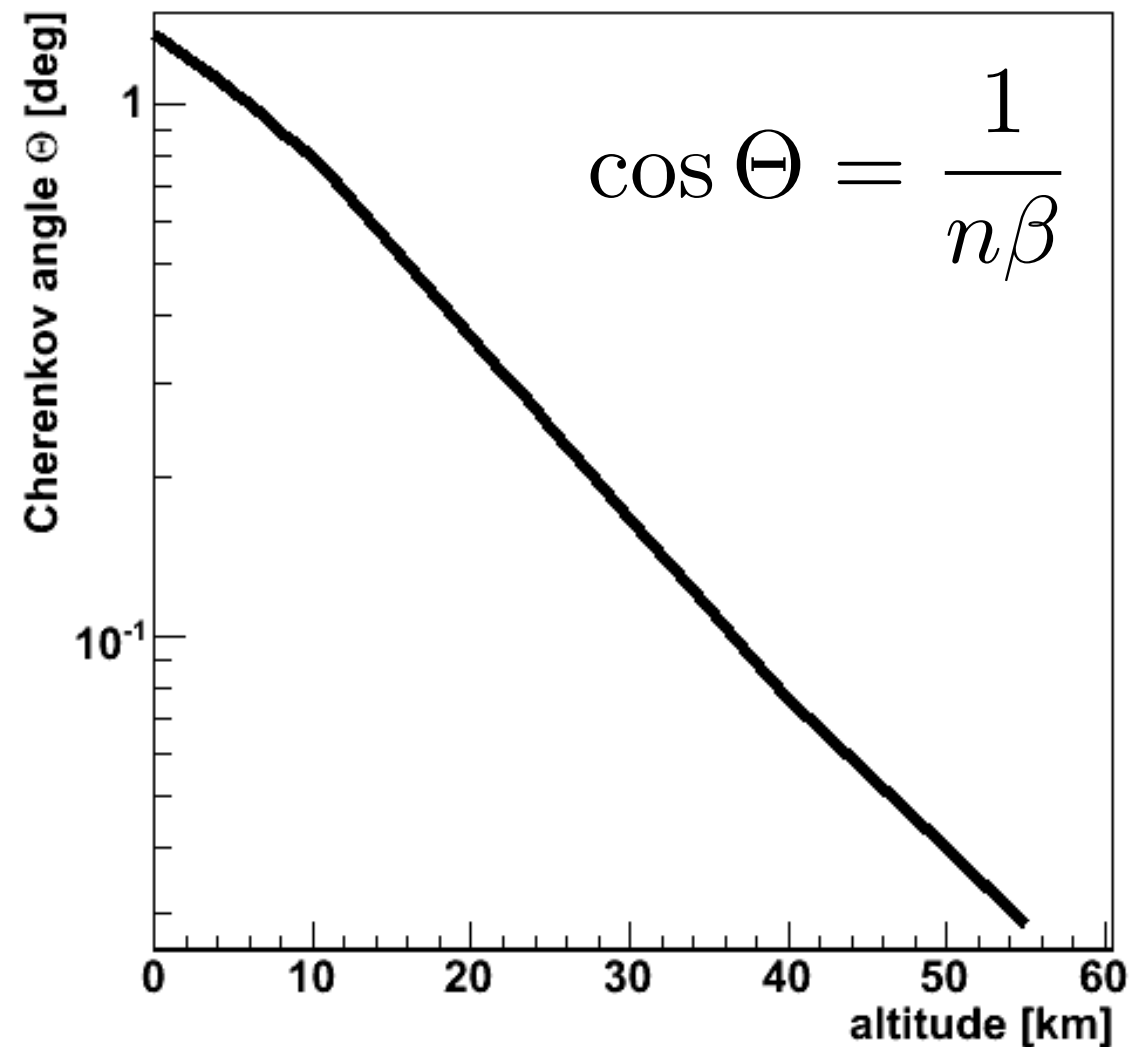
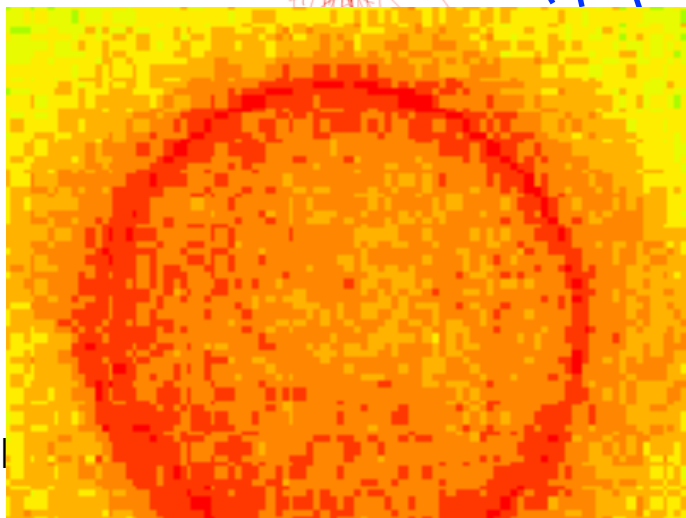
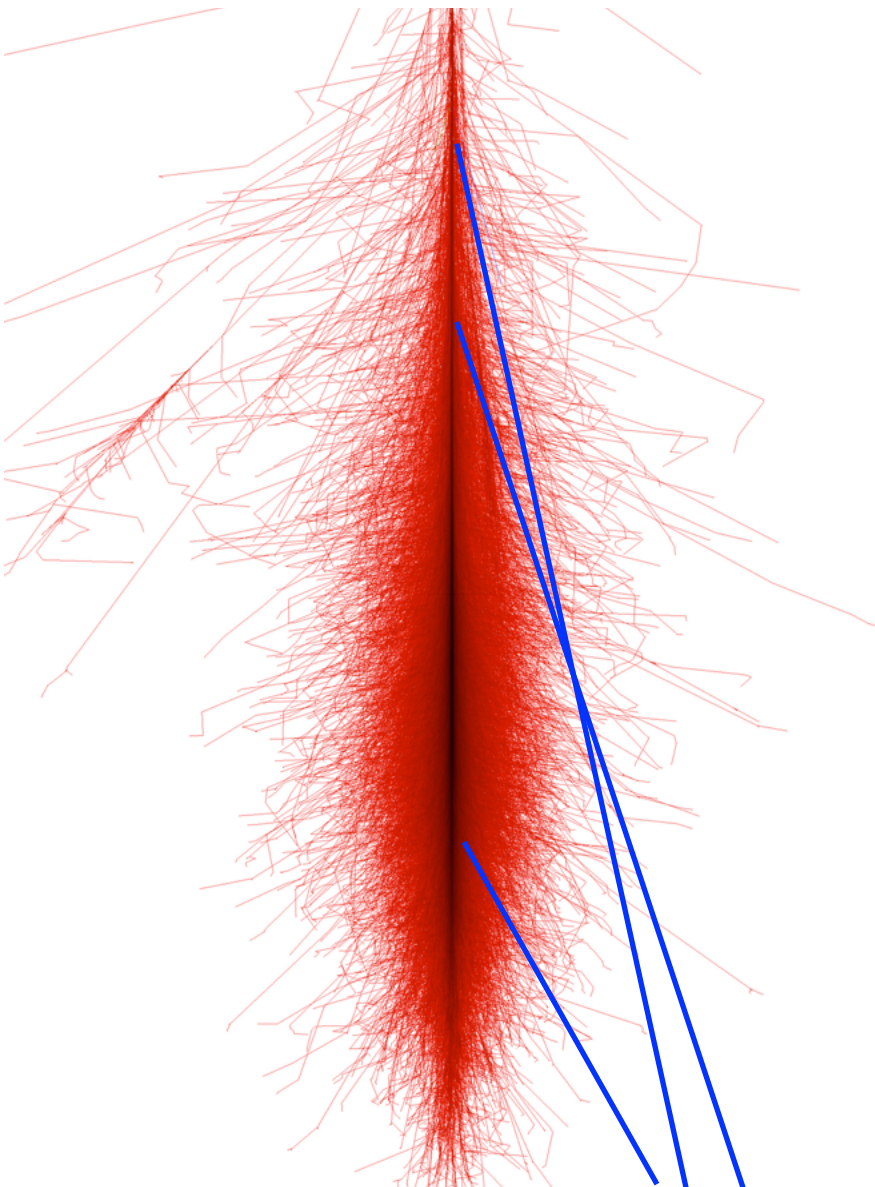


~1.3 deg at sea level

# Cherenkov emission in the Atmosphere

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$$n = 1 + 0.000283 \rho(h)/\rho(0)$$

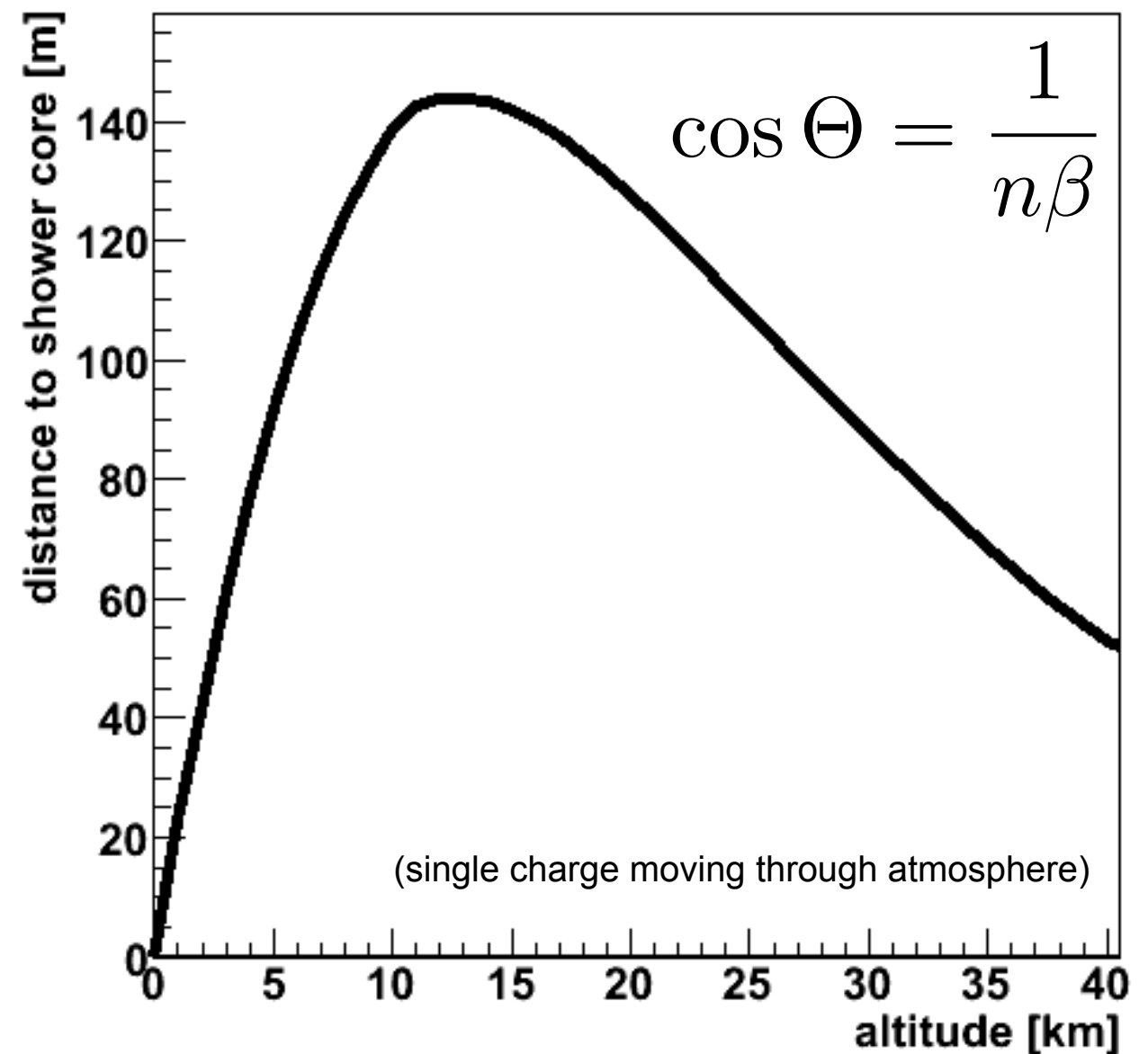
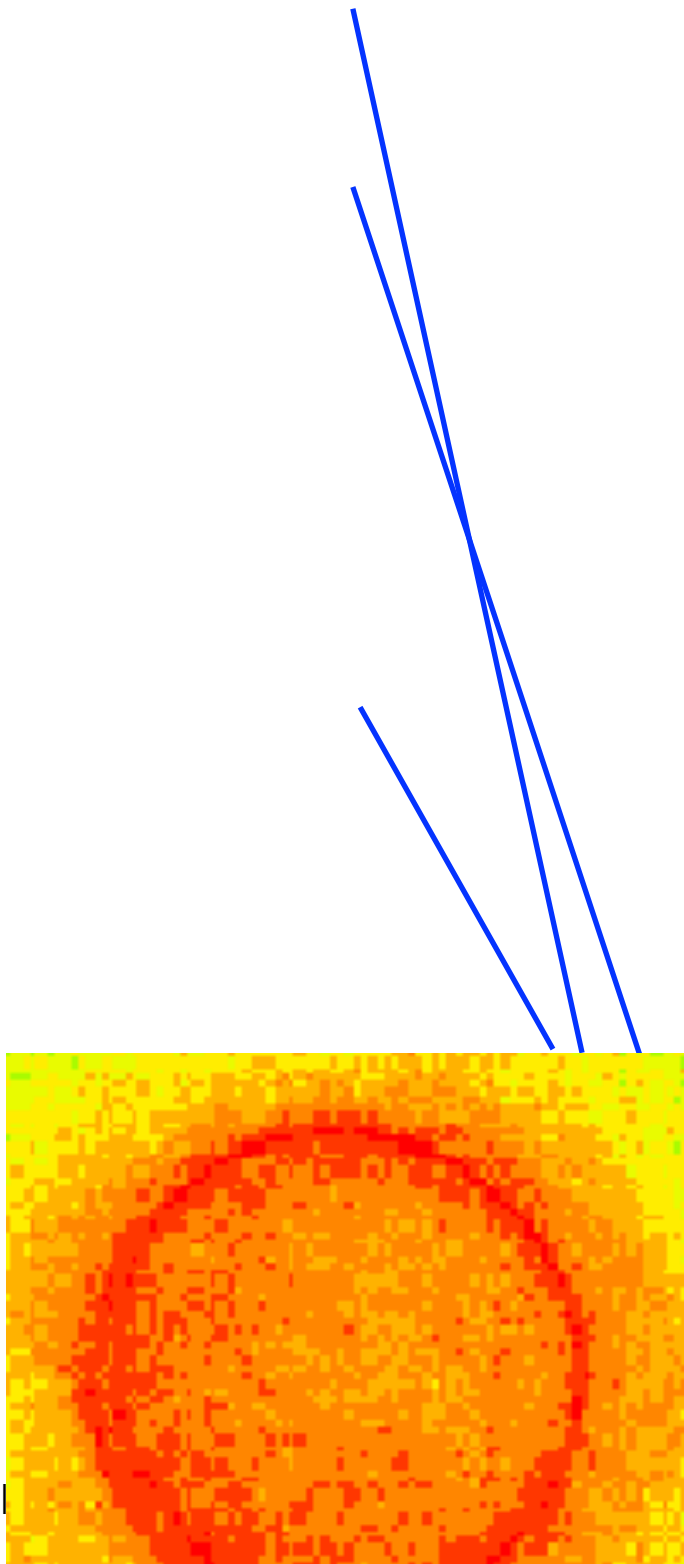


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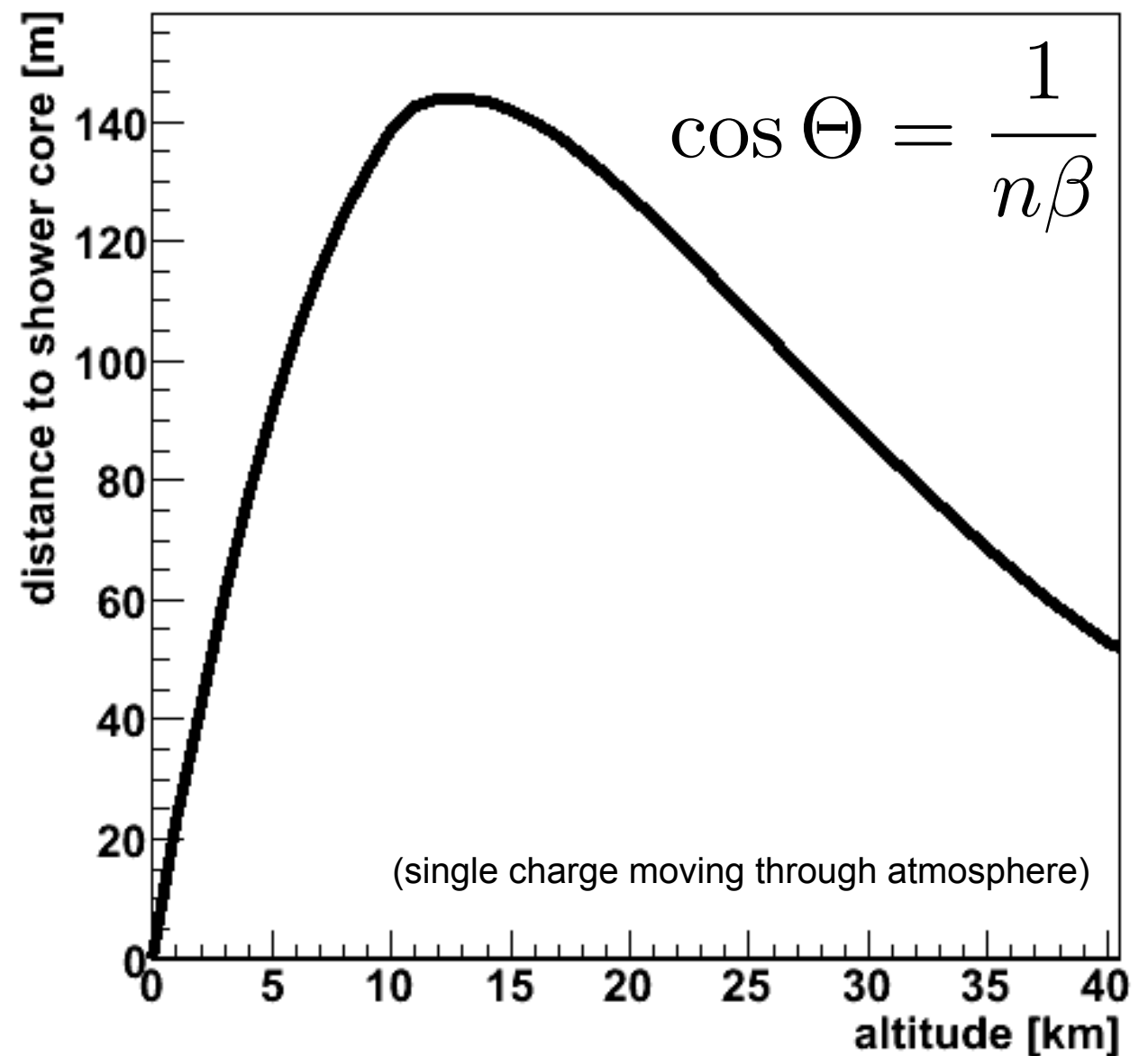
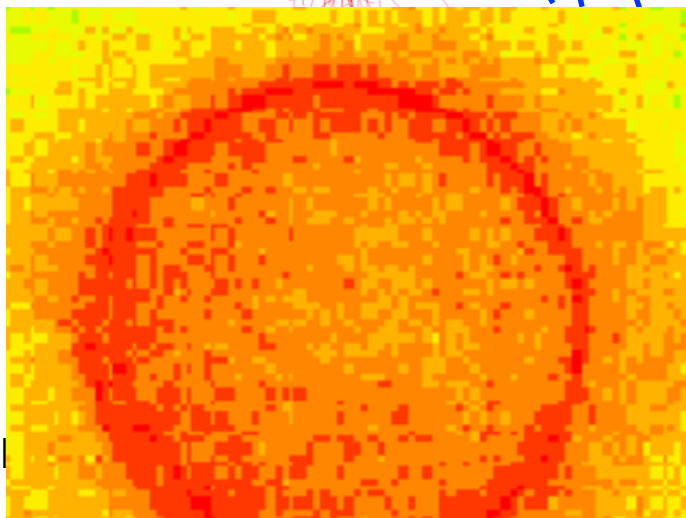
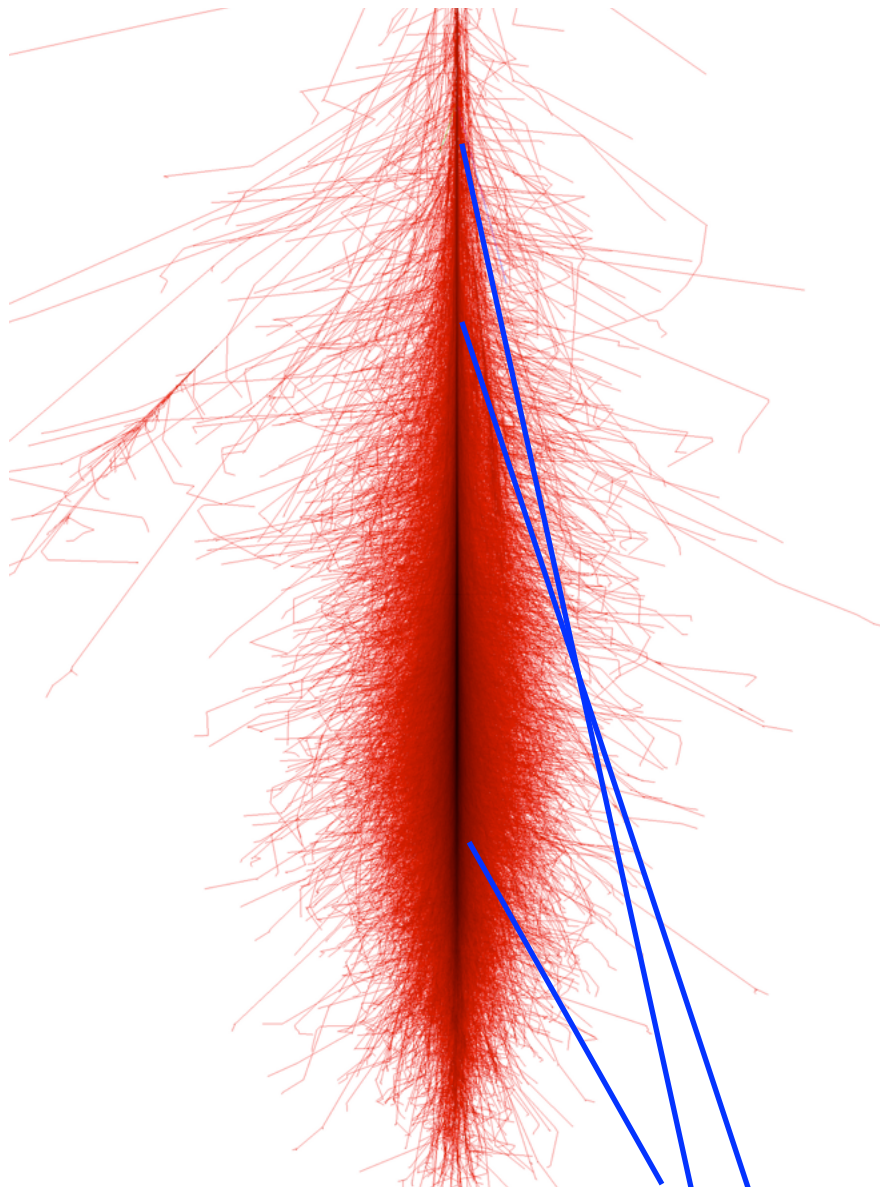




# Cherenkov emission in the Atmosphere

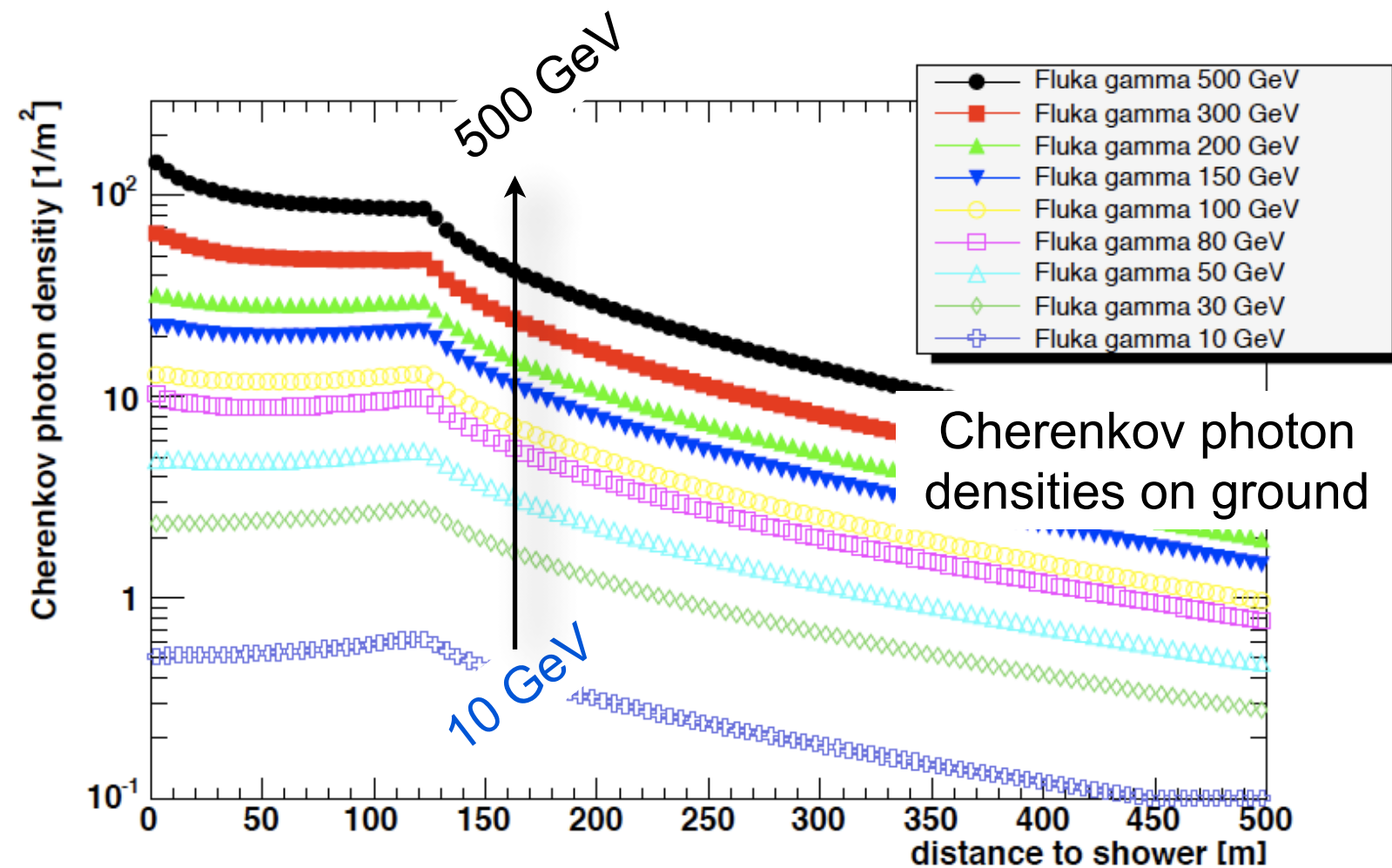
refractive index in air scales with density

$$n = 1 + 0.000283 \rho(h)/\rho(0)$$



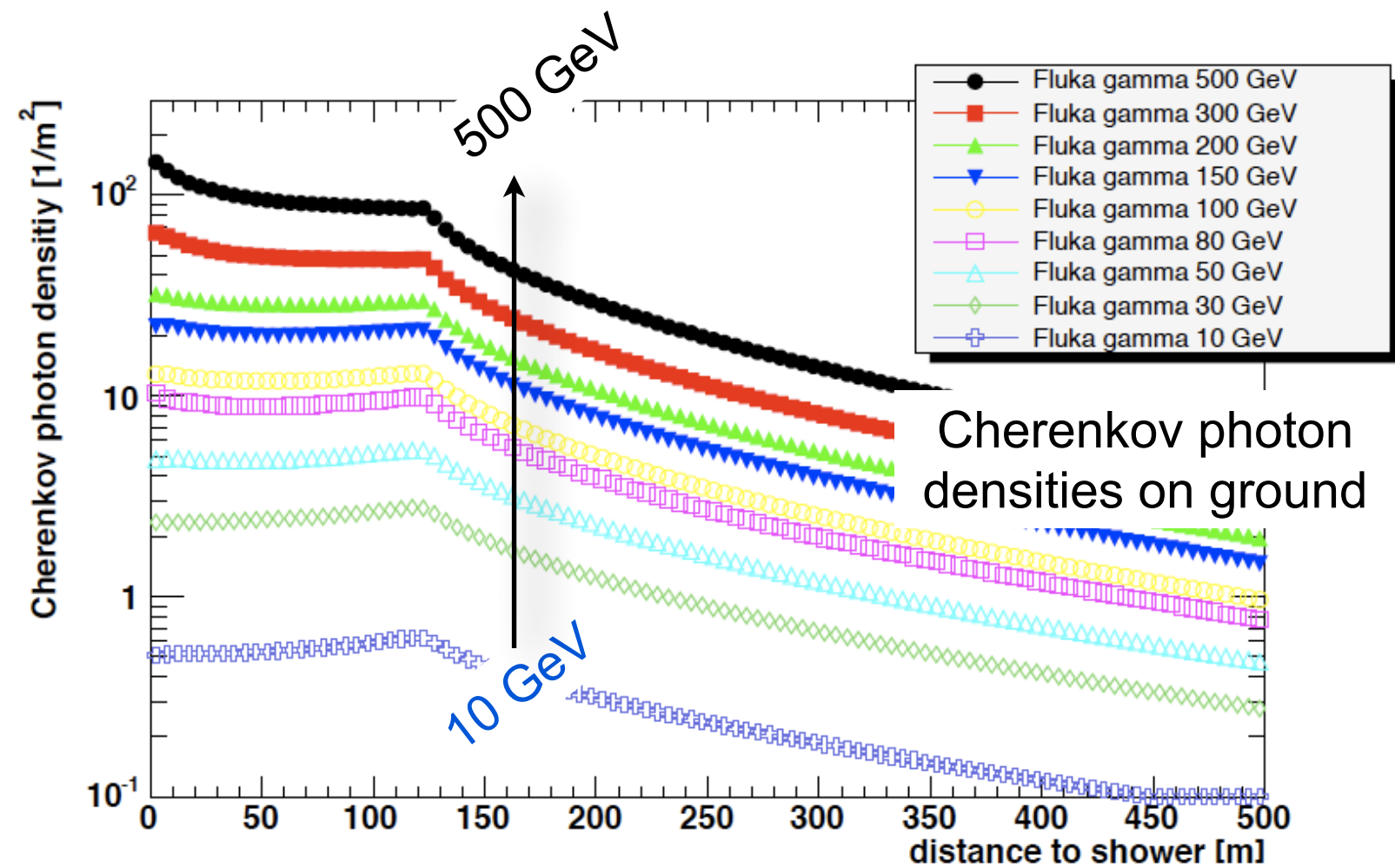
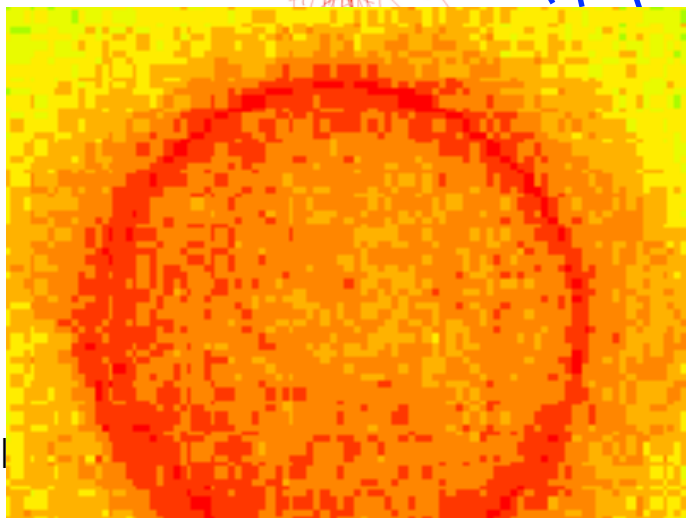
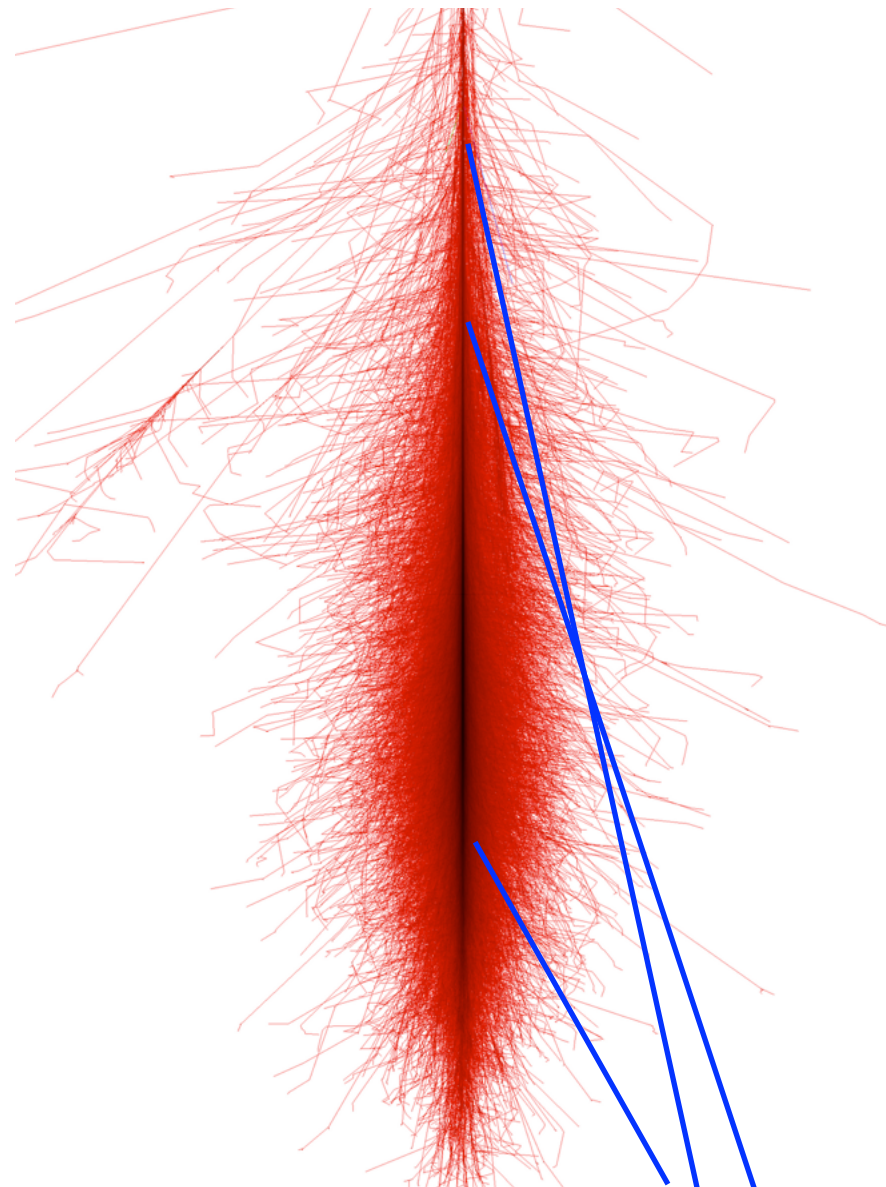


# Lateral distributions.



Cherenkov light from air showers:  
weak ( $\sim 10 \text{ ph/m}^2$ ), short ( $\sim \text{ns}$ ),  
blue (300-550nm) flash of light

# Lateral distributions.



Cherenkov light from air showers:  
weak ( $\sim 10$  ph/ $m^2$ ), short ( $\sim ns$ ),  
blue (300-550nm) flash of light



# Lateral distributions

KASCADE air shower array



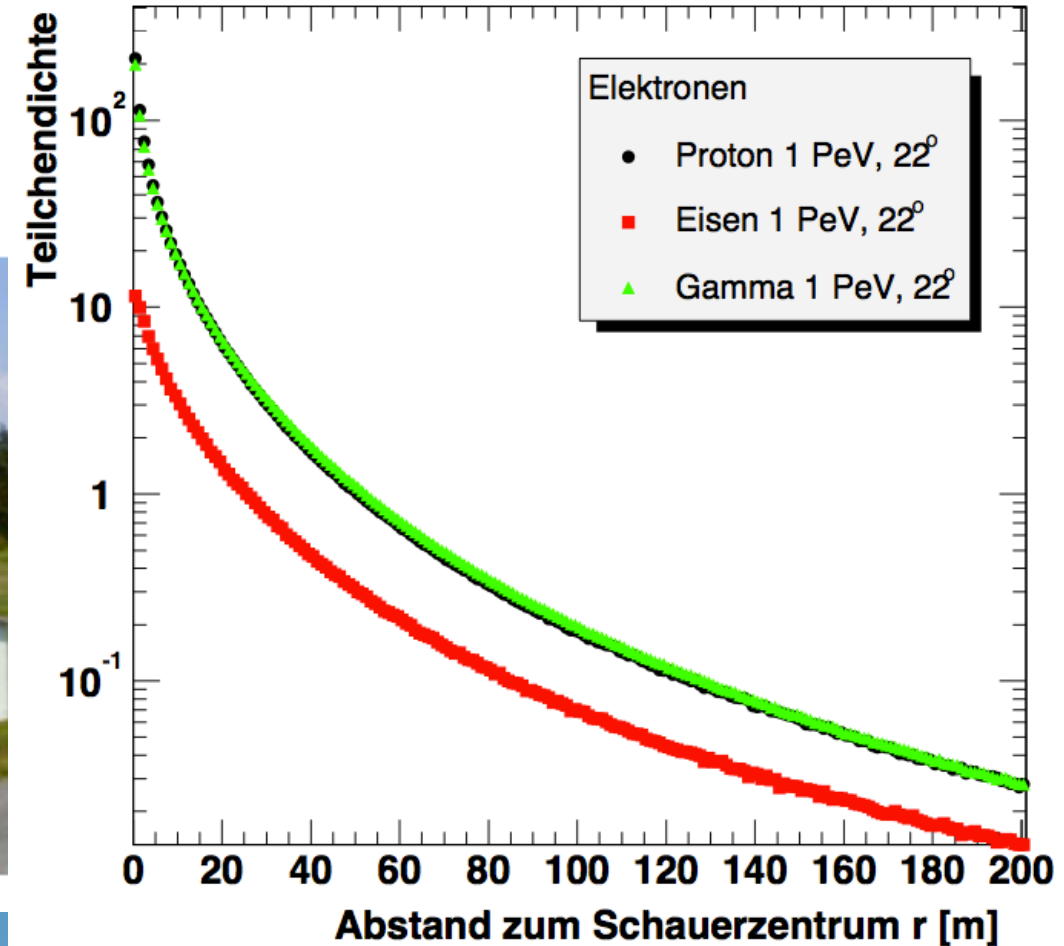
VERITAS



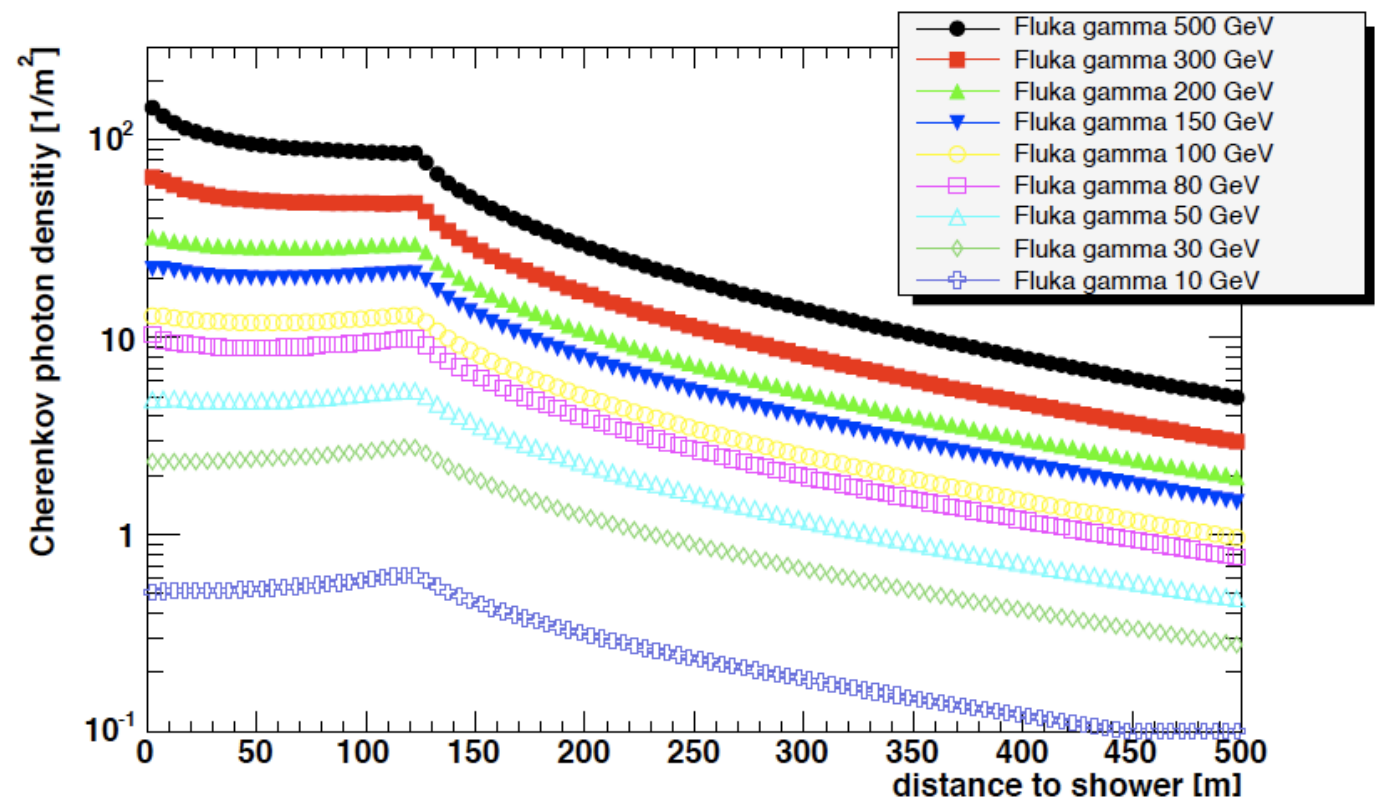


# Lateral distributions

KASCADE air shower array

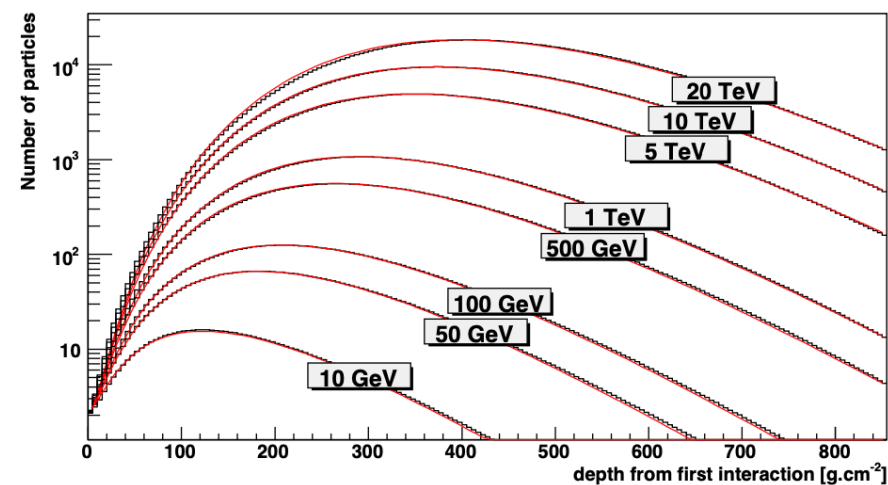
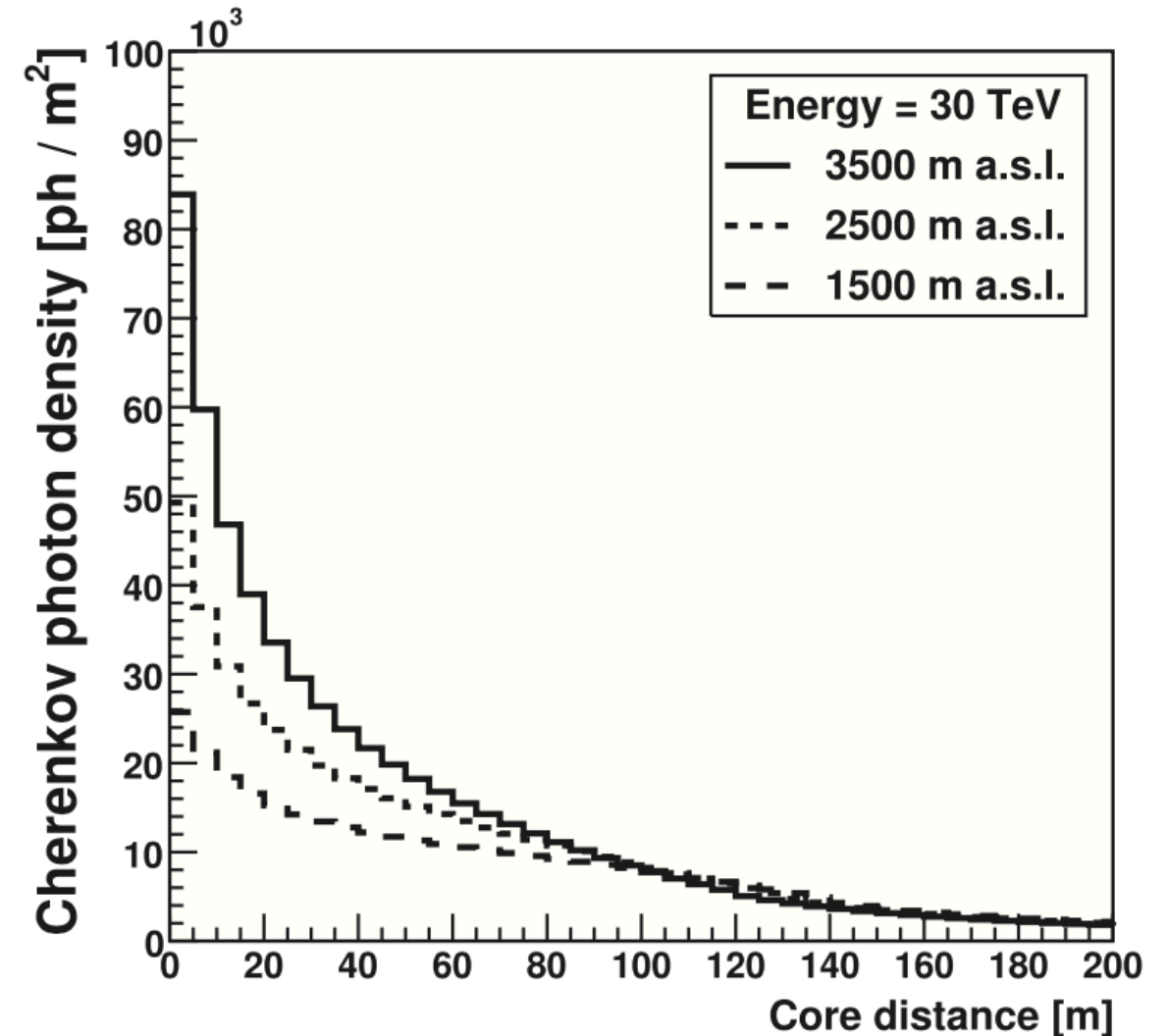
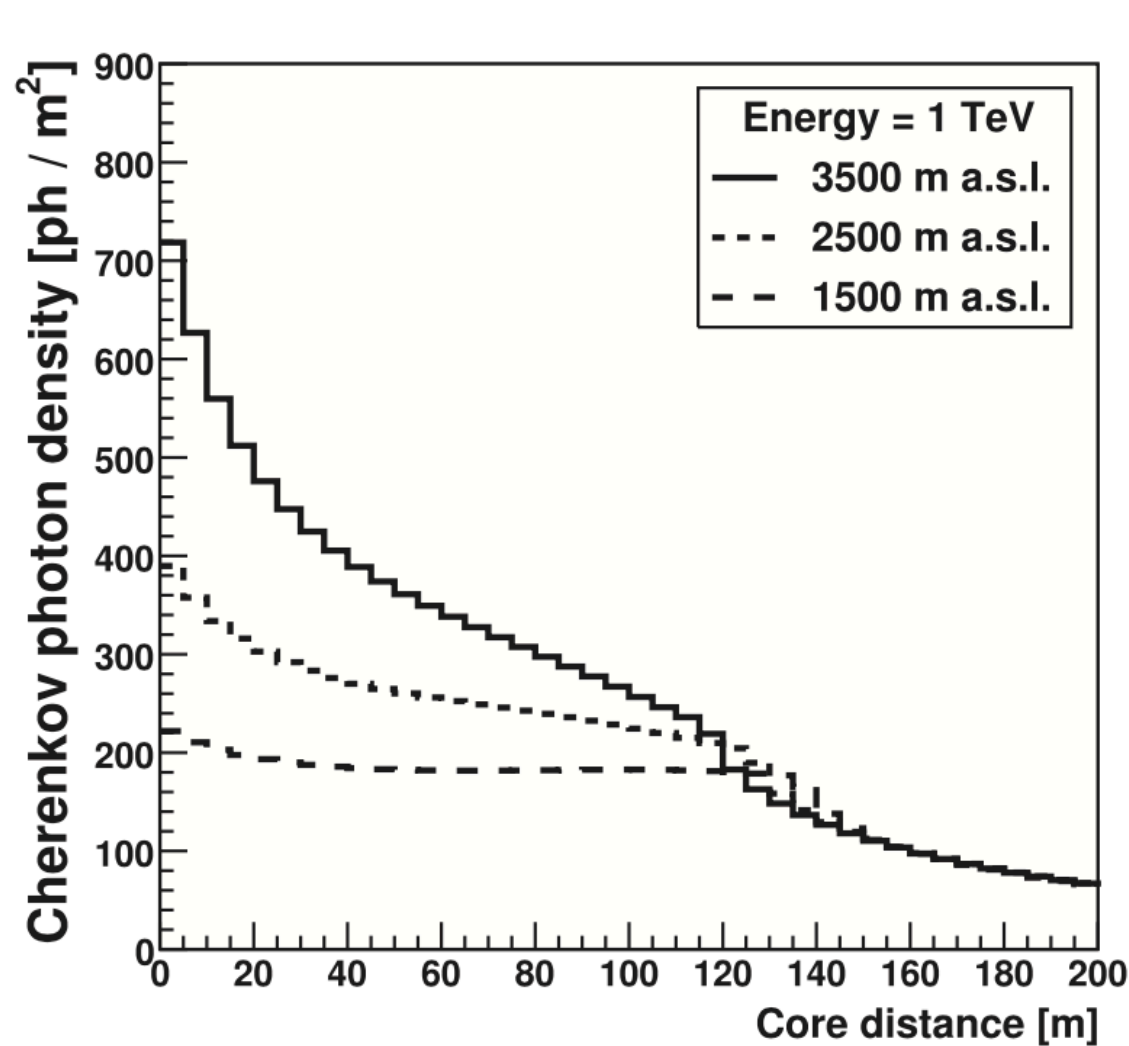


VERITAS



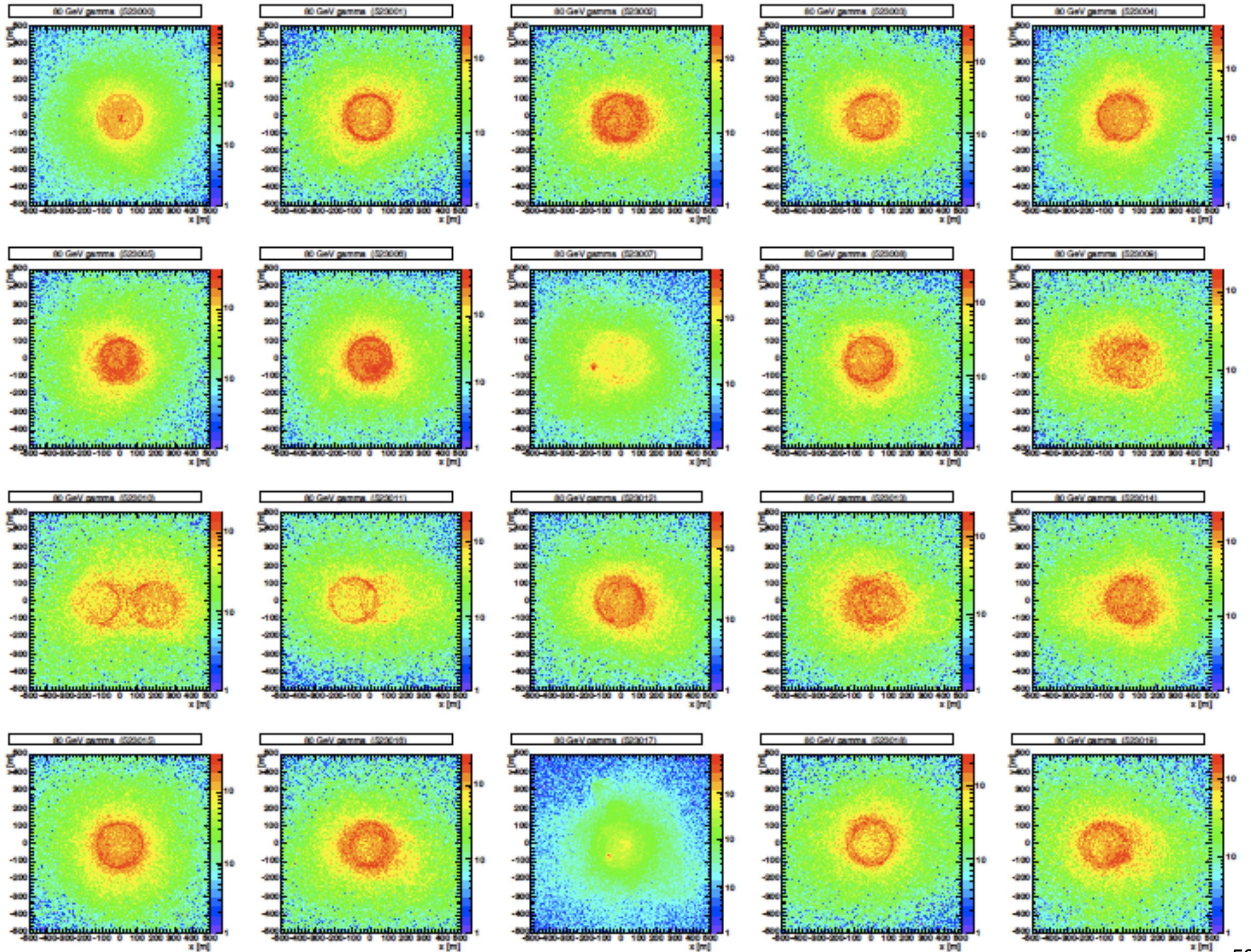
# Lateral distributions vs shower development.

*T. Hassan et al./Astroparticle Physics 93 (2017) 76–85*



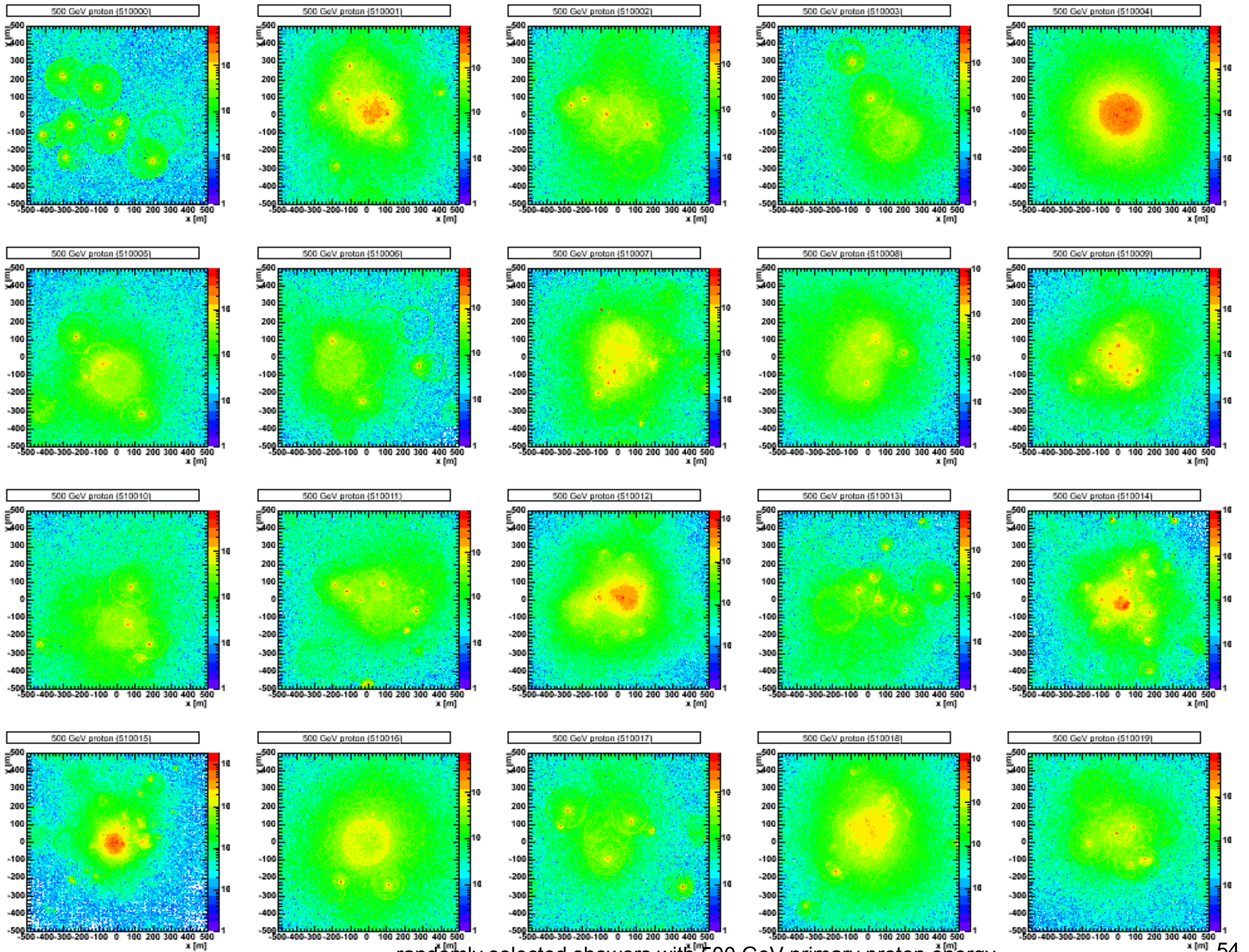
de Naurois 2009





randomly selected showers with 80 GeV primary photon energy

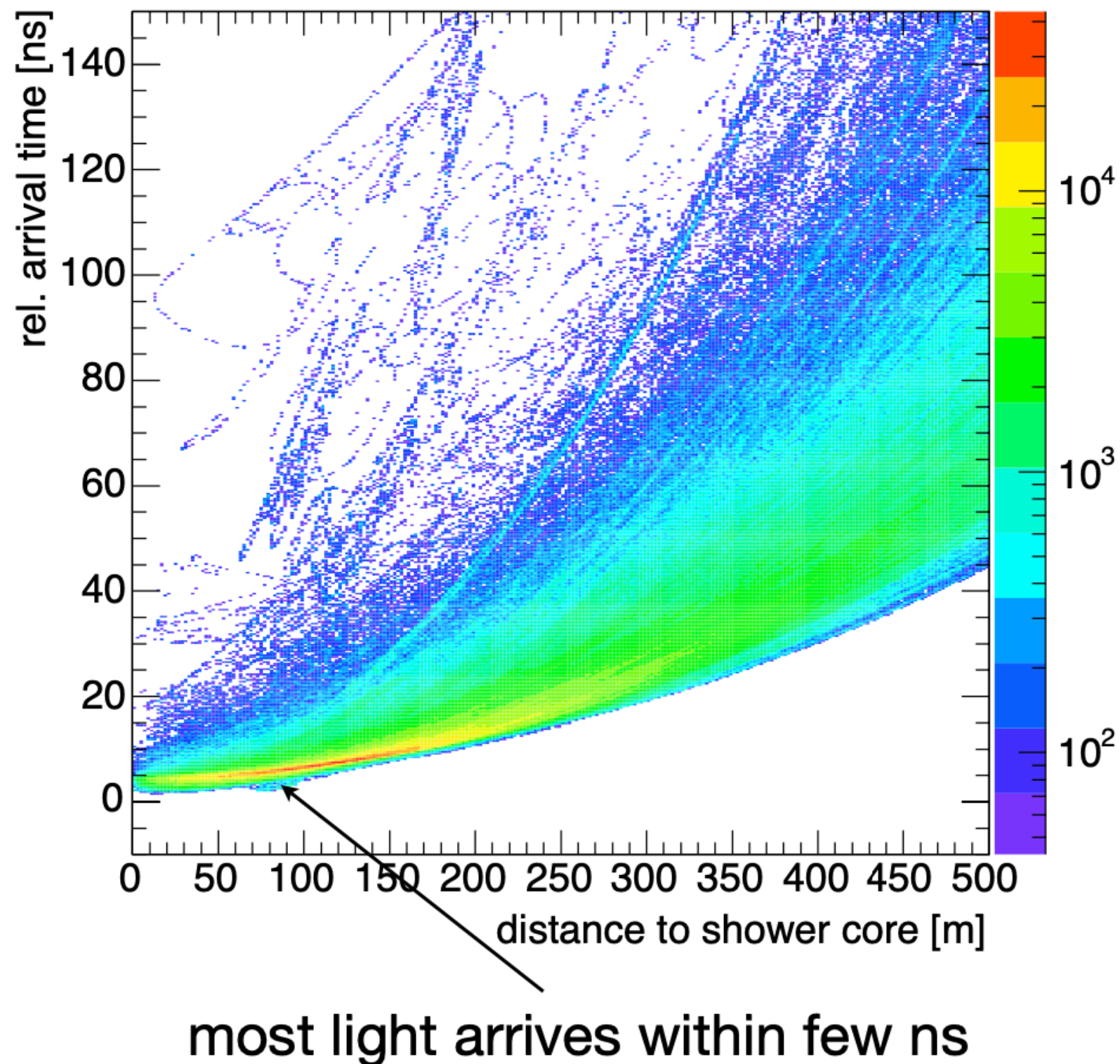




randomly selected showers with 500 GeV primary proton energy

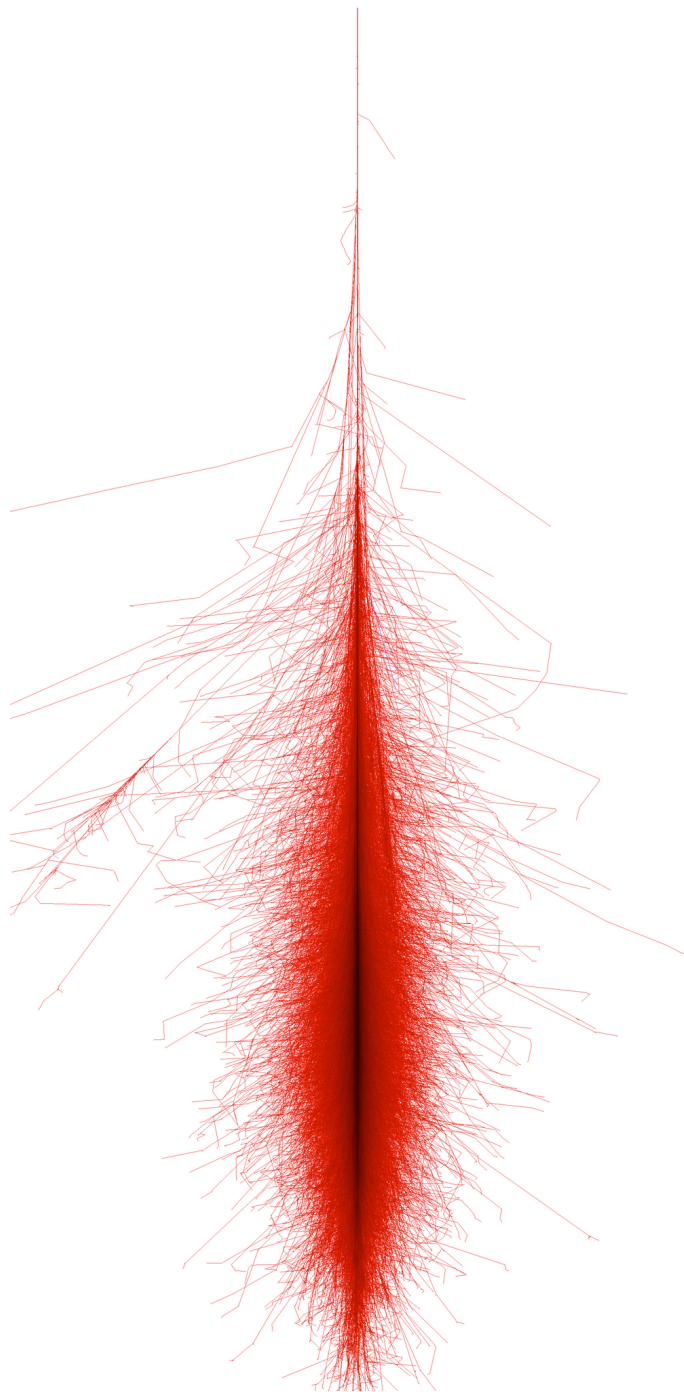


# Cherenkov photon arrival time.

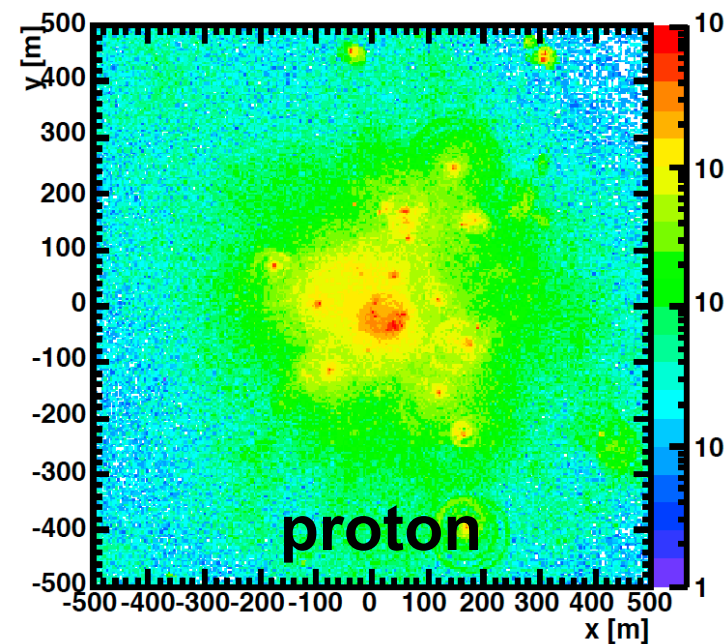
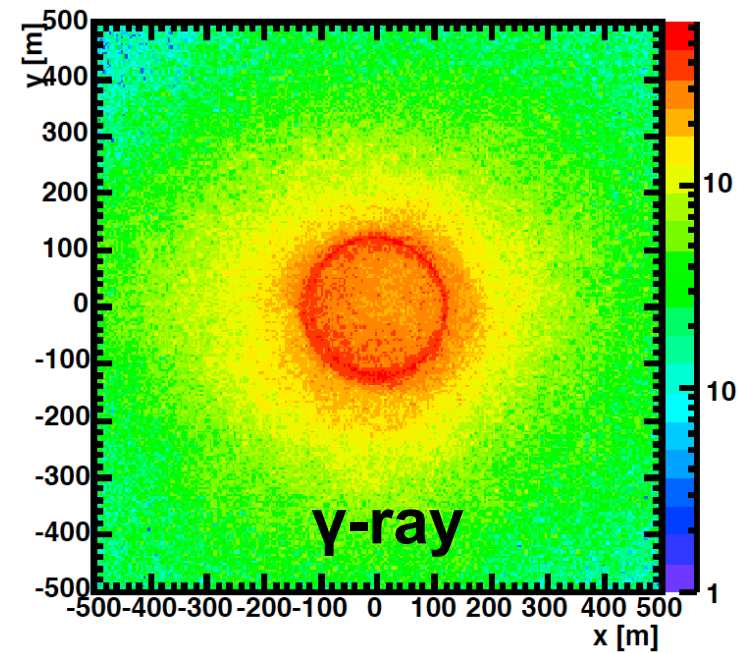


# Proton vs Gamma-ray showers

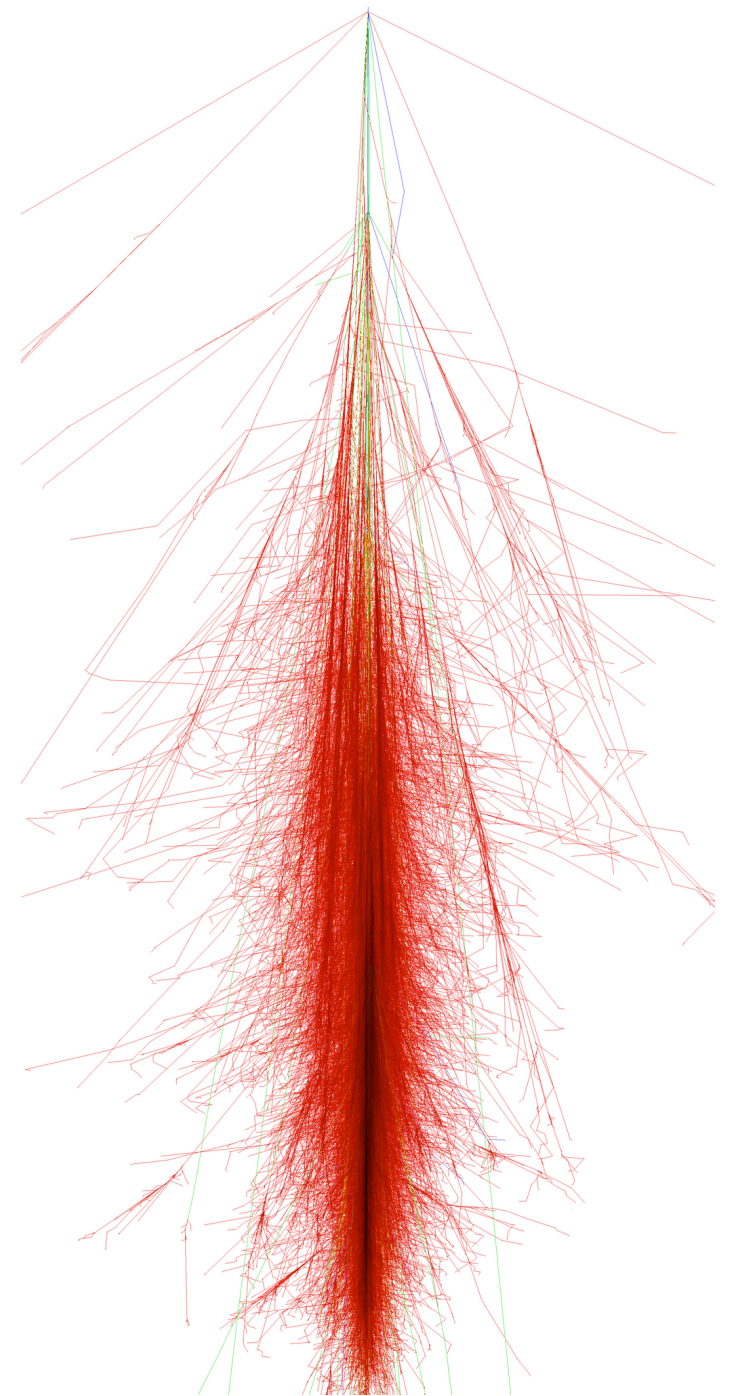
**$\gamma$ -ray**



**Cherenkov photons on ground**

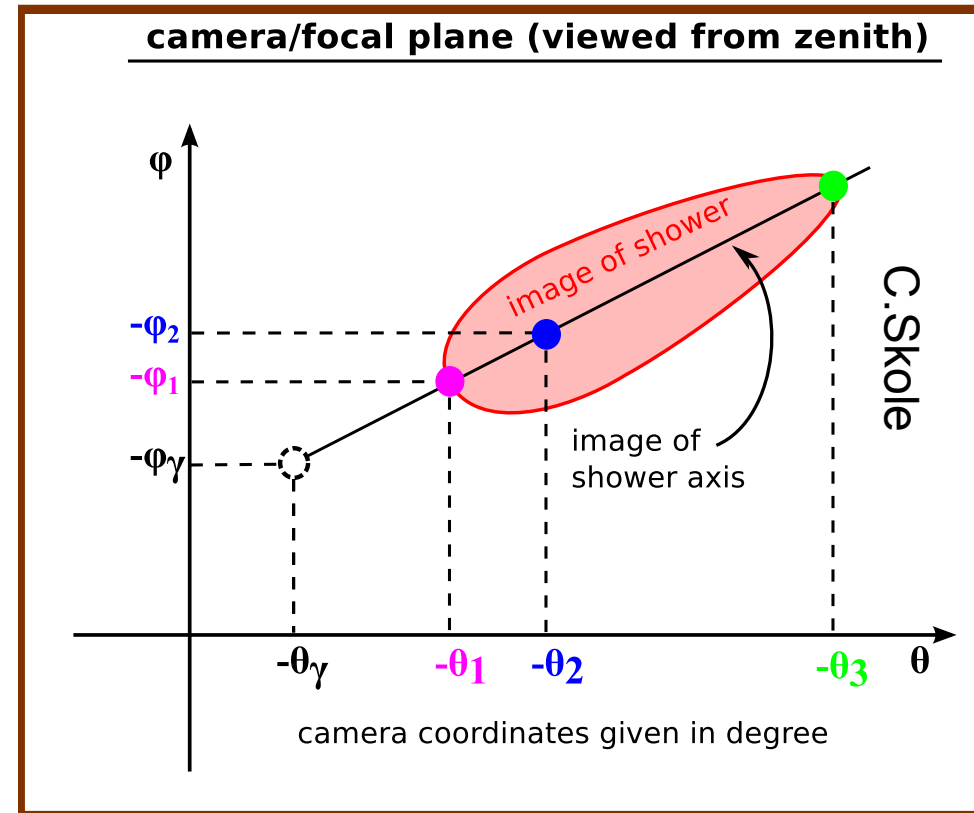
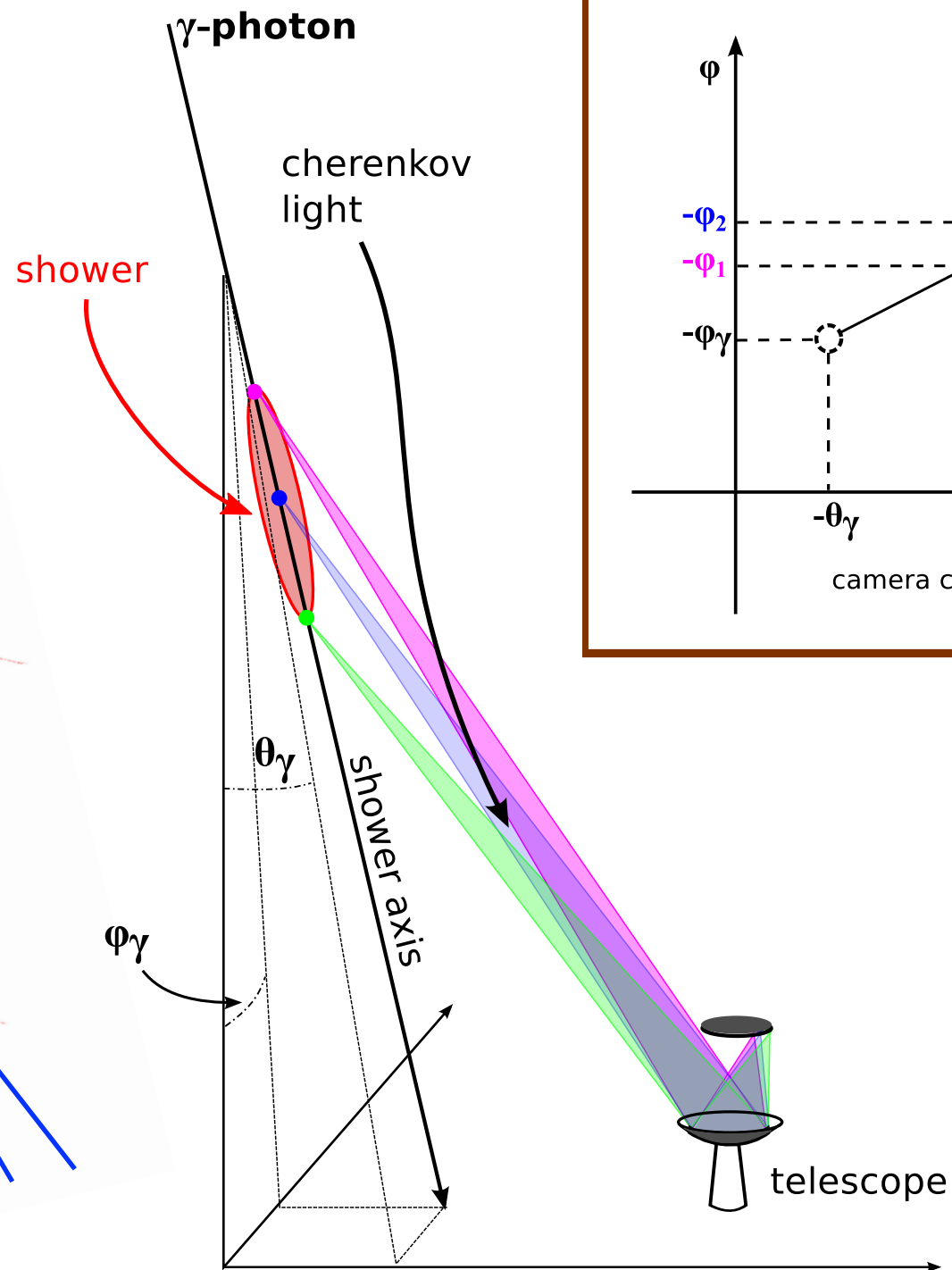
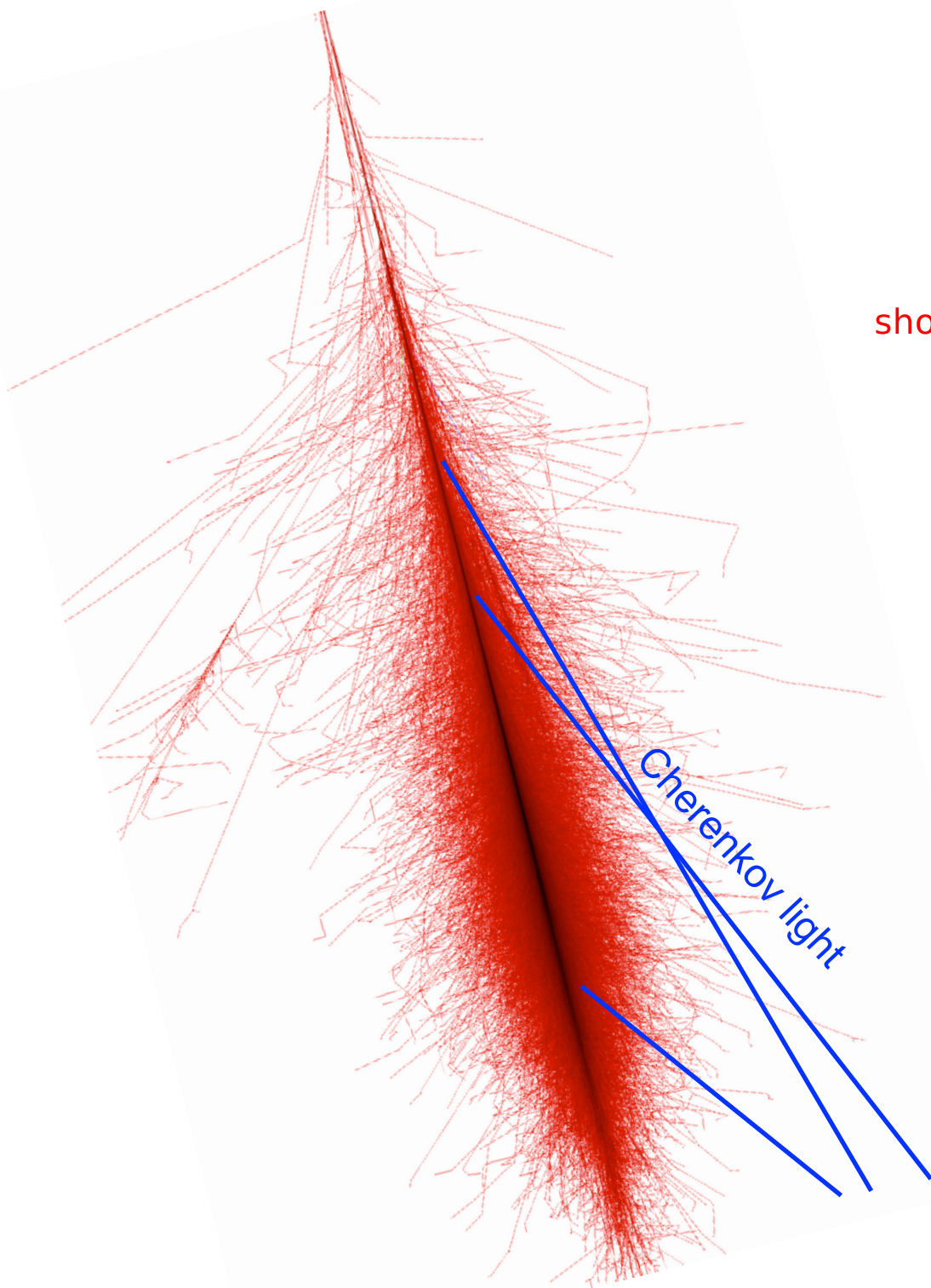


**proton**



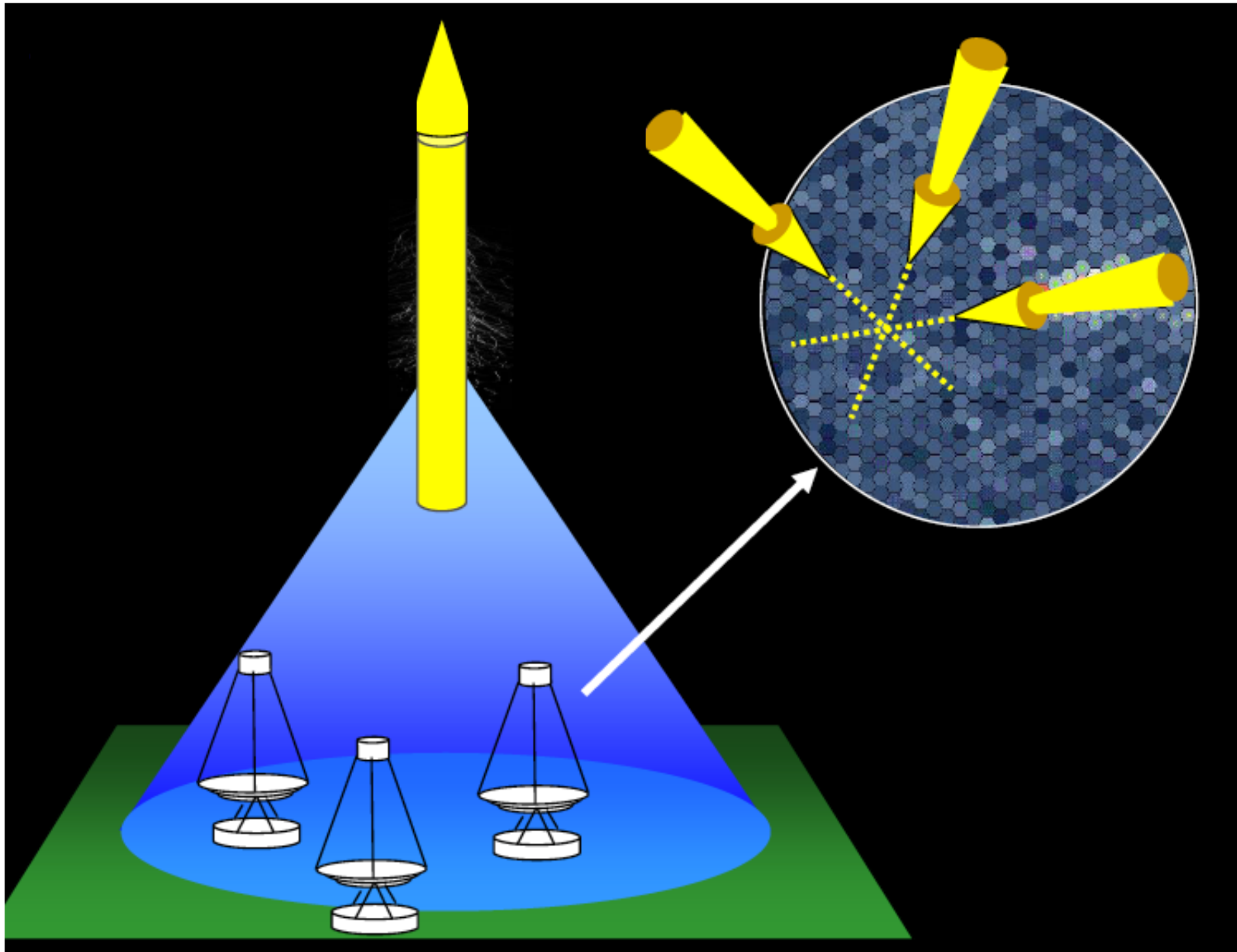


# Imaging Technique - Air Showers



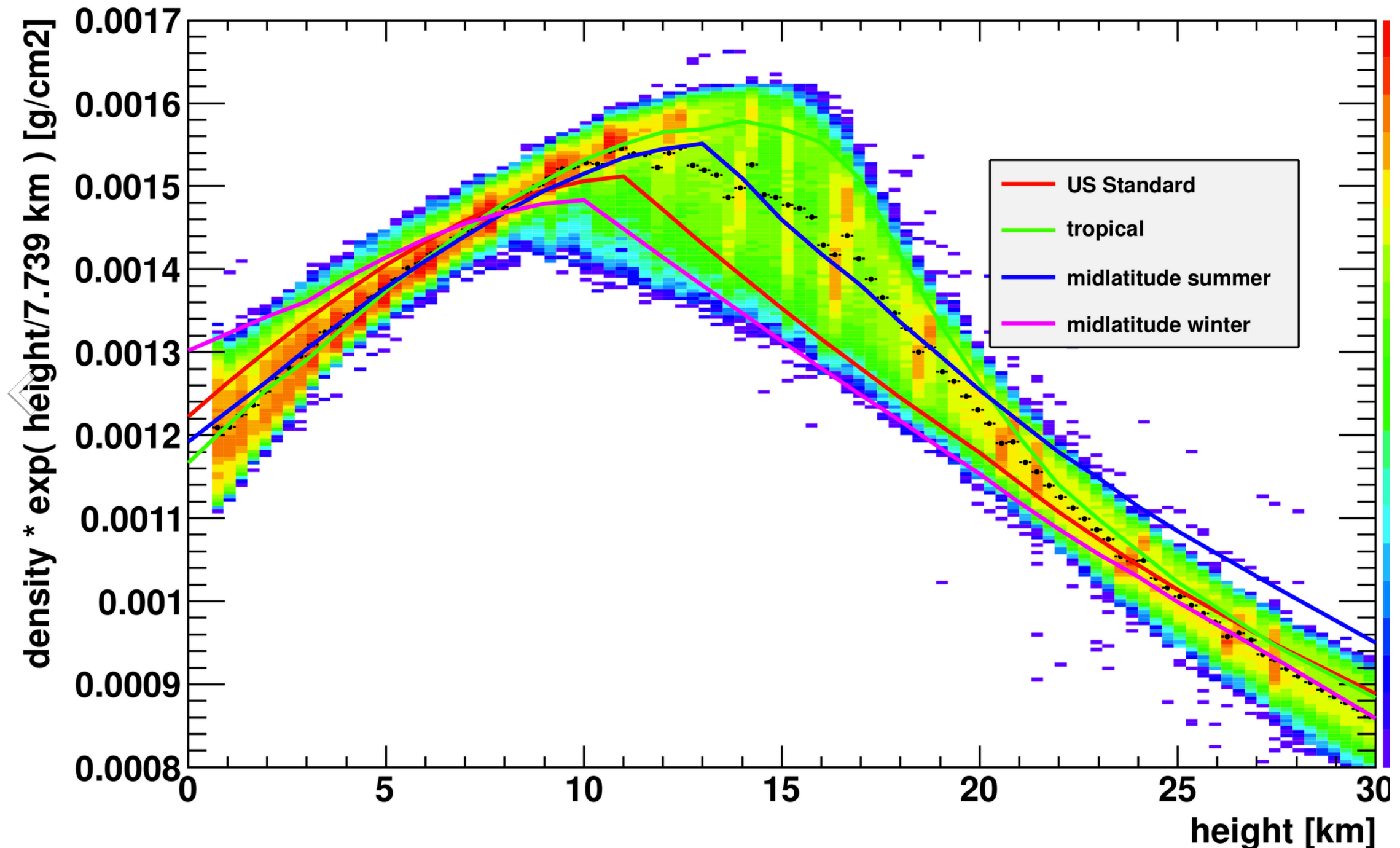


# Stereoscopy.



# Seasonal changes - density vs height.

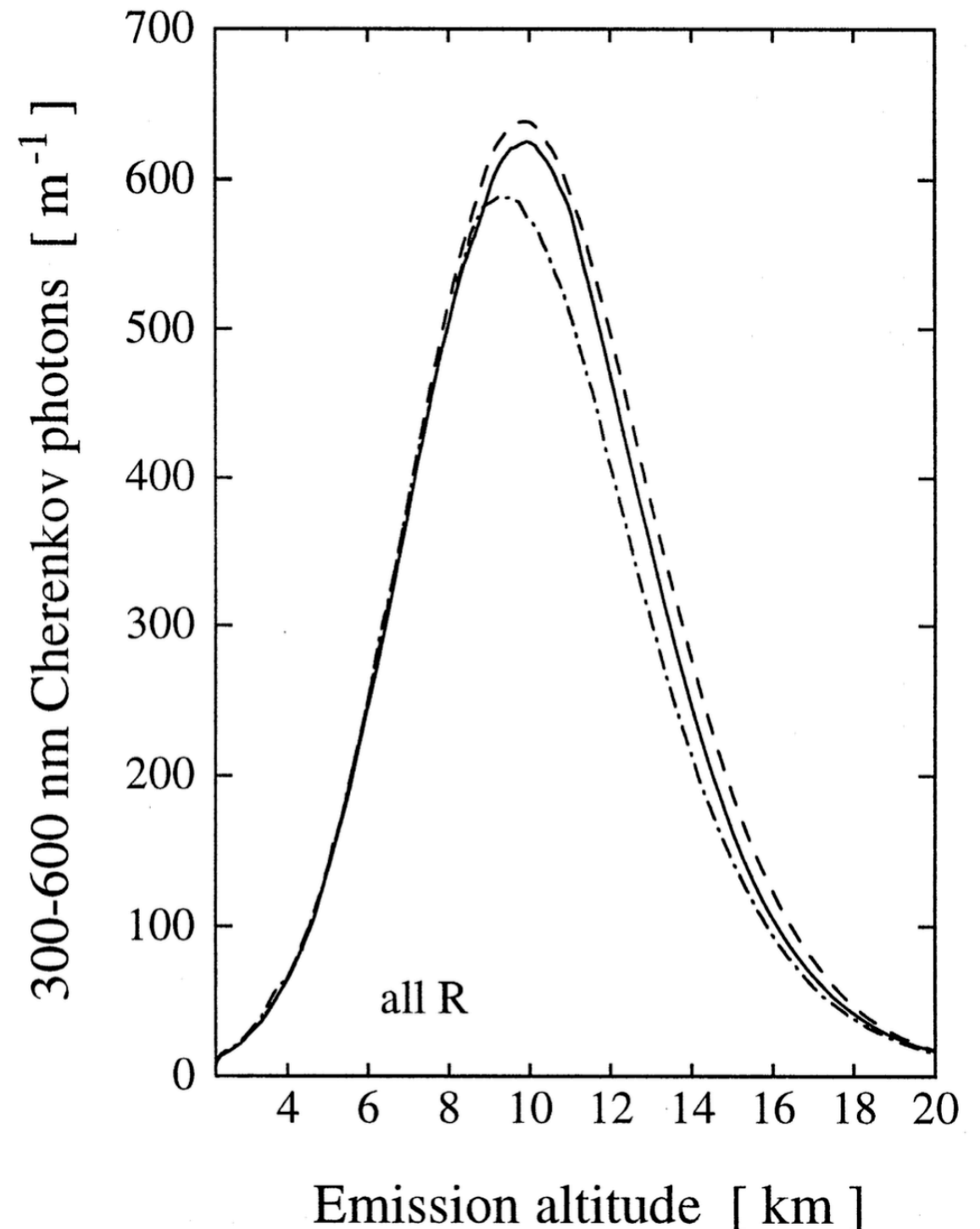
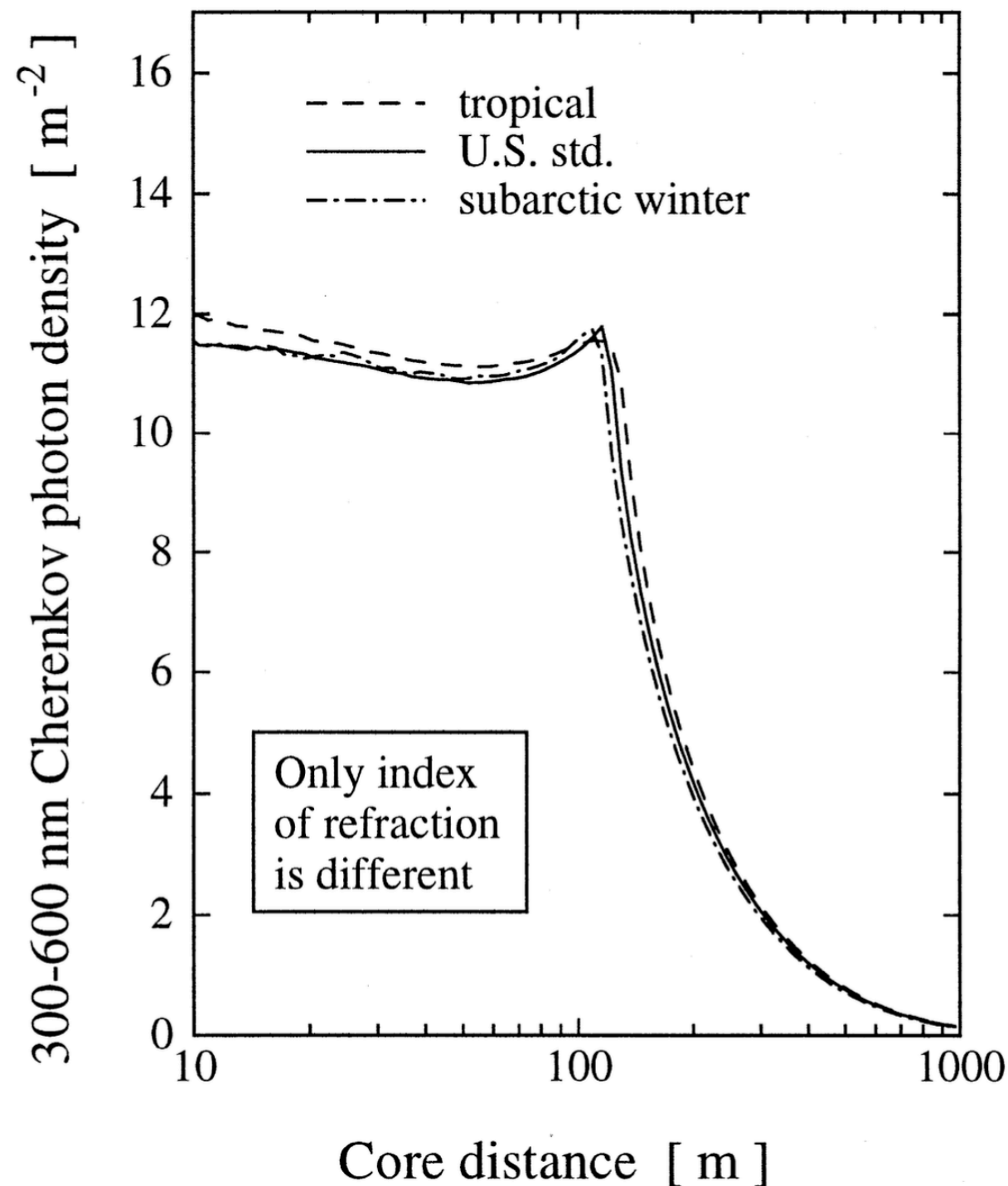
Example from Tucson, Arizona (1995-2010)



Changes shower development and refractive index.

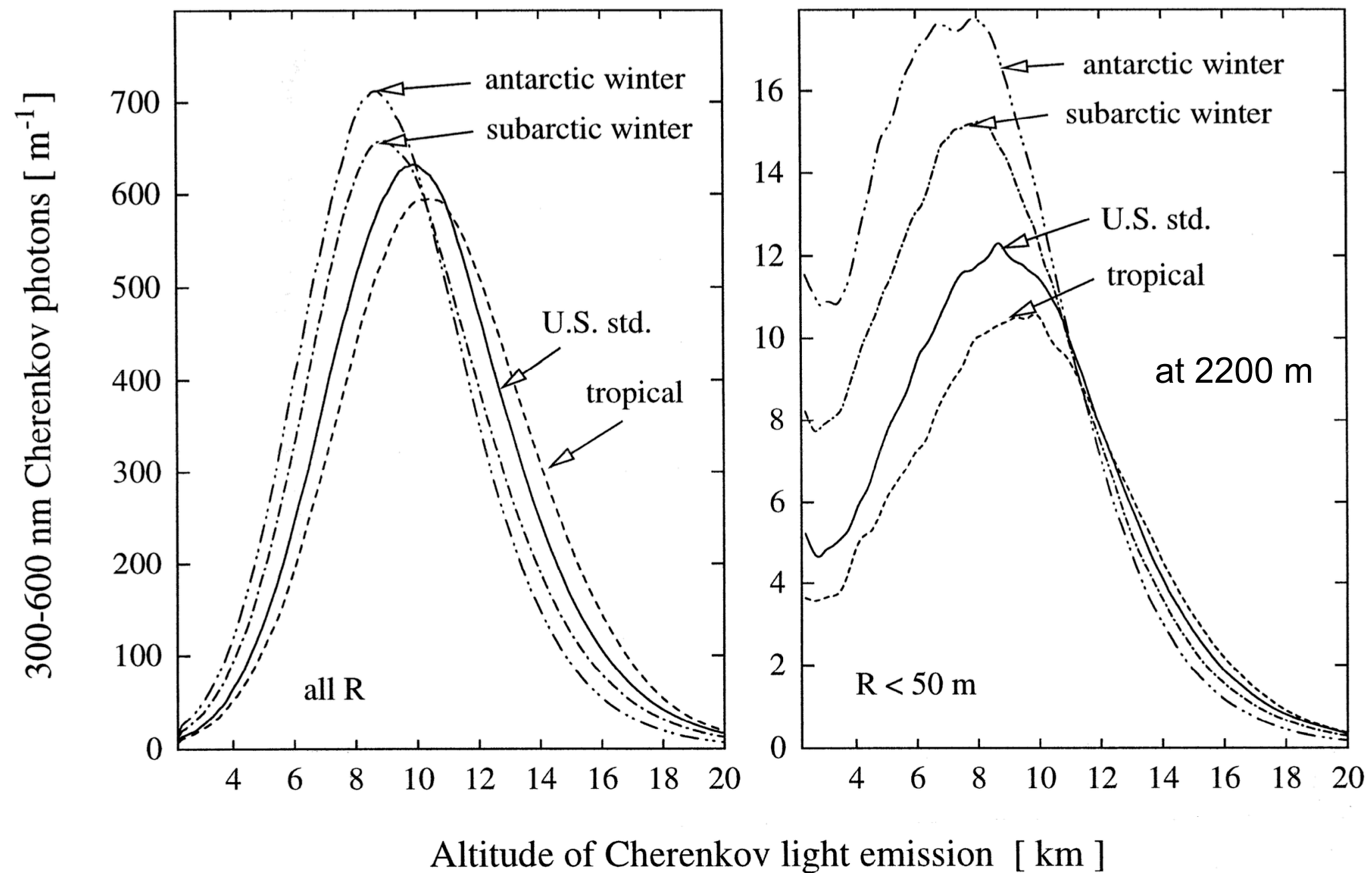
# Refractive index only (same density profile).

*K. Bernlöhr / Astroparticle Physics 12 (2000) 255–268*



# Different atmospheric profiles.

*K. Bernlöhr / Astroparticle Physics 12 (2000) 255–268*

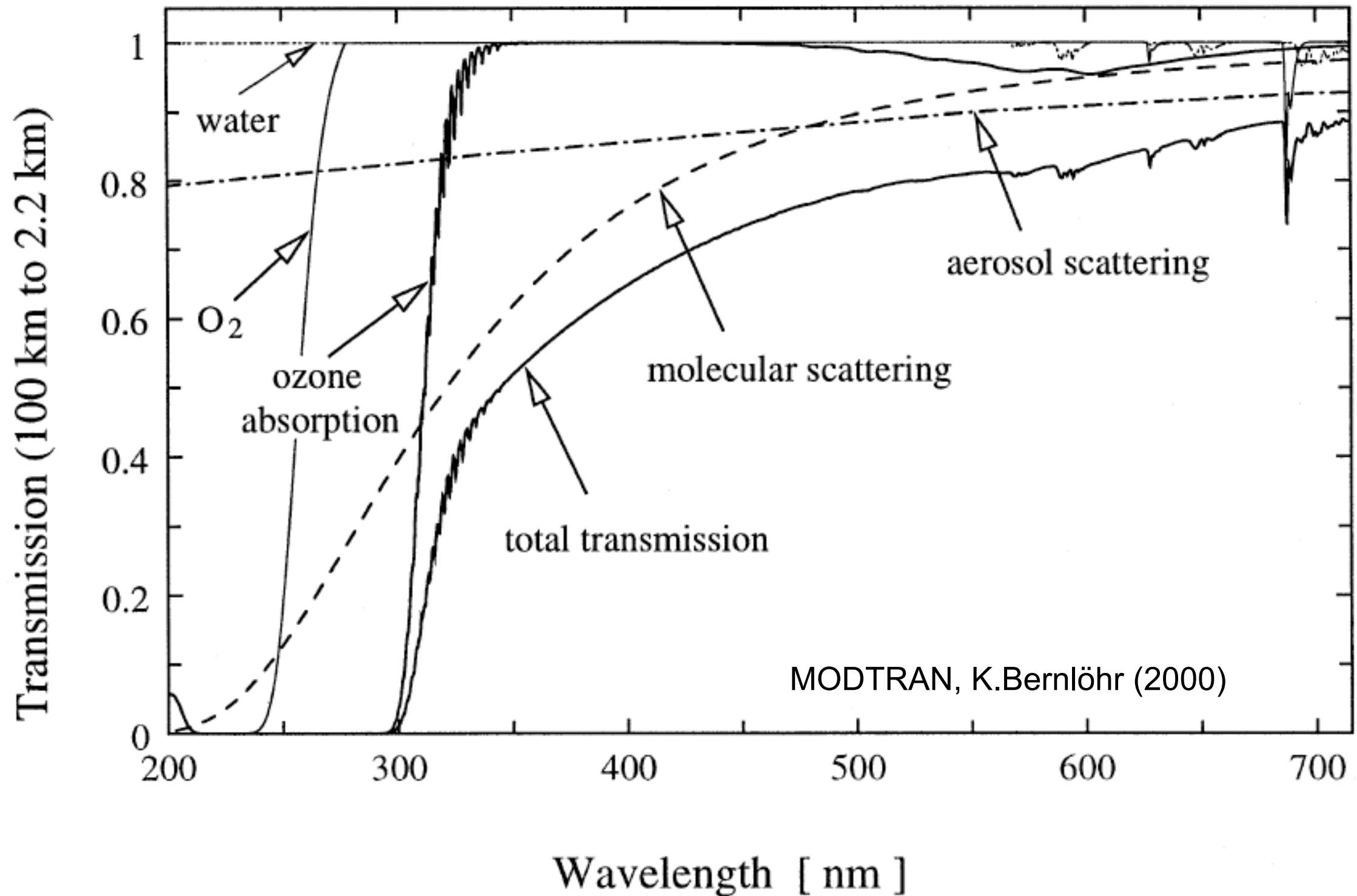




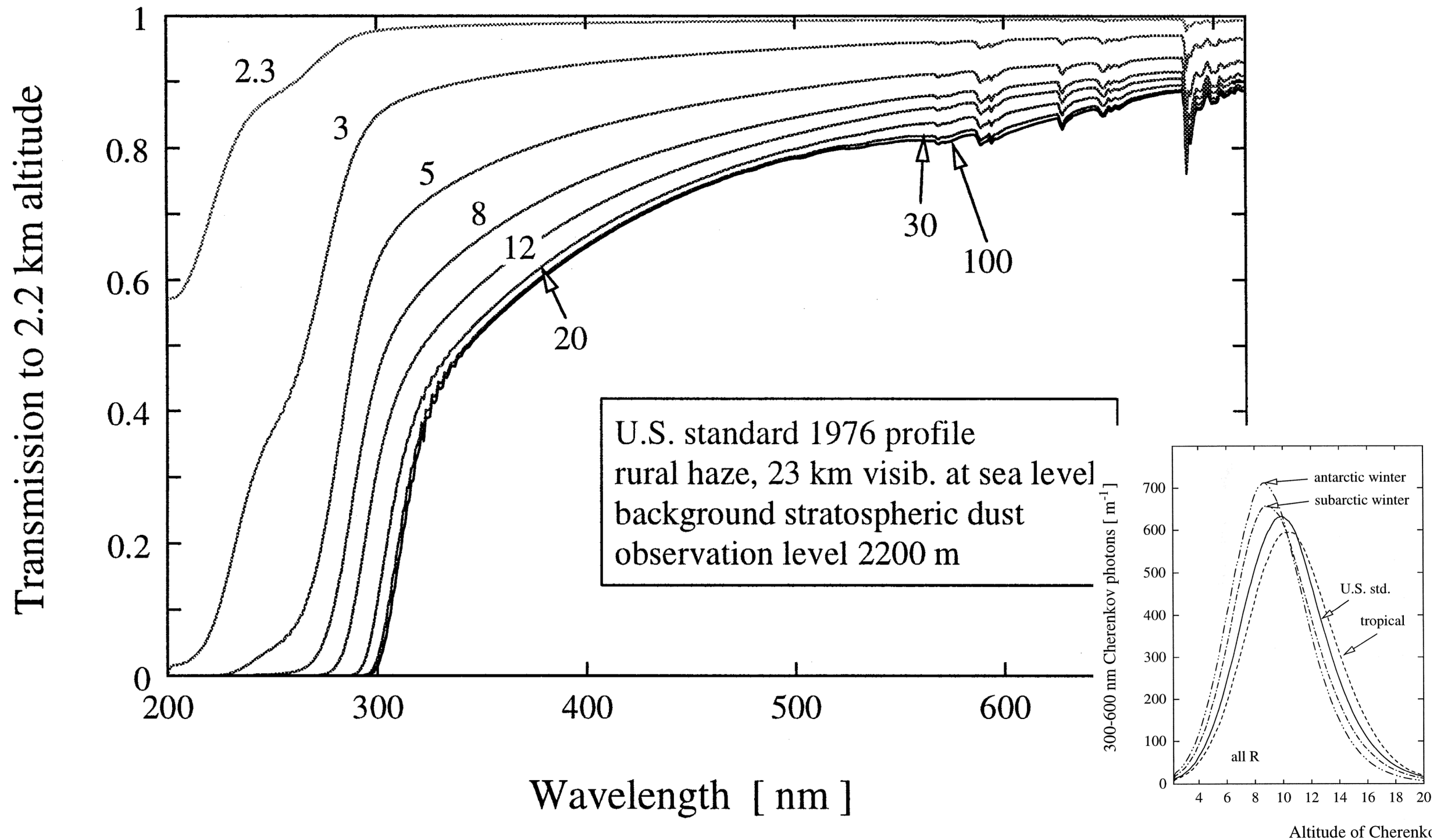
# Propagation of Cherenkov light.

- molecular absorption bands
- molecular (Rayleigh) scattering
- aerosol (Mie) scattering & absorption
- current simulations: scattered == absorbed
- clouds not covered here.

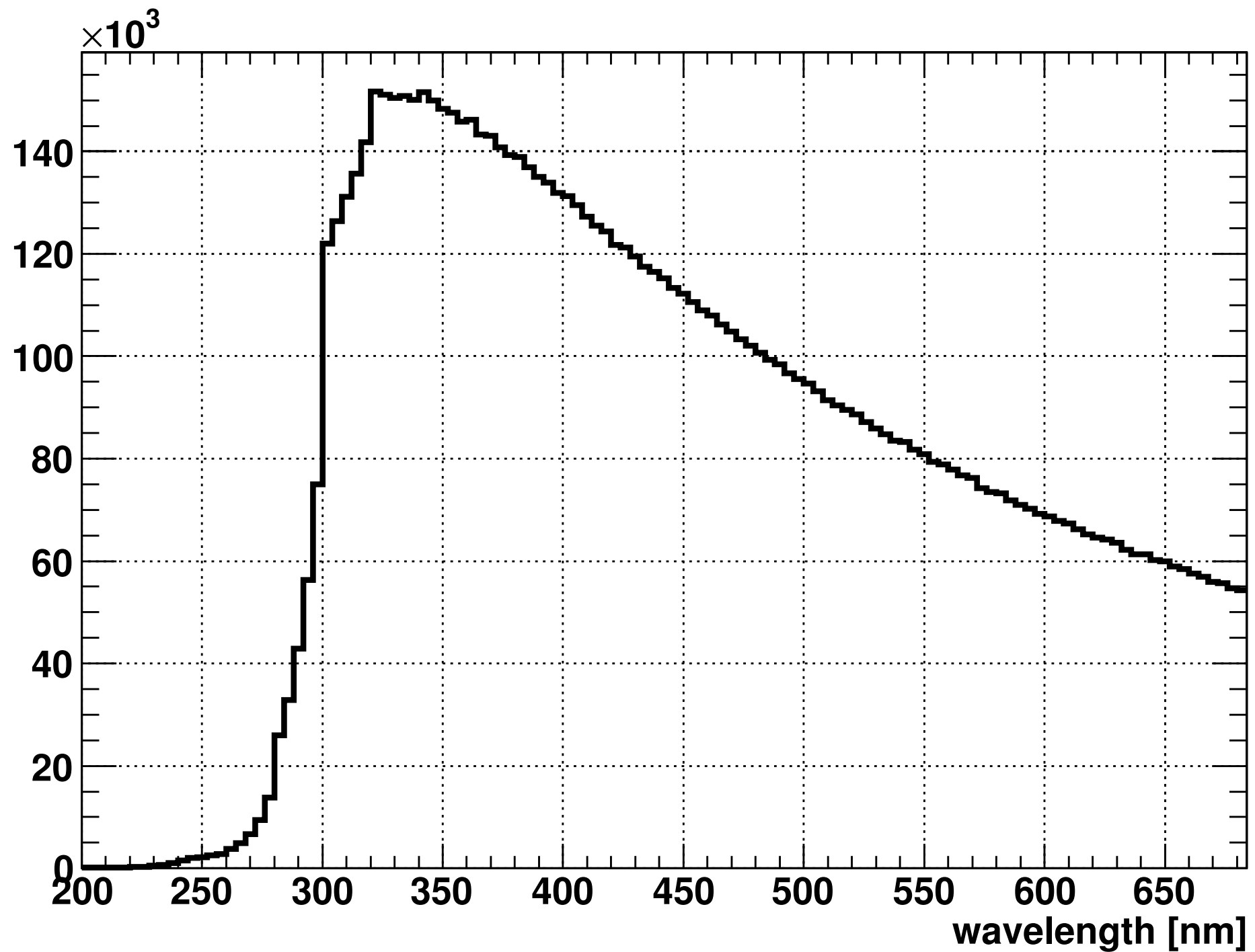
# Atmospheric extinction.



# Atmospheric Extinction.

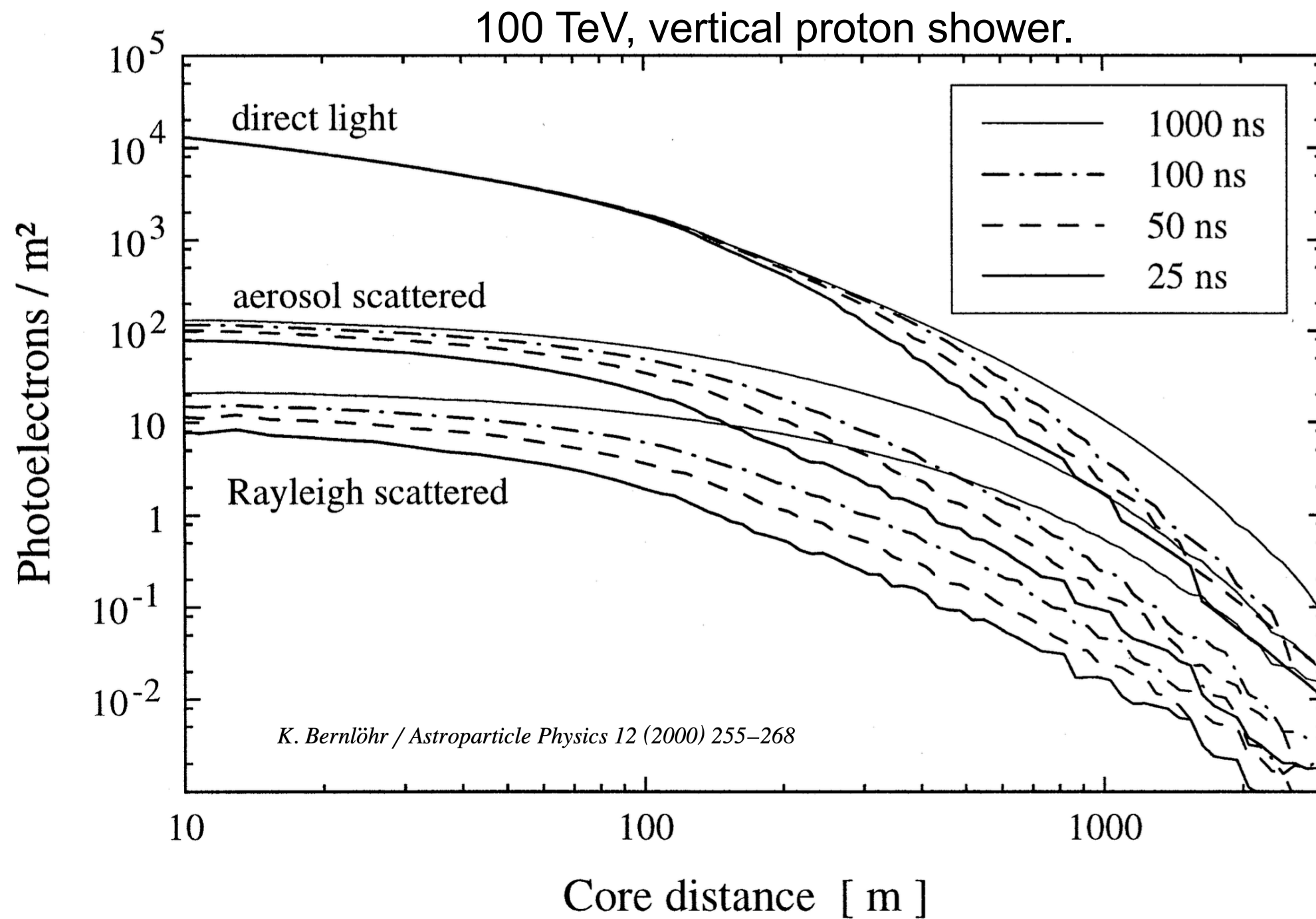


# Cherenkov spectrum after extinction.





# Scattered == absorbed?

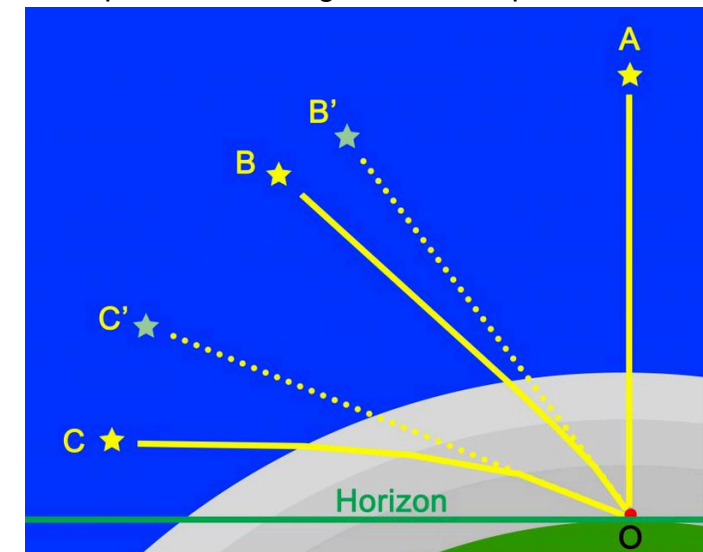
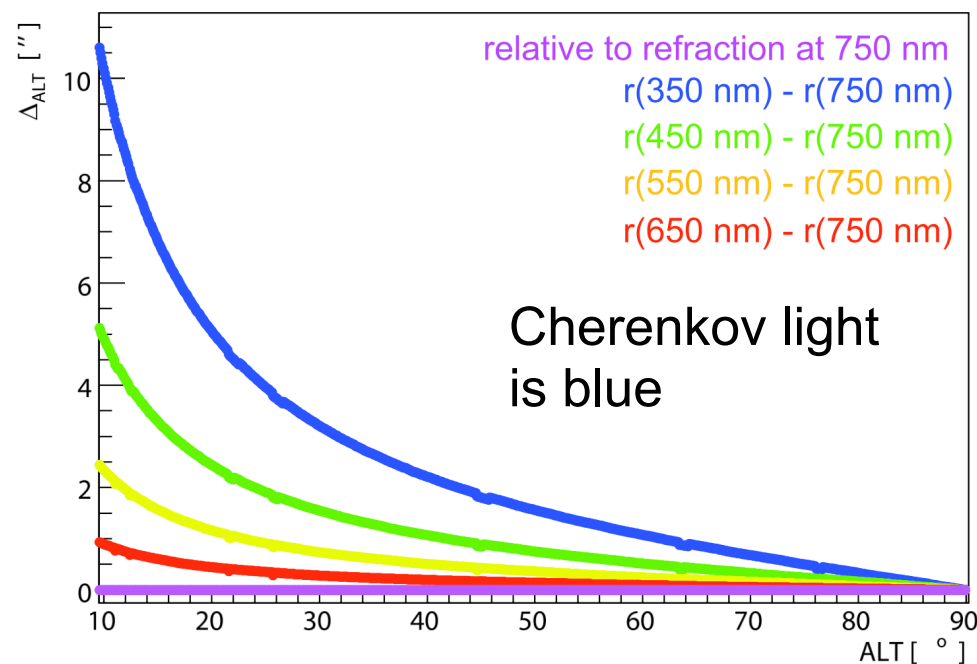
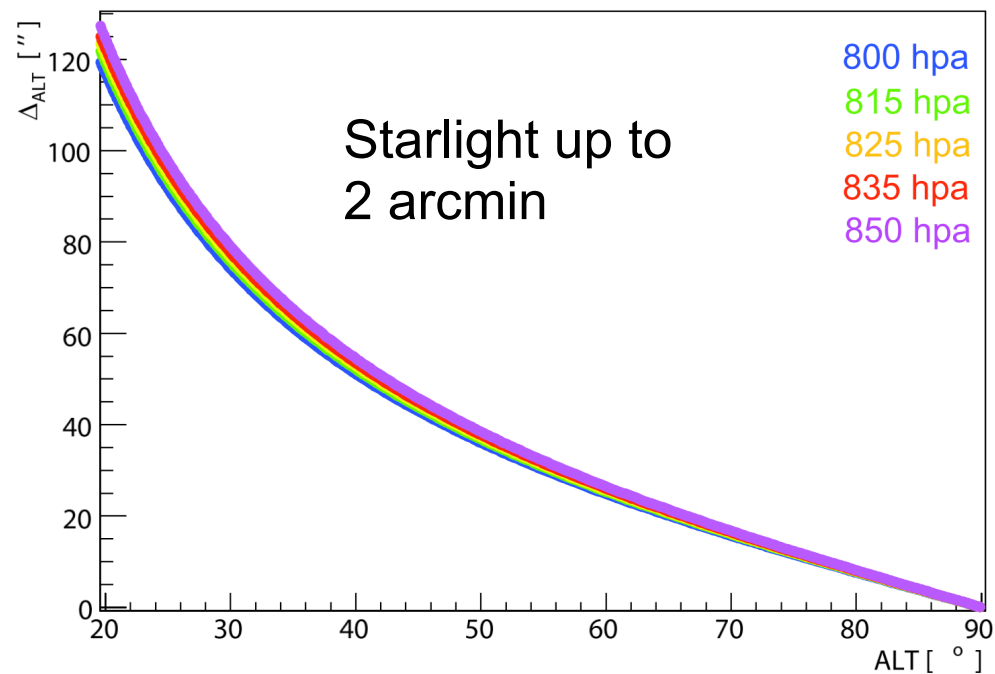


# Refraction.

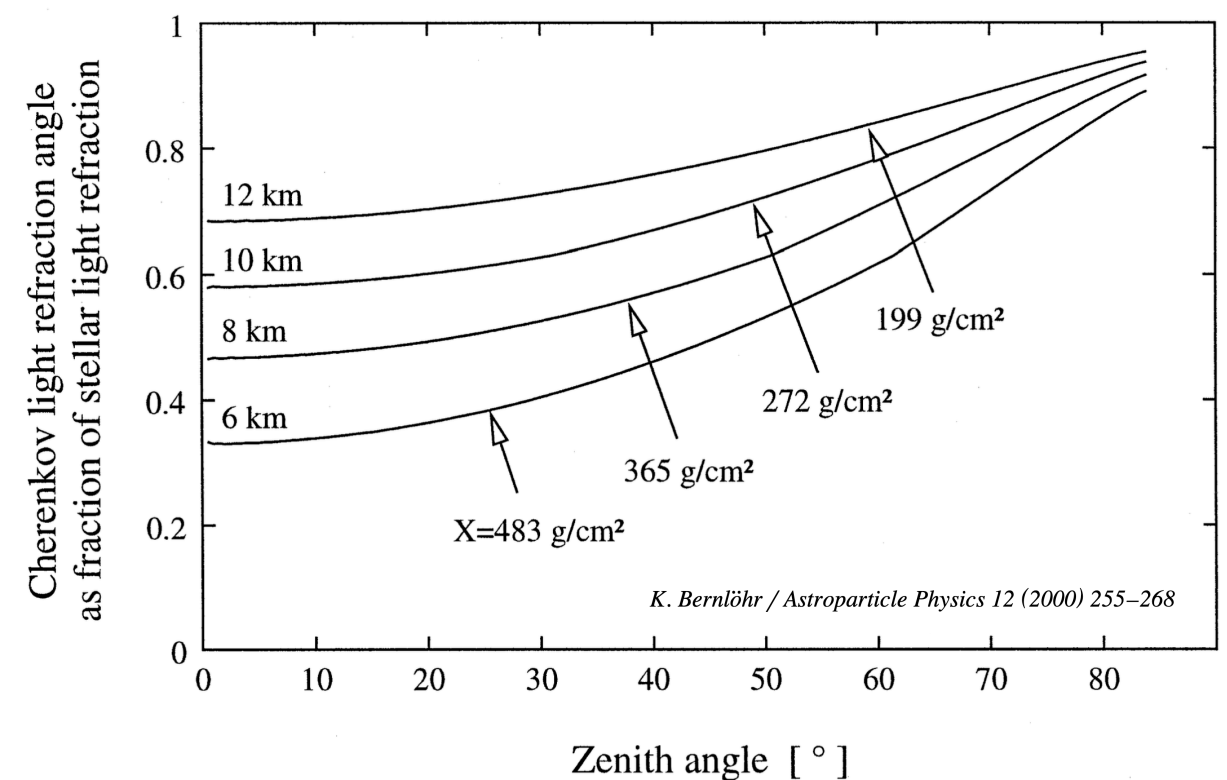
Snell's law:

$$\sin(\theta_2) = \frac{n_1}{n_2} \cdot \sin(\theta_1)$$

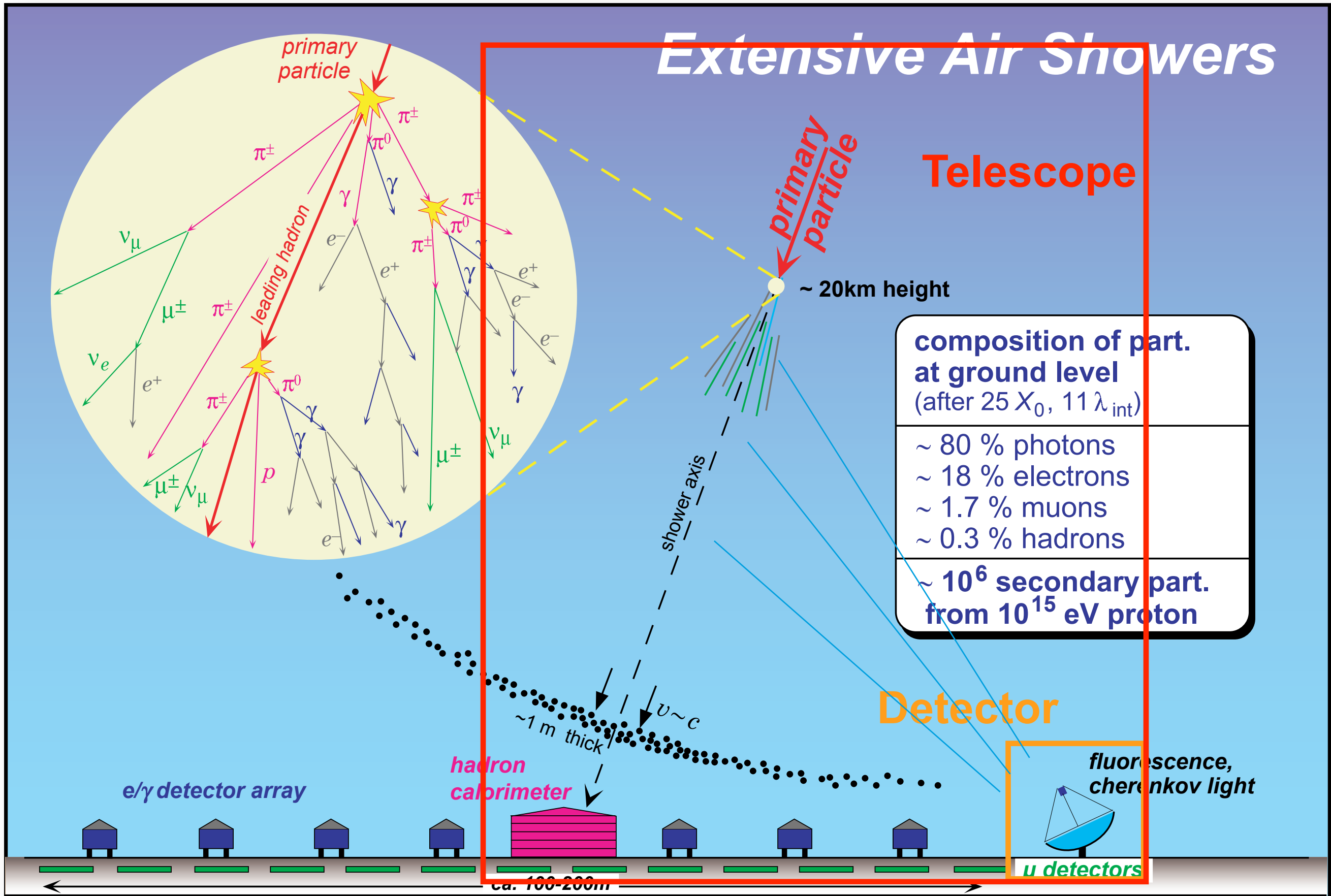
Thesis I. Braun (2007)



Cherenkov light is emitted in the atmosphere



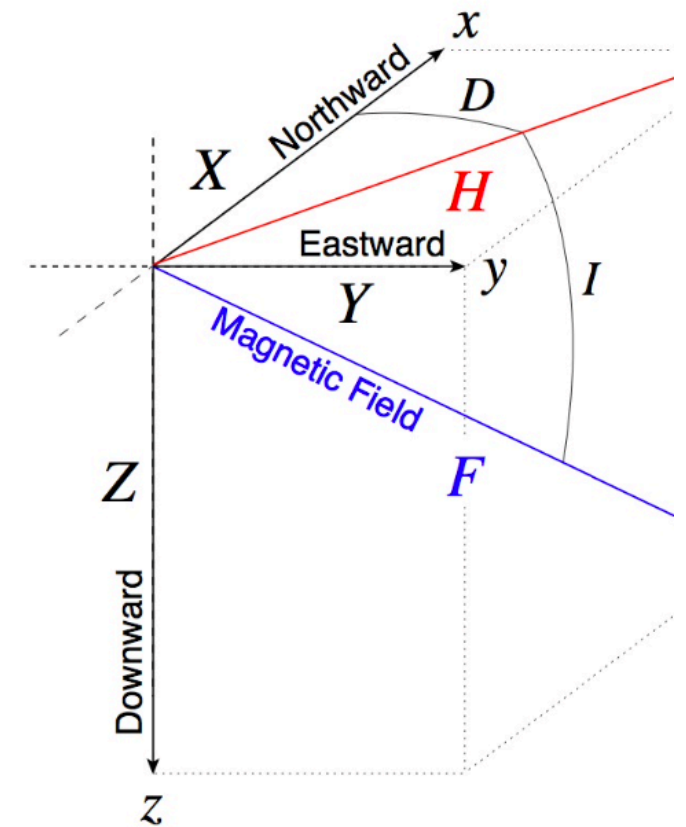
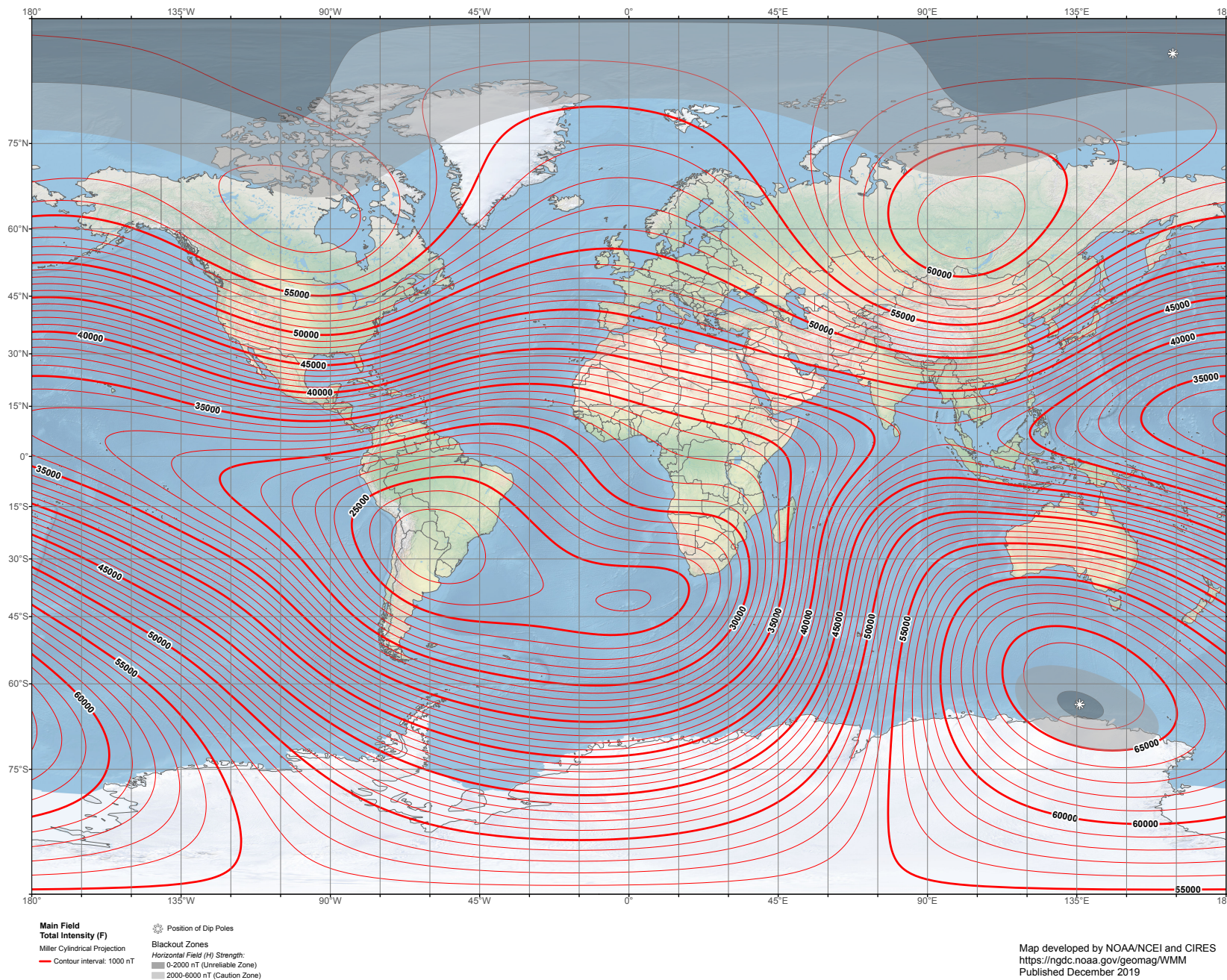
# Extensive Air Showers





# Geomagnetic field.

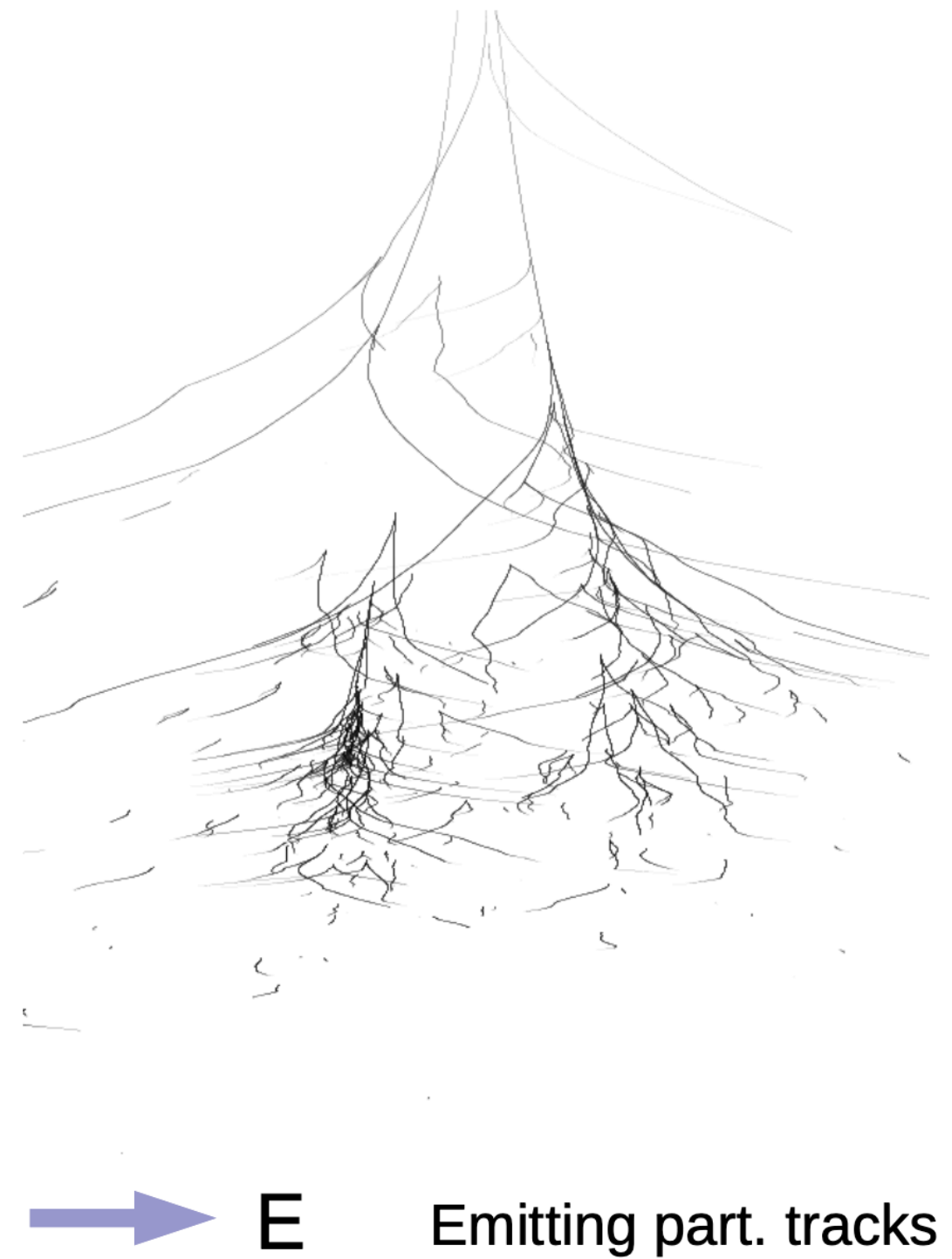
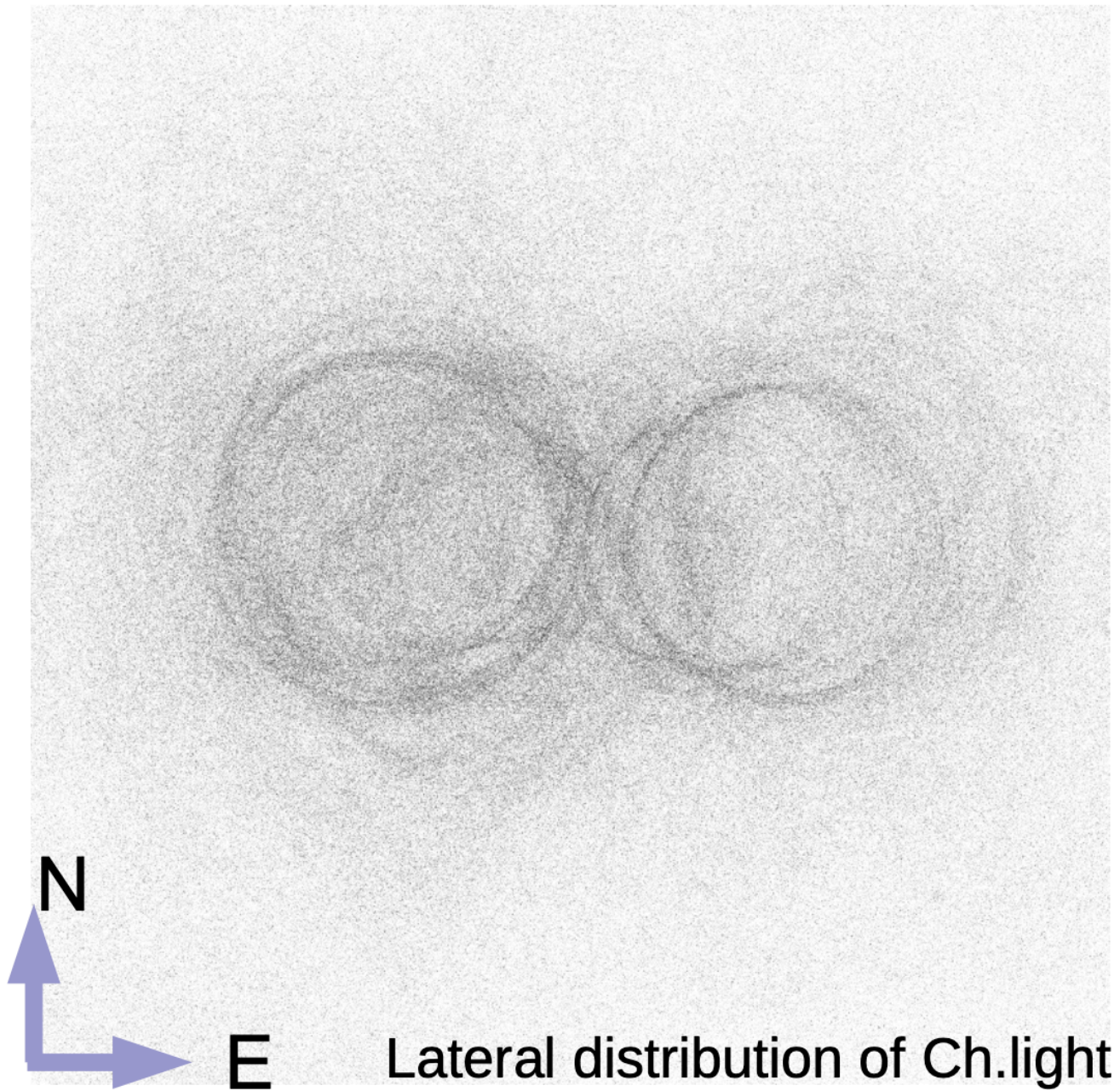
US/UK World Magnetic Model - Epoch 2020.0  
Main Field Total Intensity (F)



Field intensity (F)  
Horizontal component (H)  
Vertical component (Z)  
Declination (D)  
Inclination (H)



# Geomagnetic field.

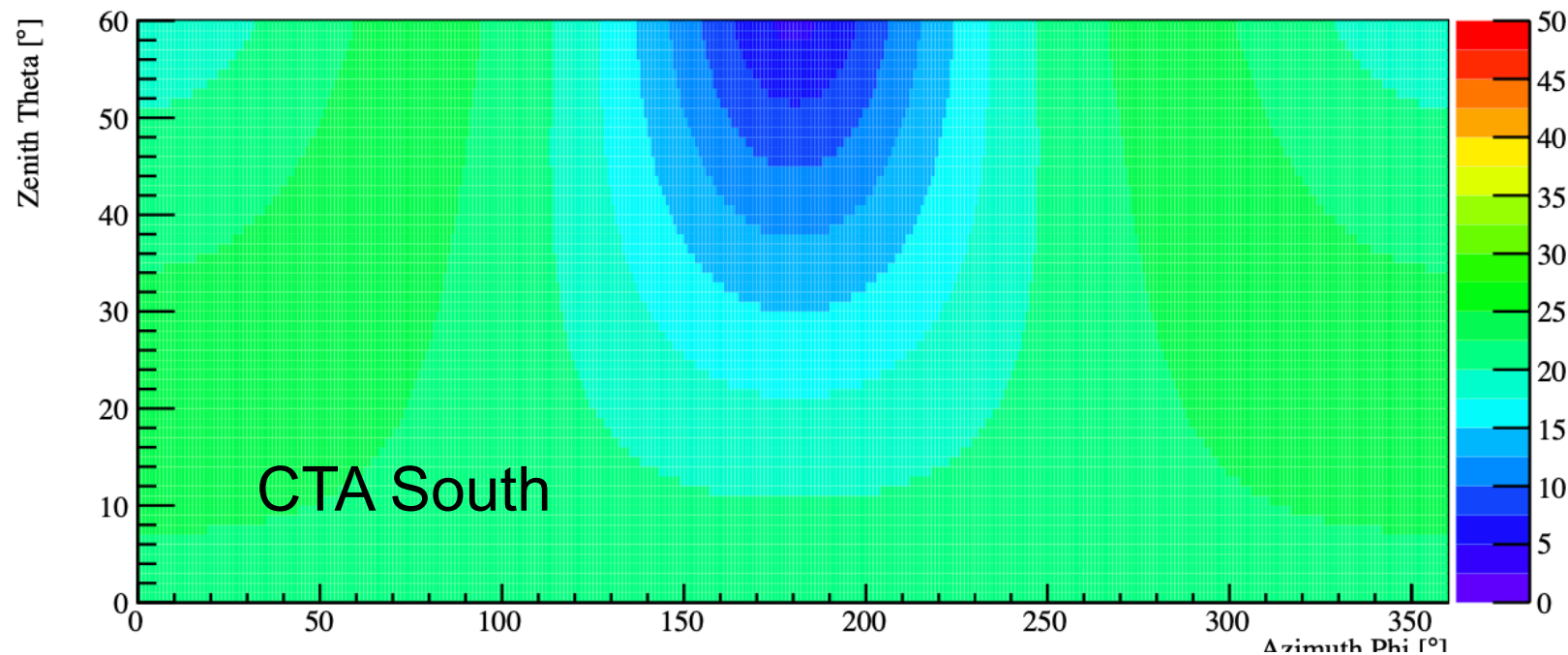


from K.Bernlöhr

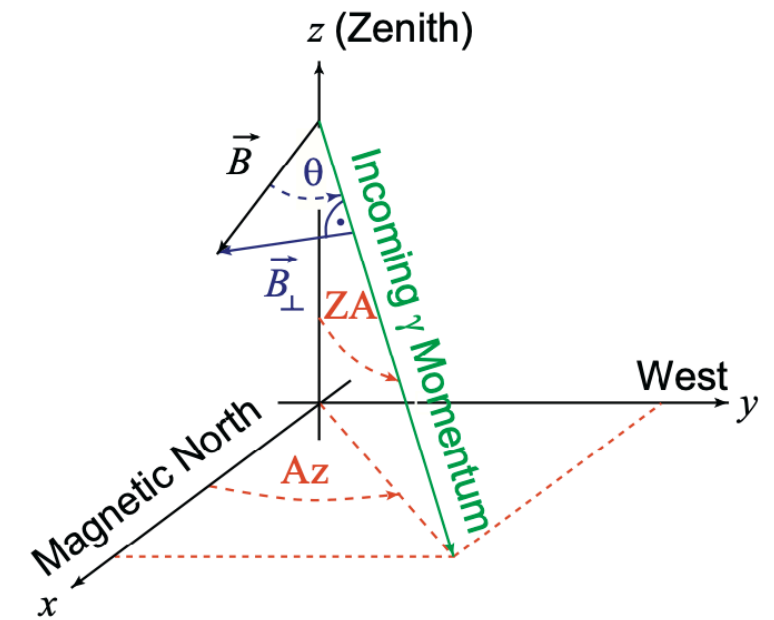
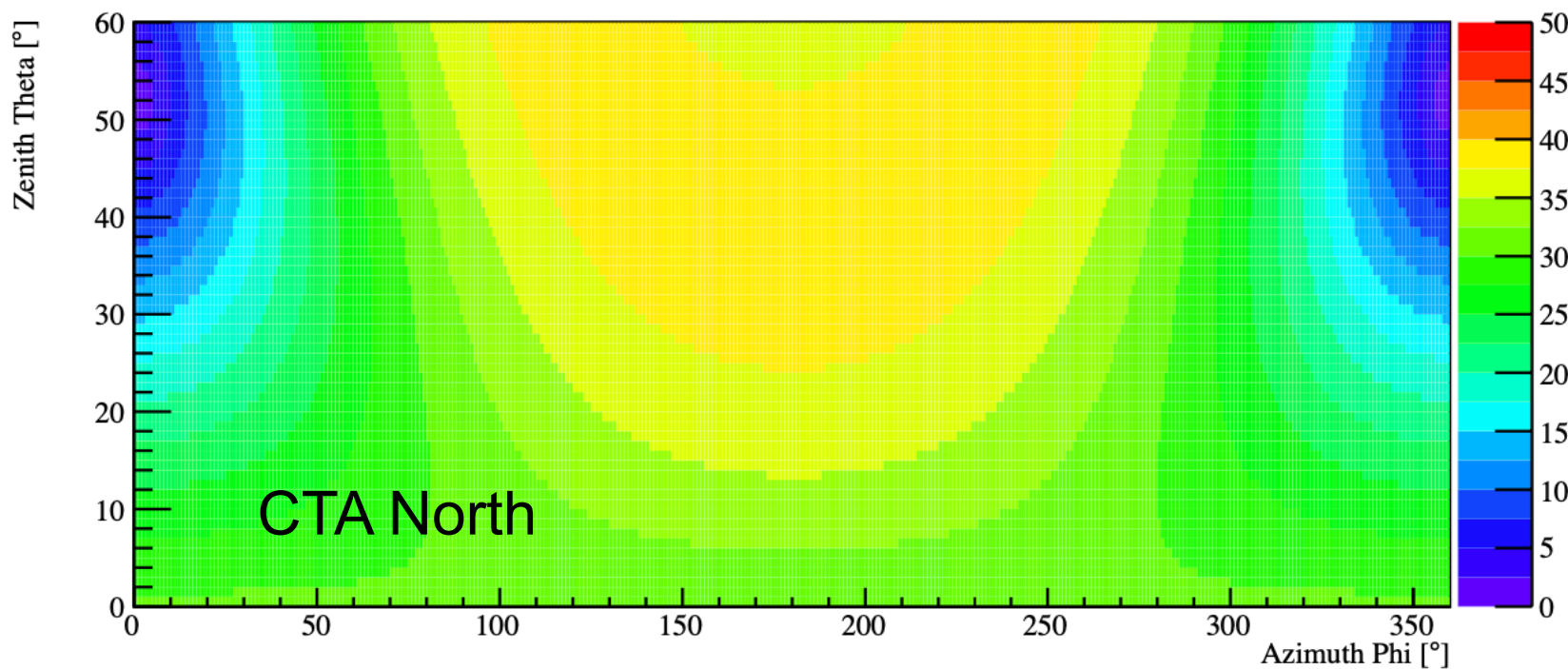
# Magnetic field normal to shower direction.

ALMA 22°59'56"S, 67°45'39"W - Magnetic Field [ $\mu\text{T}$ ]

S.C. Commichau et al. / Nuclear Instruments and Methods in Physics Research A 595 (2008) 572–586



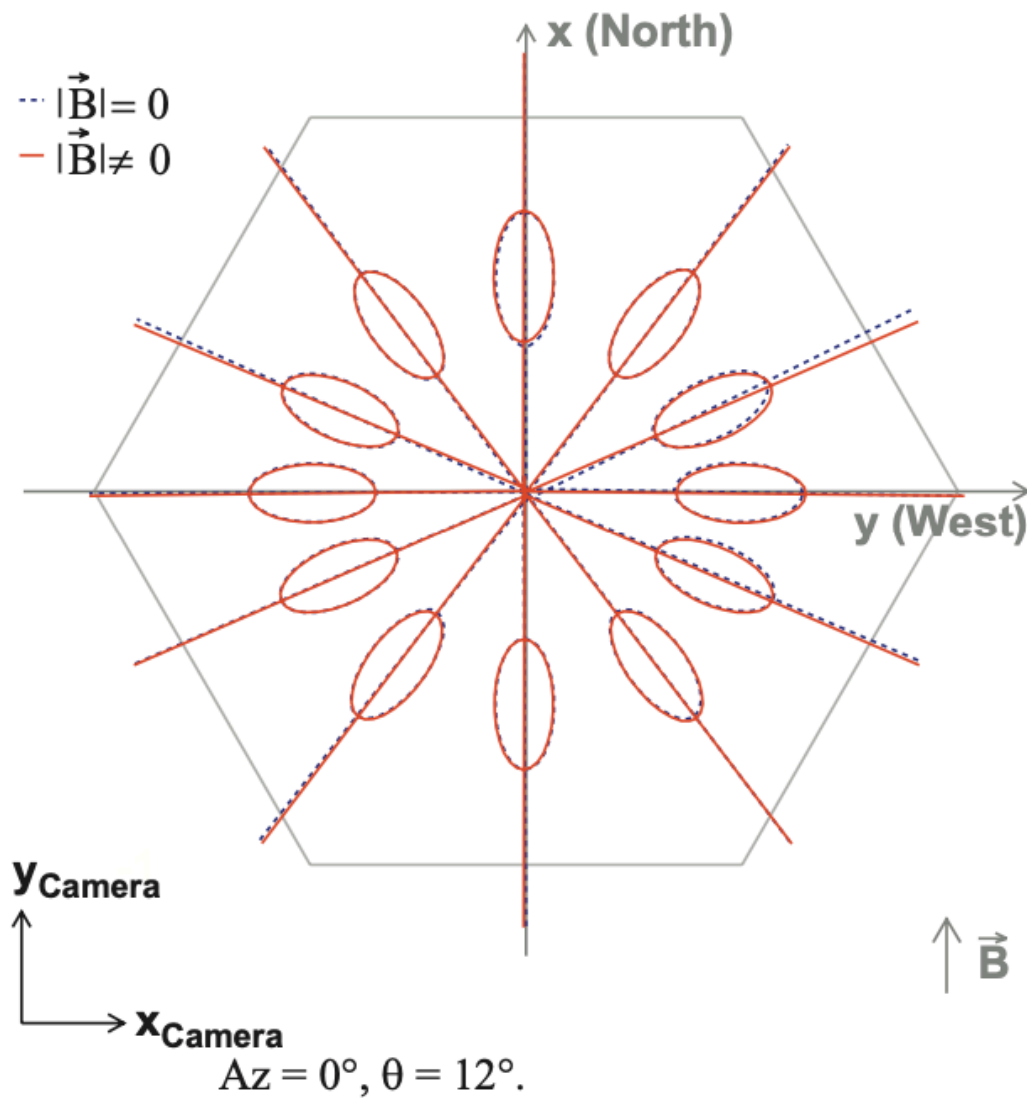
La Palma 28°45'42"N, 17°53'26"W - Magnetic Field [ $\mu\text{T}$ ]



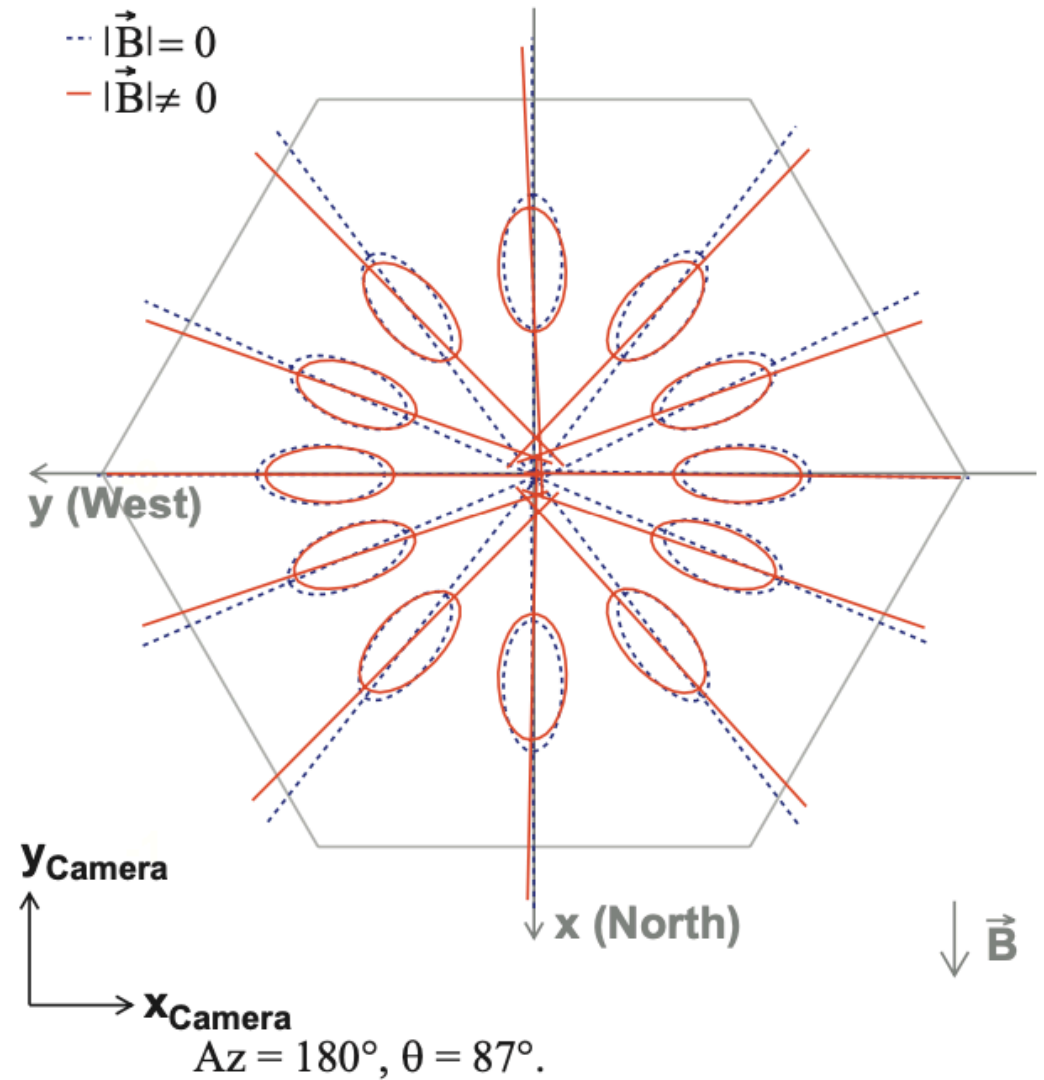


# Geomagnetic field - impact on image reconstruction.

a



b

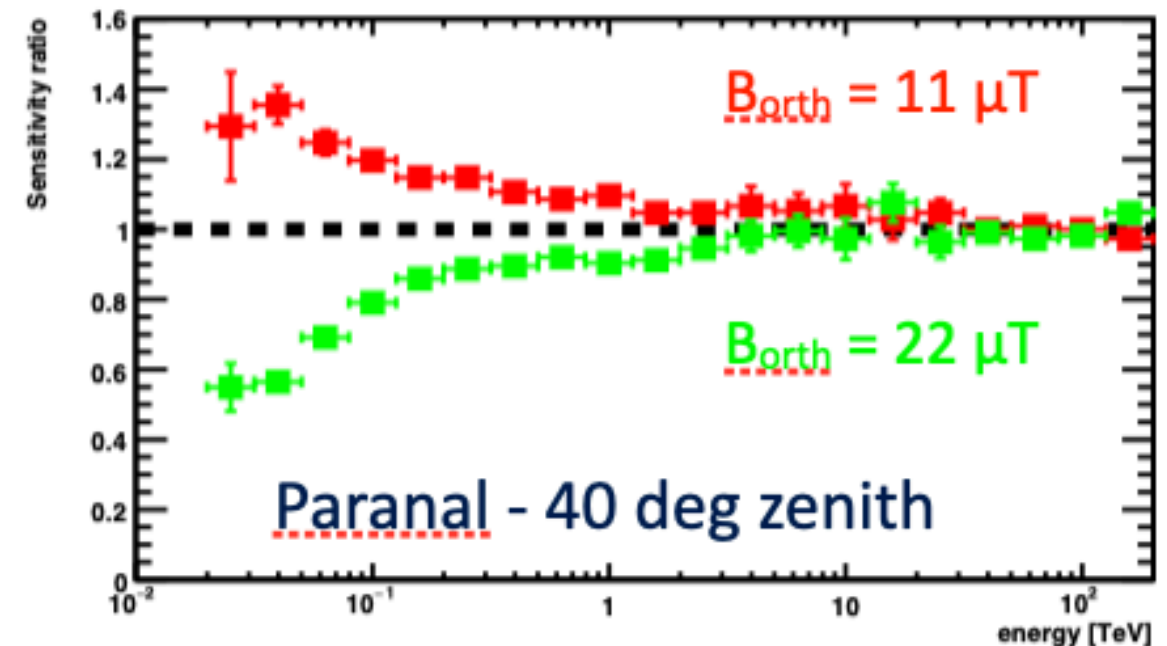
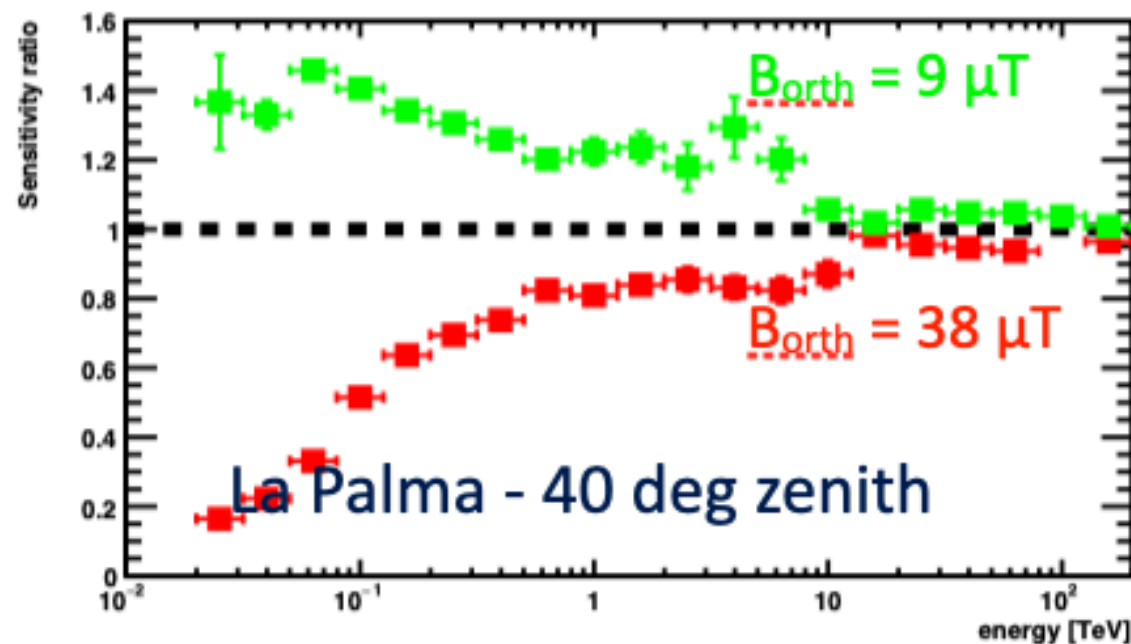
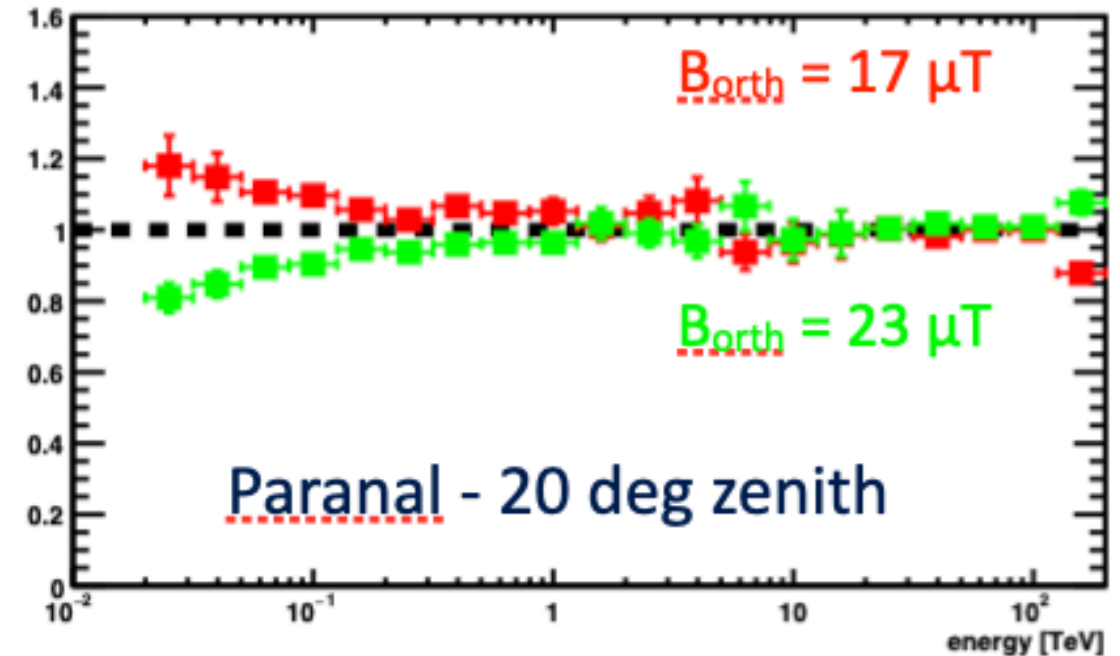
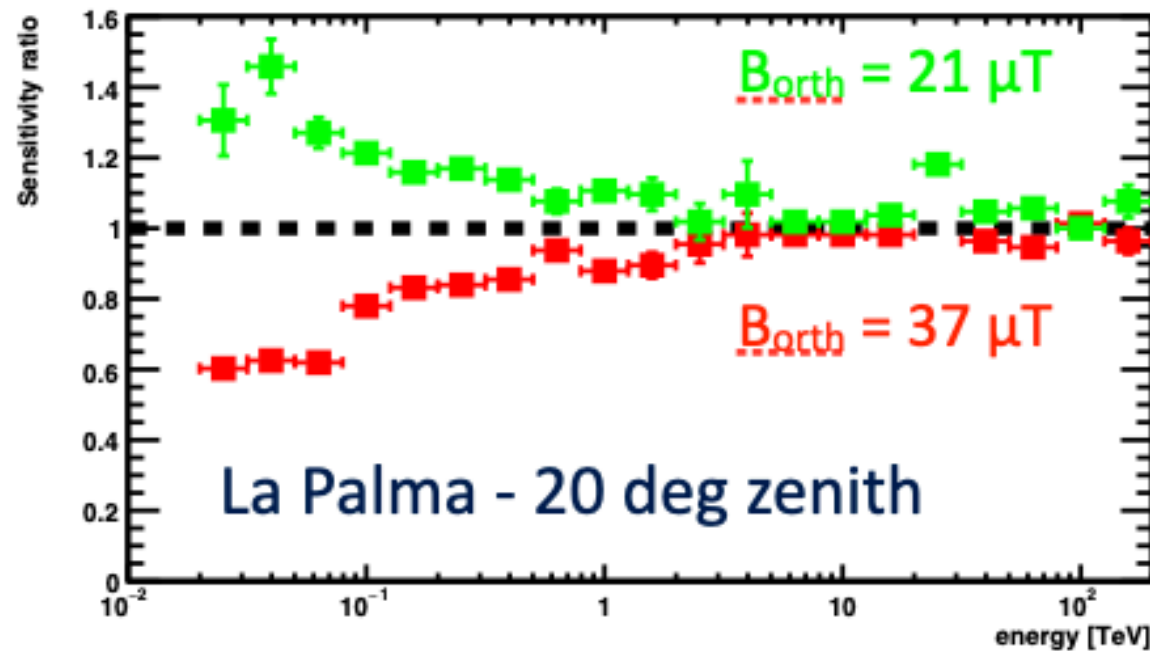


· 450 GeV  $\gamma$ -rays, 100 m impact parameter, ZA = 40°, Az = 0° and 180°,

S.C. Commichau et al. / Nuclear Instruments and Methods in Physics Research A 595 (2008) 572–586

# Geomagnetic field - impact on sensitivity.

Looking North - Looking South

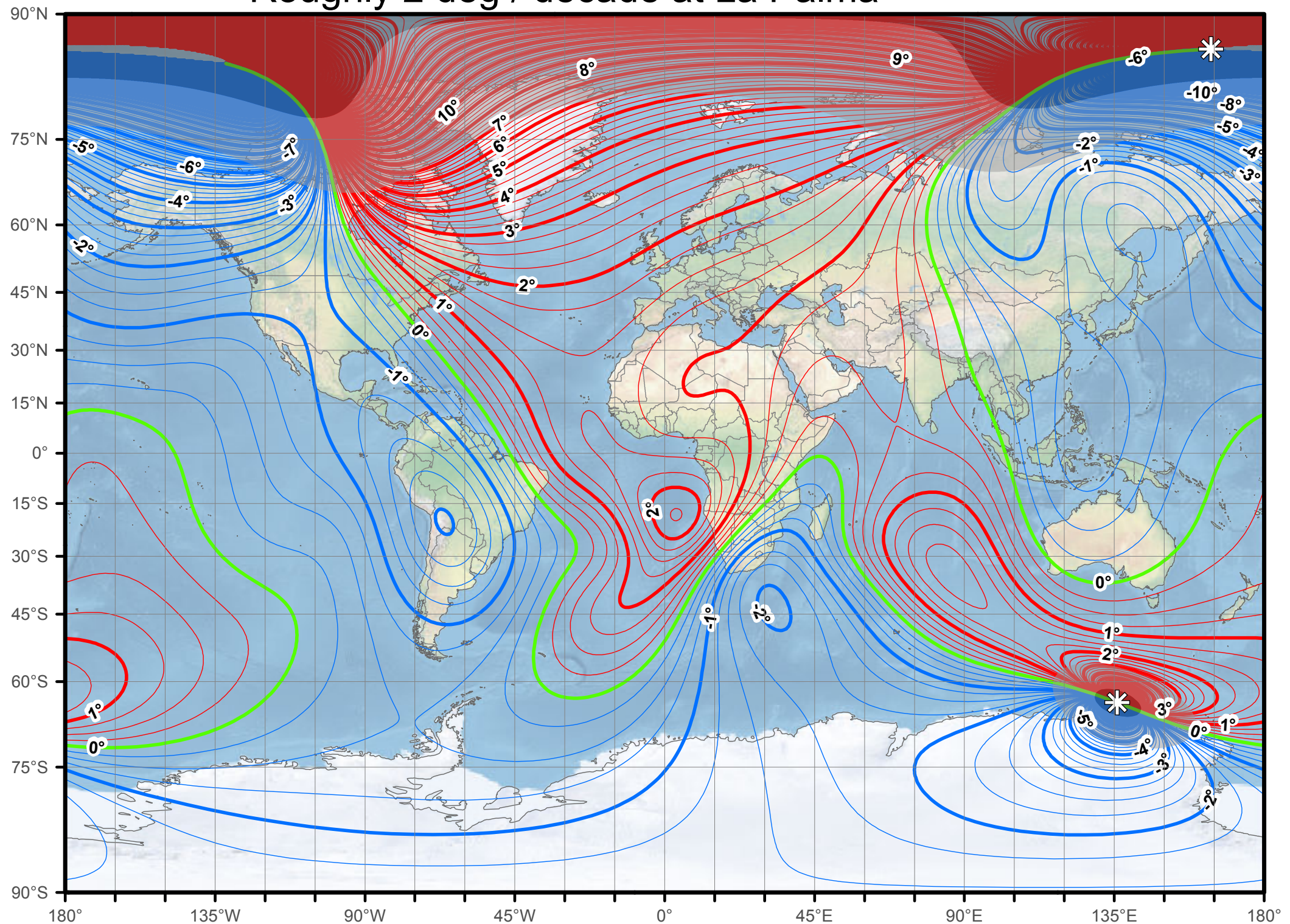


(using analysis techniques ignoring the impact of the geomag. field on the shower development)

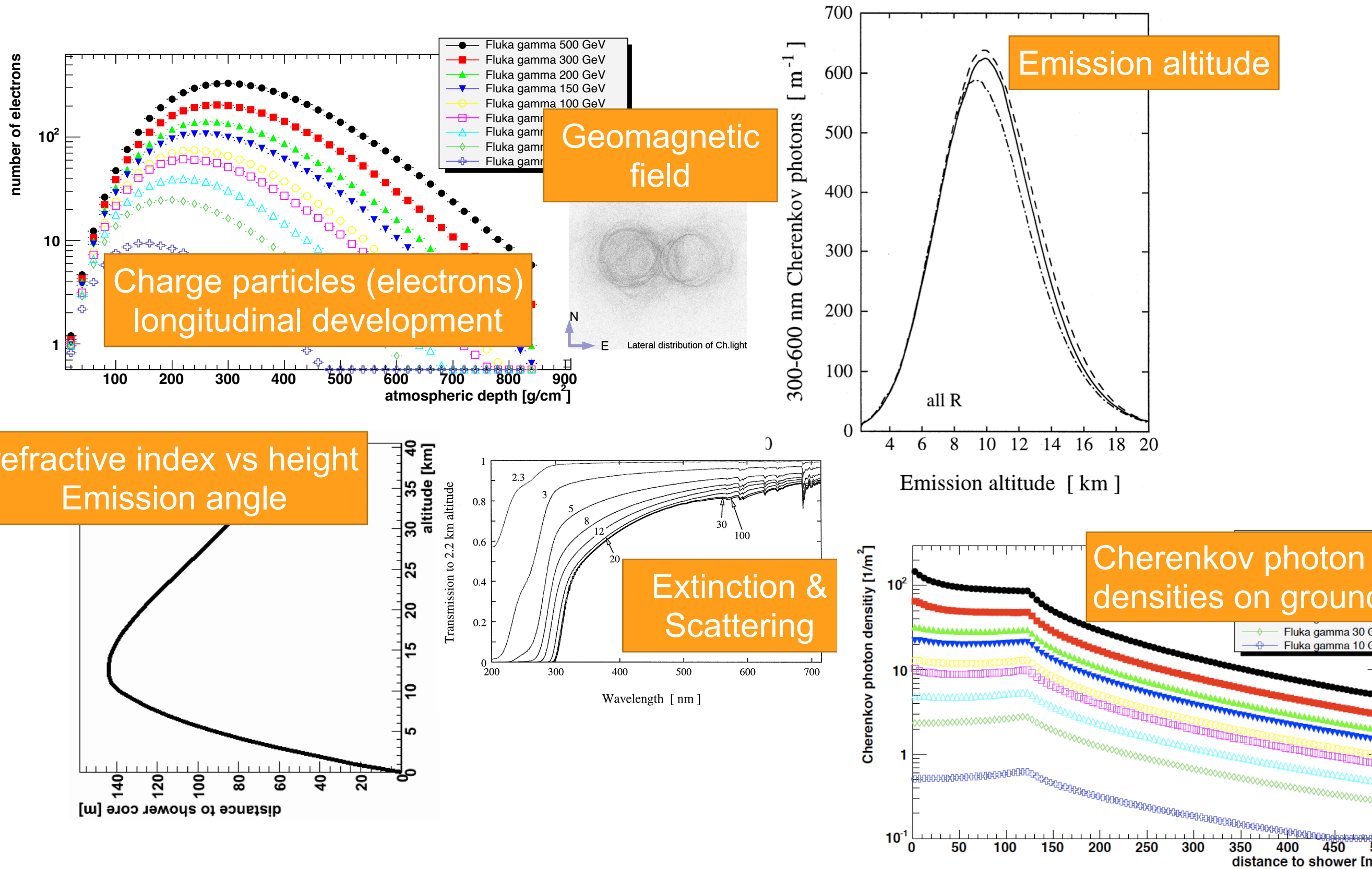


# Geomagnetic field - 10 y change in declination.

Roughly 2 deg / decade at La Palma



# Summary - Cherenkov photons on the ground.





# First detectors

first TeV gamma-ray observatory in the US

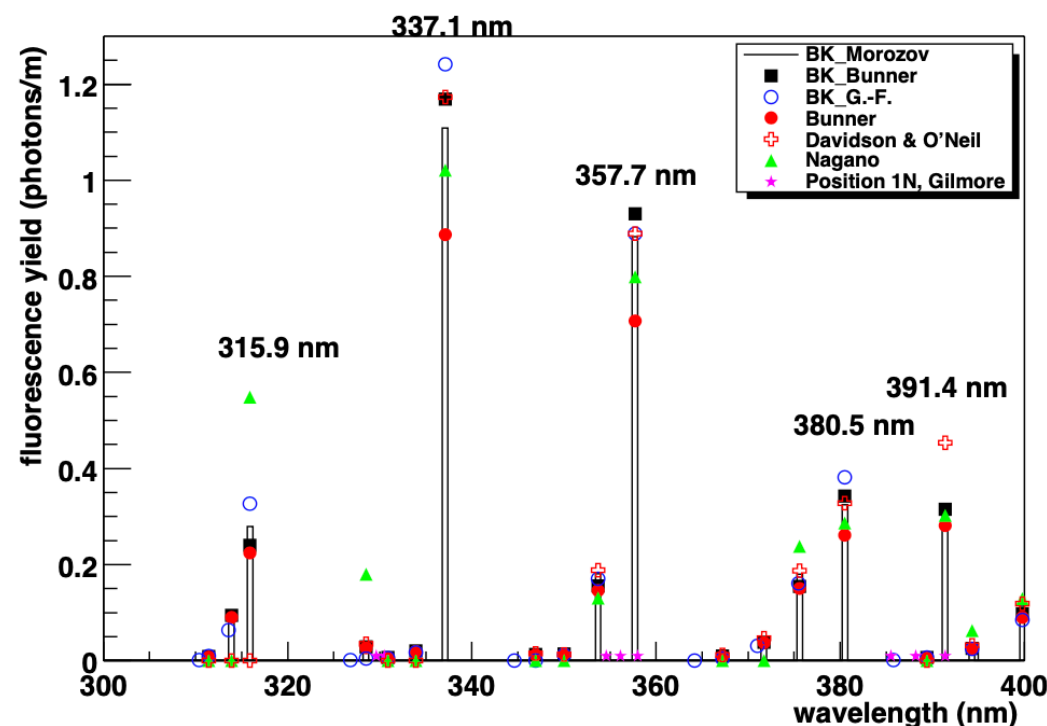


# Backgrounds.

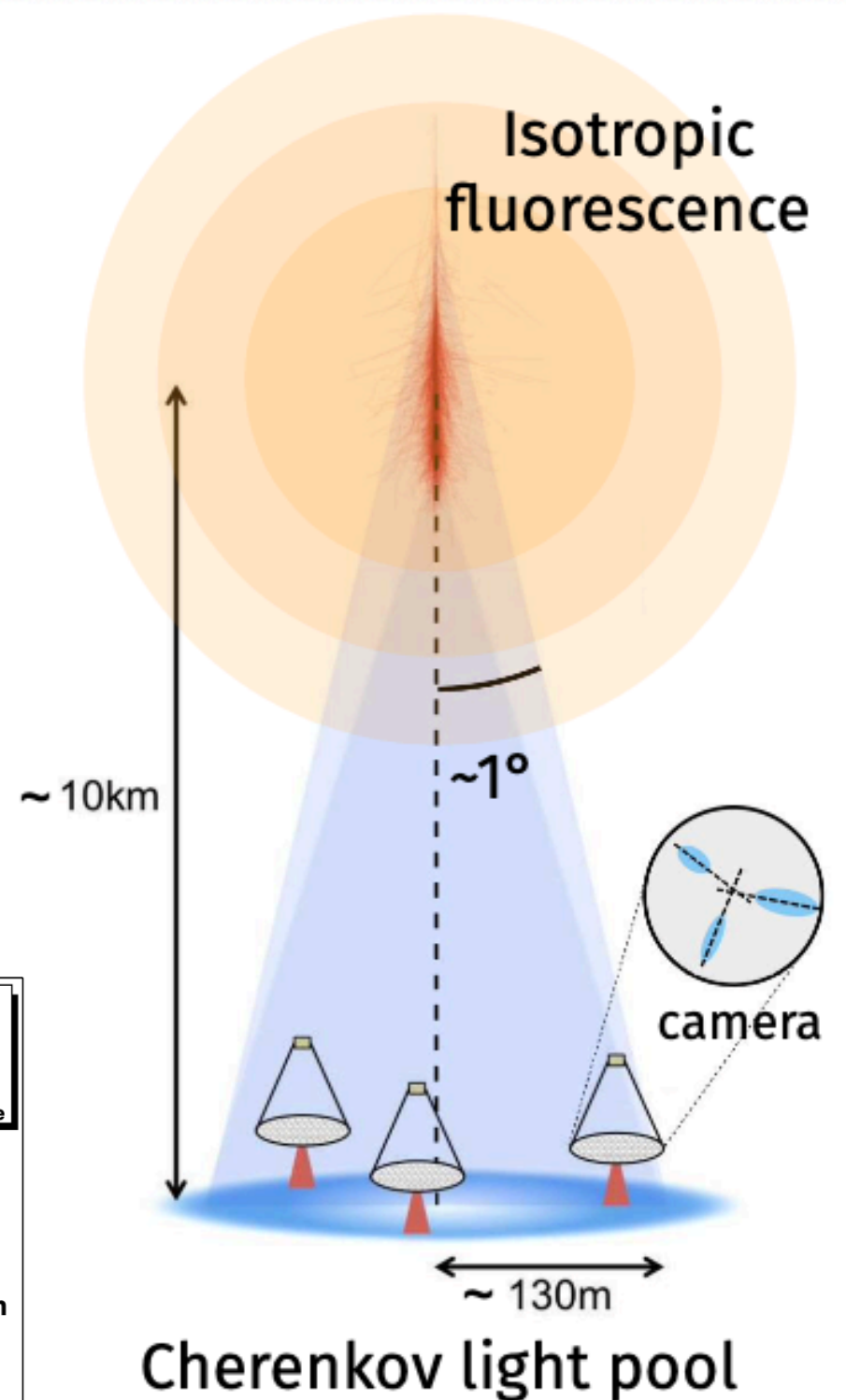


# Fluorescence.

- fluorescence emission from de-excitation of  $N_2$  states (290-430 nm)
- less efficient light emission  
for 1 GeV electron near ground: 30 photons from Cherenkov light vs 4 photons from fluorescence light (per m track length)
- longer time profile: microseconds vs 10s of nanoseconds

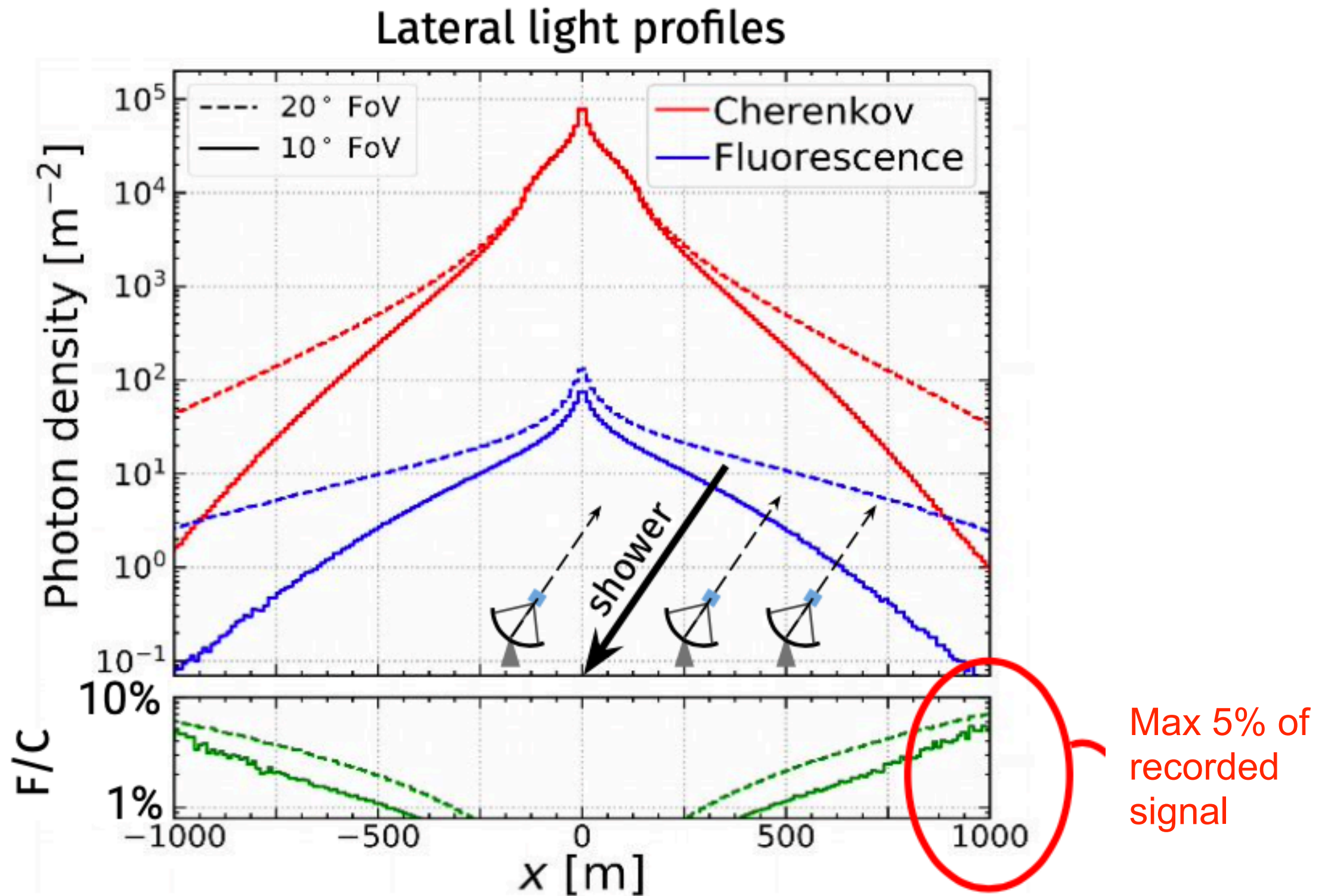


Keilhauer et al 2005

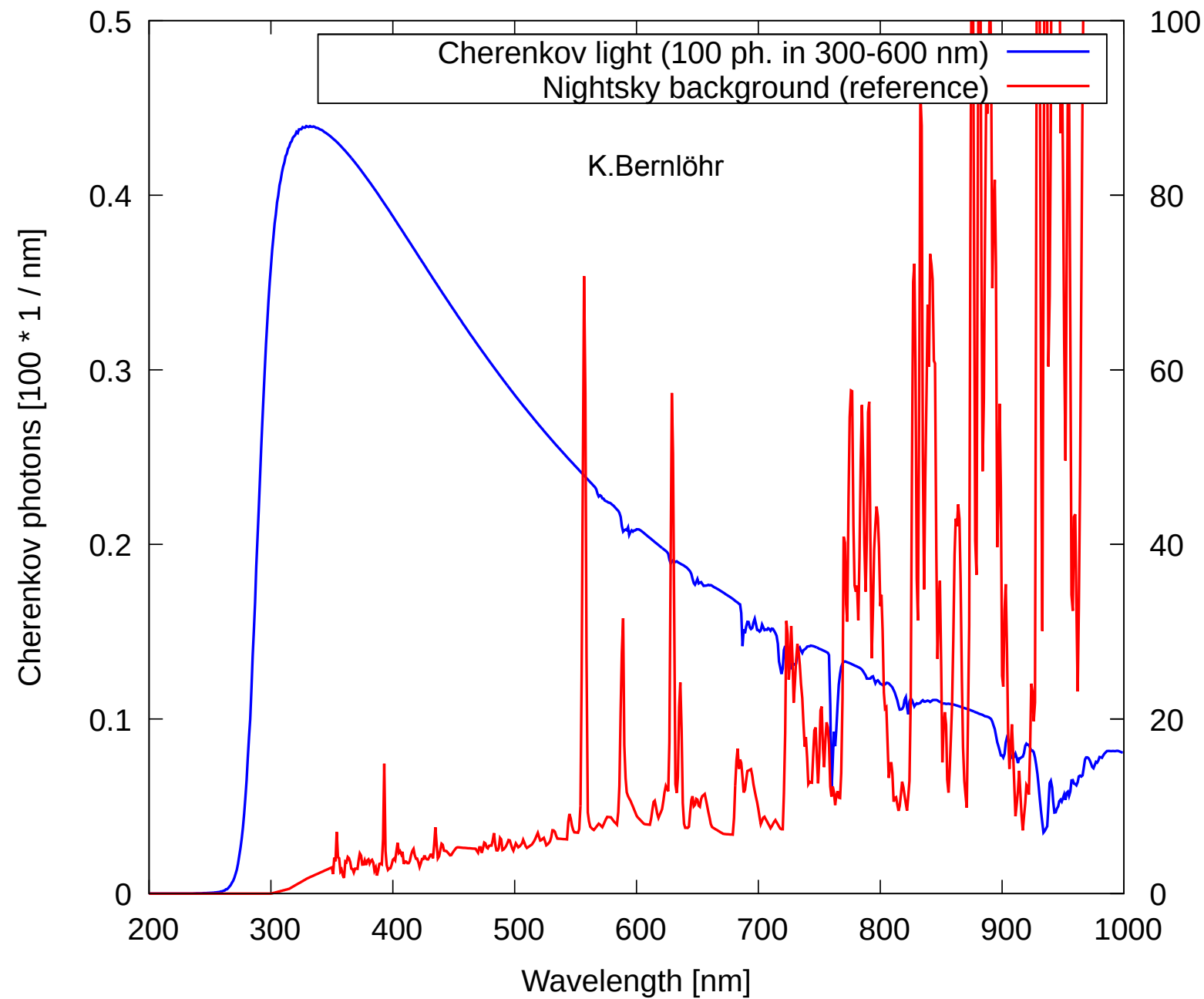


Morcuende et al 2005

# Fluorescence.

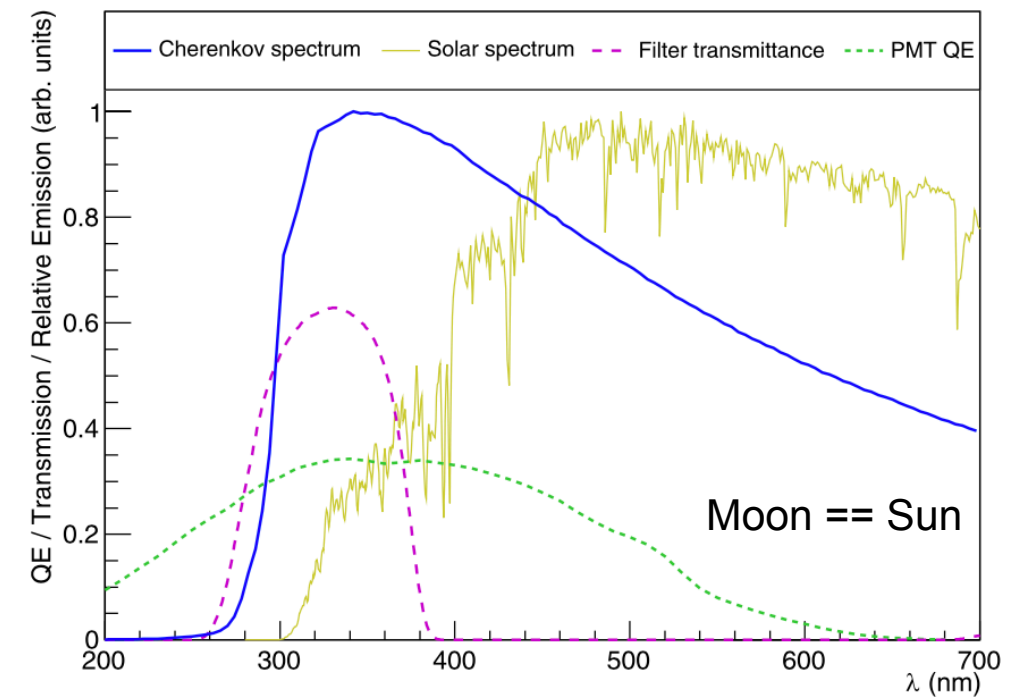


# Night sky background.

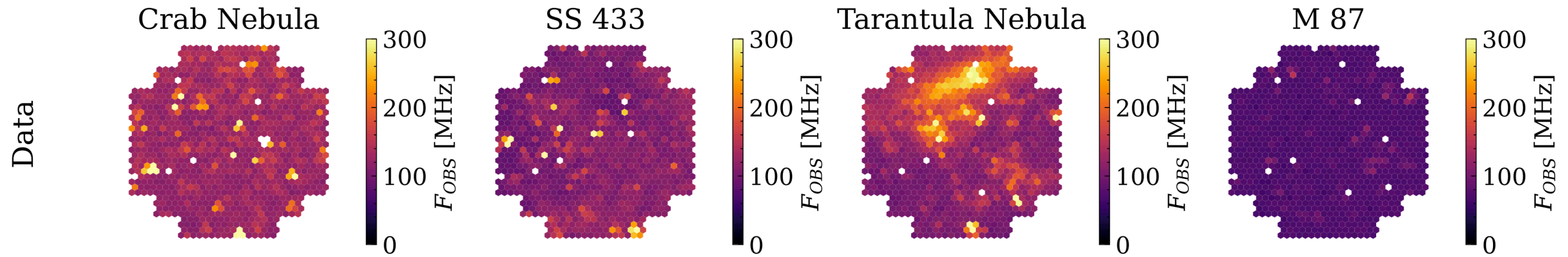


NSB photons [ $1 / (\text{nm m}^2 \text{ ns sr})$ ]

*S. Archambault et al. / Astroparticle Physics 91 (2017) 34–43*



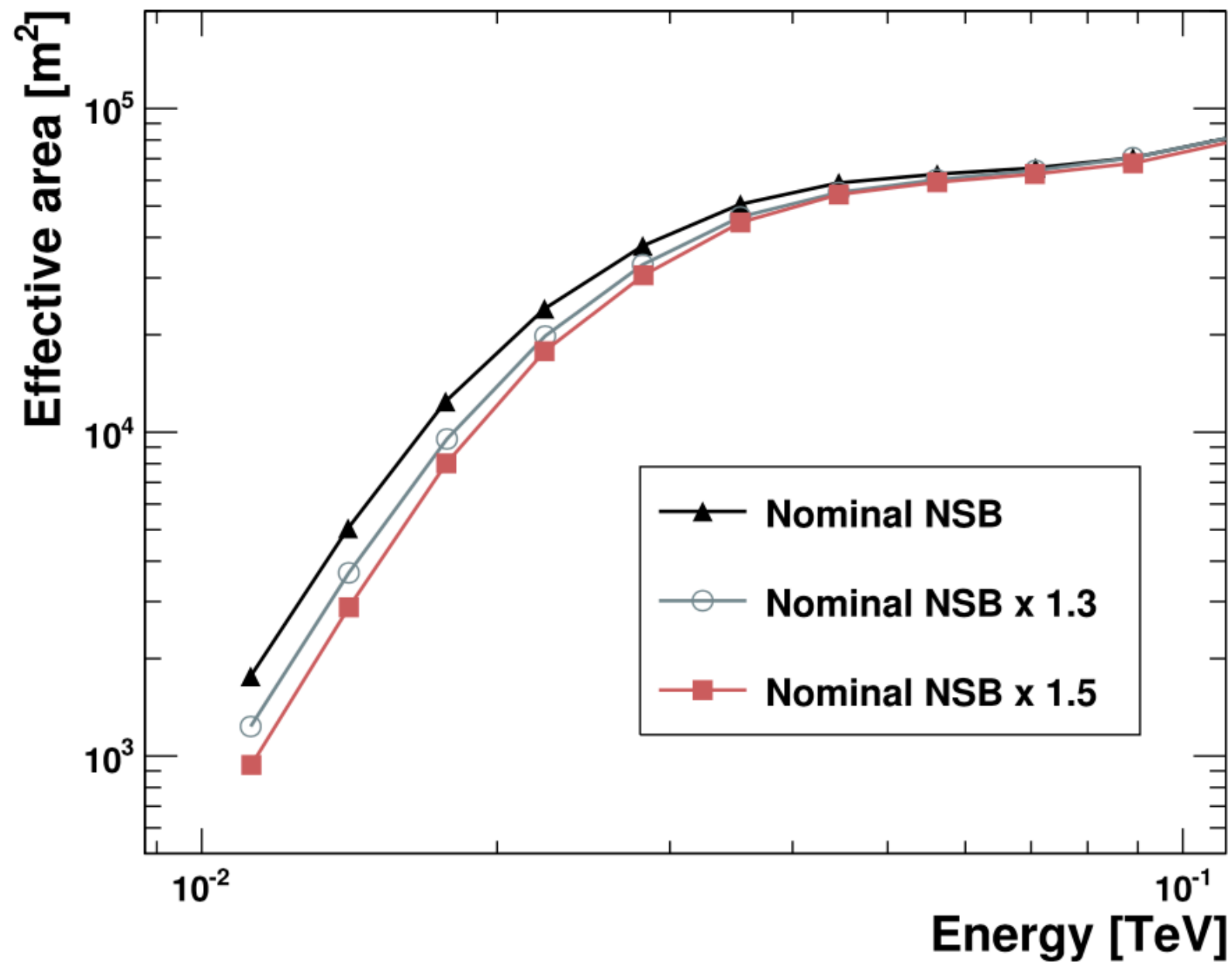
# Night-sky background - stars



Roellinghoff et al 2025



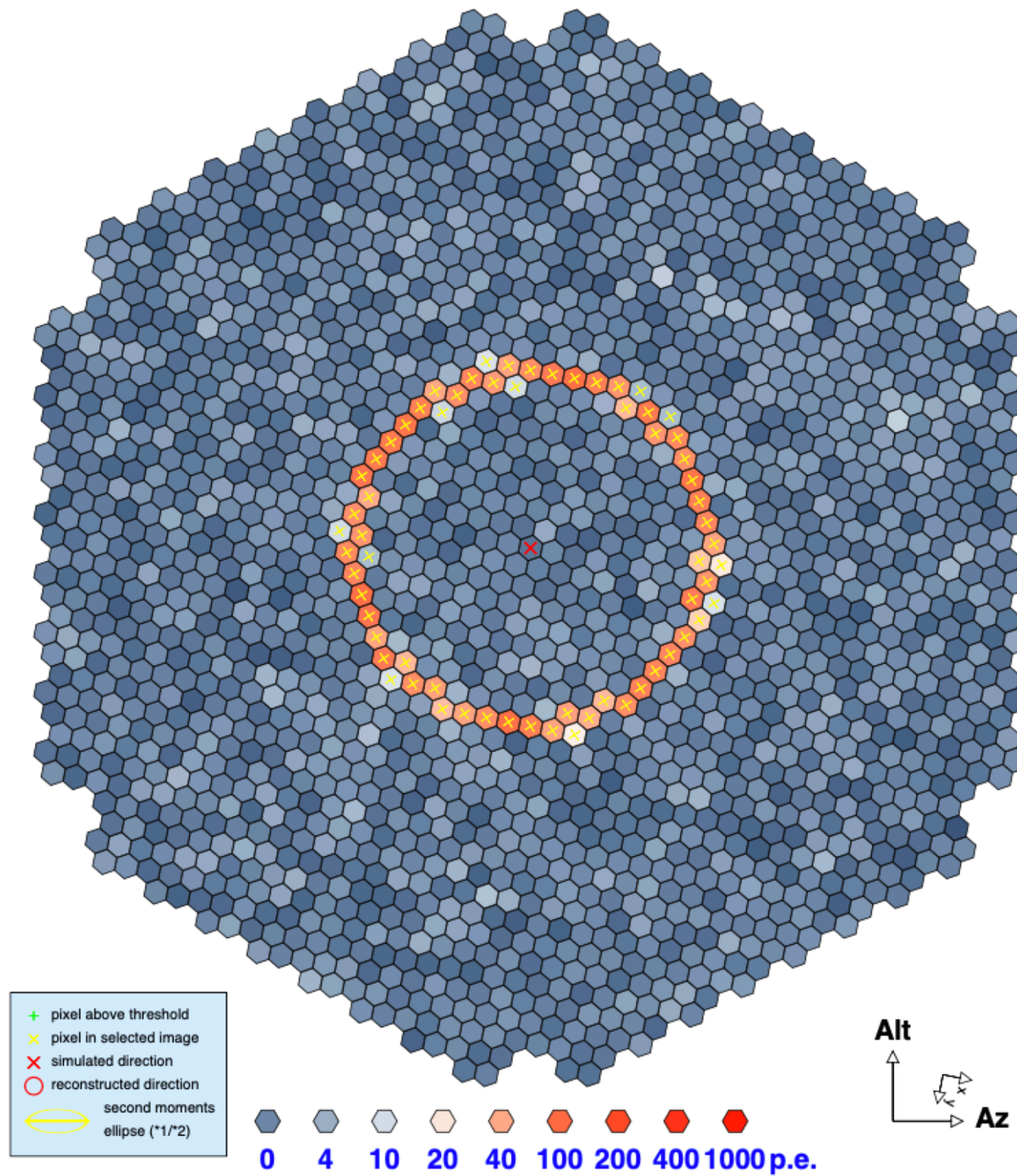
# Impact of high night-sky-background light levels.



*T. Hassan et al. / Astroparticle Physics 93 (2017) 76–85*

# Muons.

K.Bernlöhr



# Muons

arXiv > astro-ph > arXiv:1907.04375

Astrophysics > Instrumentation and Methods for Astrophysics

[Submitted on 9 Jul 2019]

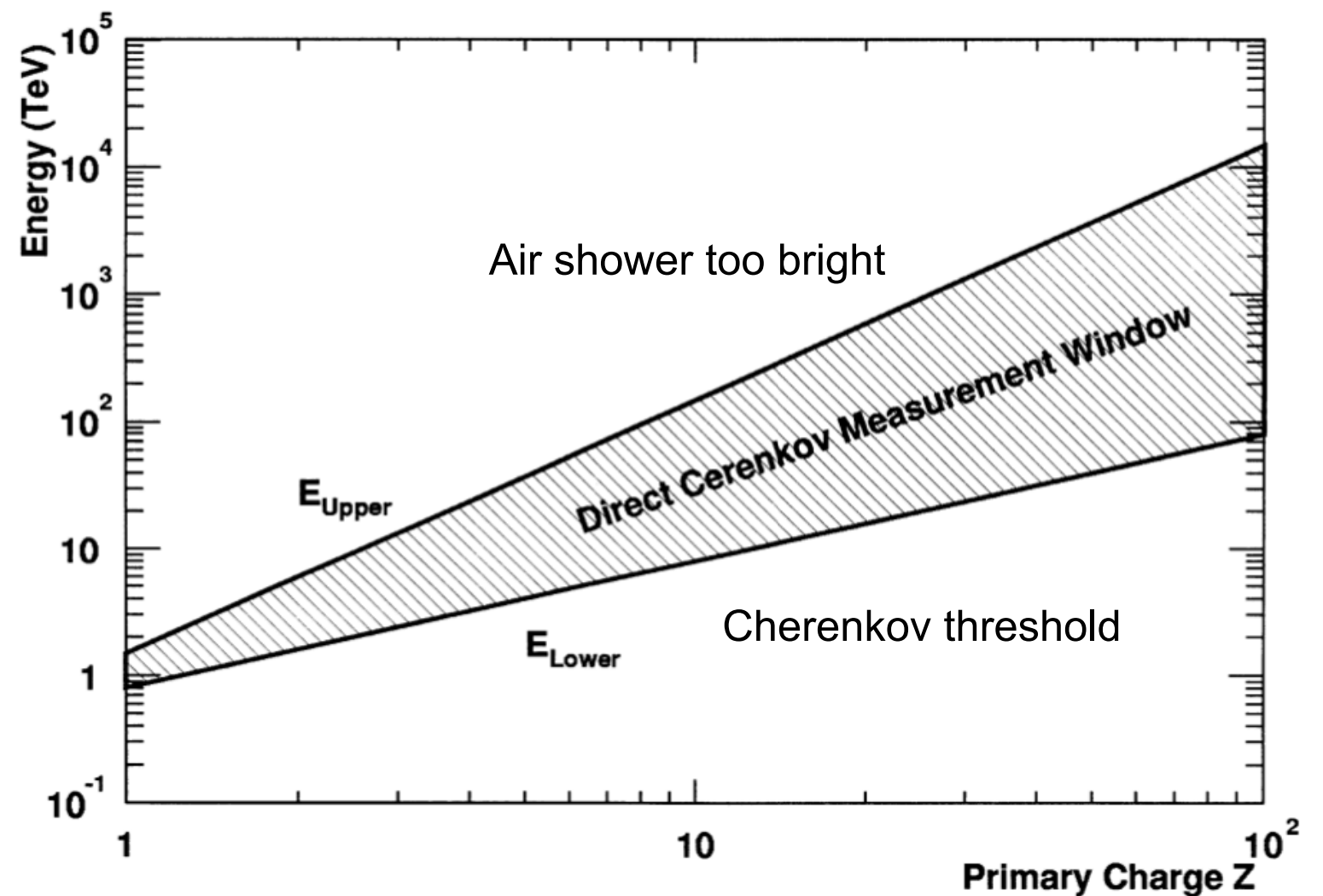
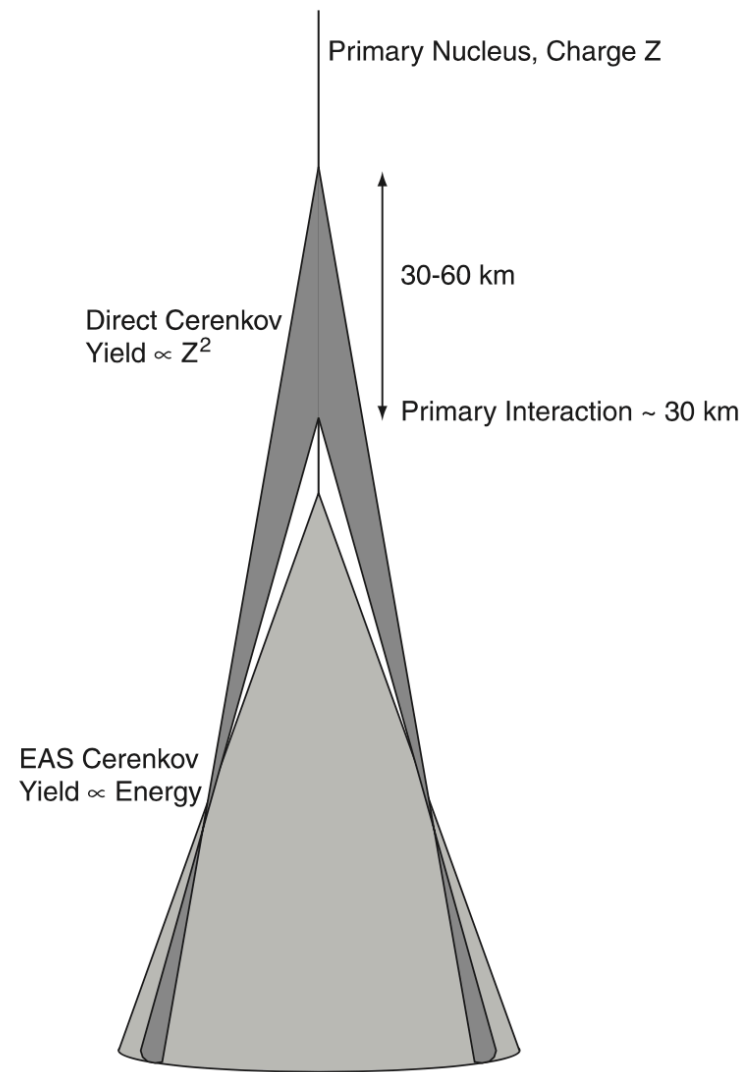
## Using Muon Rings for the Calibration of the Cherenkov Telescope Array: A Systematic Review of the Method and its Potential Accuracy

Markus Gaug, Steven Fegan, Alison Mitchell, Maria-Concetta Maccarone, Teresa Mineo, Akira Okumura

The analysis of ring images produced by muons in an Imaging Atmospheric Cherenkov Telescope (IACT) provides a powerful and precise method to calibrate the IACT optical throughput and monitor its optical point-spread function (PSF). First proposed in collaboration in the early 90's, this method has been refined by the so-called second generation of IACT experiments: H.E.S.S., MAGIC and VERITAS. We review here the progress made with these instruments and investigate the applicability of the method for the different telescope types forming the future Cherenkov Telescope Array (CTA). We find several additional systematic effects not yet taken into account by previous authors and propose several new analytical methods for the analysis. Slight modifications in hardware and analysis need to be made to ensure that such a calibration works as accurately as required for the CTA. We derive analytic estimates for the expected muon data rates for optical throughput calibration, fielding and monitoring of the optical PSF. The achievable statistical and systematic uncertainties of the method are also assessed.

# Direct Cherenkov Light (not a background).

$$\frac{dN}{dx} = 2\pi\alpha z^2 \int_{\lambda_1}^{\lambda_2} \left(1 - \frac{1}{n^2\beta^2}\right) \frac{d\lambda}{\lambda^2} = 2\pi\alpha z^2 \int_{\lambda_1}^{\lambda_2} \sin^2 \Theta \frac{d\lambda}{\lambda^2}$$

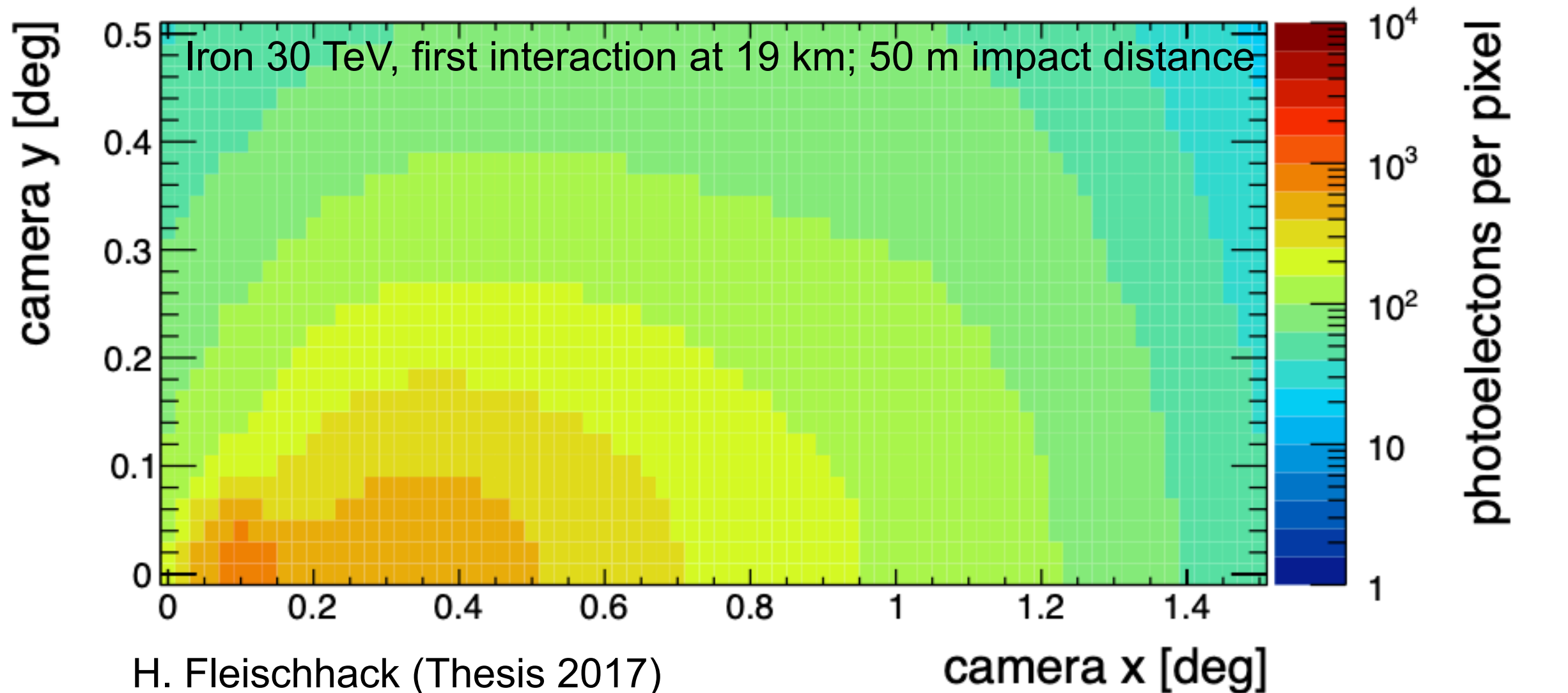


*D.B. Kieda et al. / Astroparticle Physics 15 (2001) 287–303*



# Direct Cherenkov Light (not a background).

$$\frac{dN}{dx} = 2\pi\alpha z^2 \int_{\lambda_1}^{\lambda_2} \left(1 - \frac{1}{n^2\beta^2}\right) \frac{d\lambda}{\lambda^2} = 2\pi\alpha z^2 \int_{\lambda_1}^{\lambda_2} \sin^2\Theta \frac{d\lambda}{\lambda^2}$$



Primary Charge  $z$

*D.B. Kieda et al. / Astroparticle Physics 15 (2001) 287–303*

# Simulations.

## CORSIKA.

## sim\_telarray.

(others packages exist)

ICRC 1990.

HE 7.3-3

## AIR SHOWER SIMULATIONS FOR KASCADE

J.N.Capdevielle<sup>1</sup>, P.Gabriel, H.J.Gils, P.K.F.Grieder<sup>2</sup>, D.Heck, N.Heide,  
J.Knapp, H.J.Mayer, J.Oehlschläger, H.Rebel, G.Schatz, and T.Thouw

Kernforschungszentrum und Universität Karlsruhe,  
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F-33170 Gradignan, France

<sup>2</sup>Physikalisches Institut der Universität Bern,  
CH-3012 Bern, Switzerland

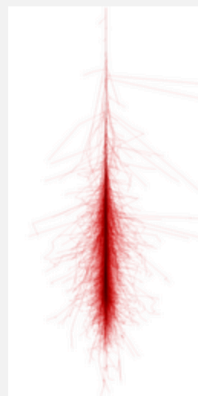
### Abstract

A detailed simulation program for extensive air showers and first results are presented. The mass composition of cosmic rays with  $E_0 \geq 10^{15}$  eV can be determined by measuring electrons, muons and hadrons simultaneously with the KASCADE detector.

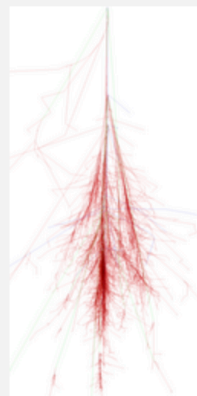
# CORSIKA

<https://www.iap.kit.edu/corsika/>

## CORSIKA 7



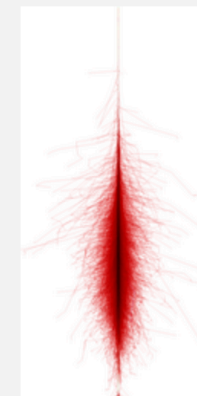
Photon shower [↗](#)



Proton shower [↗](#)



Iron shower [↗](#)



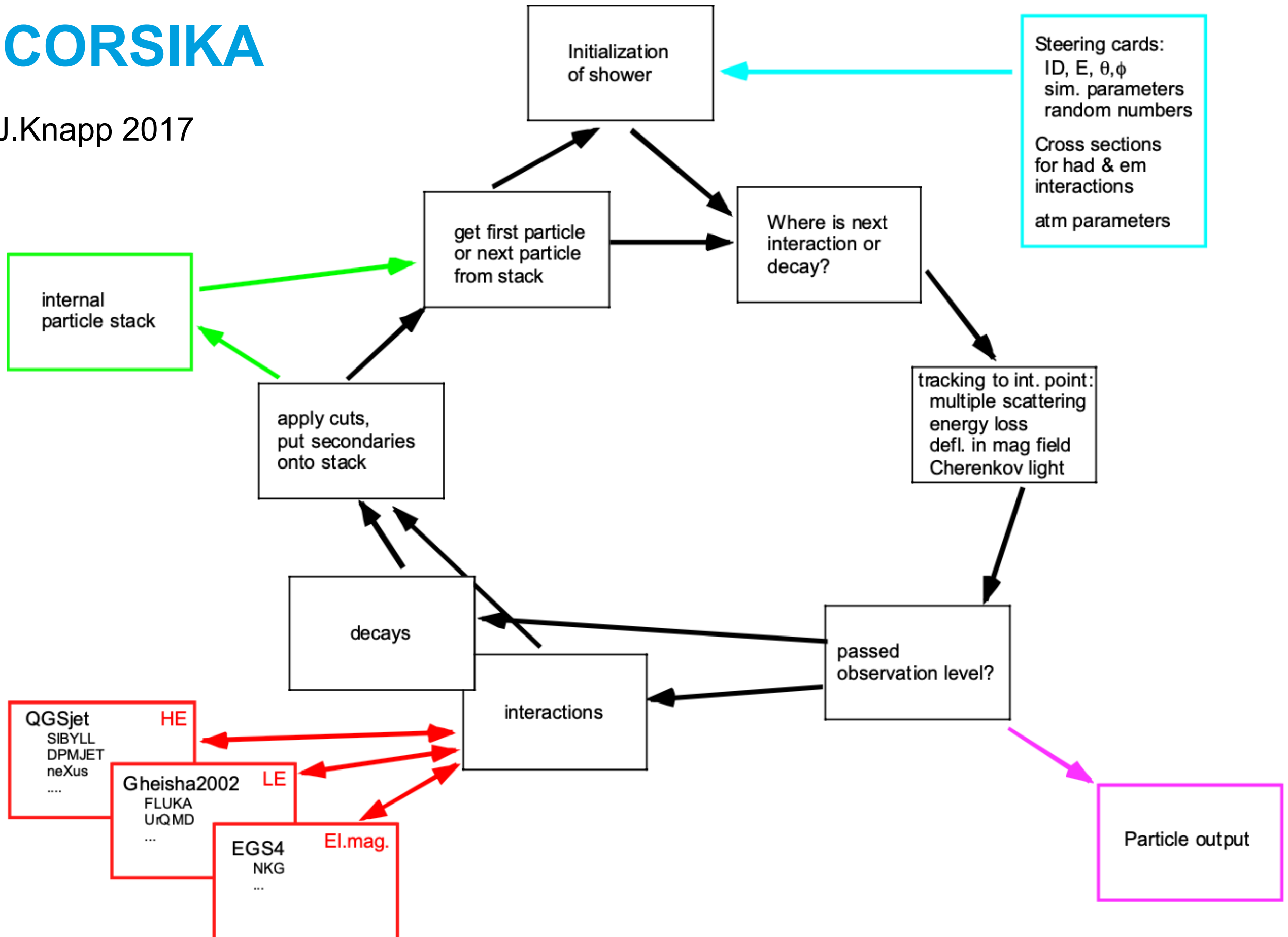
Muon shower [↗](#)

(Compiled by Fabian Schmidt, University of Leeds, UK)



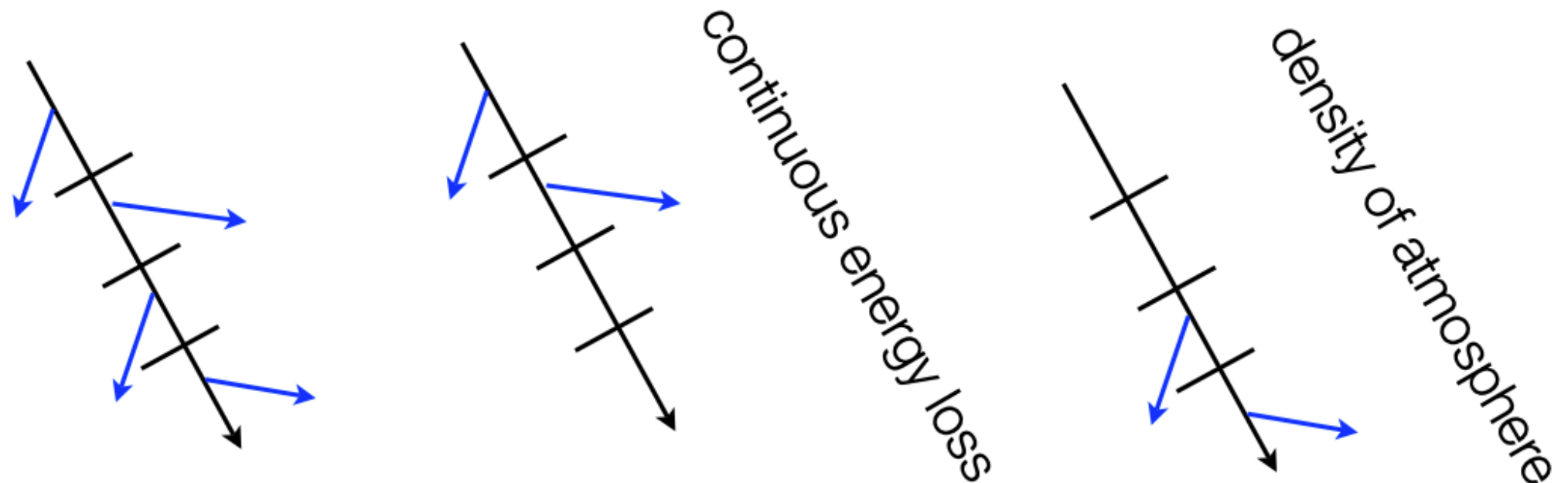
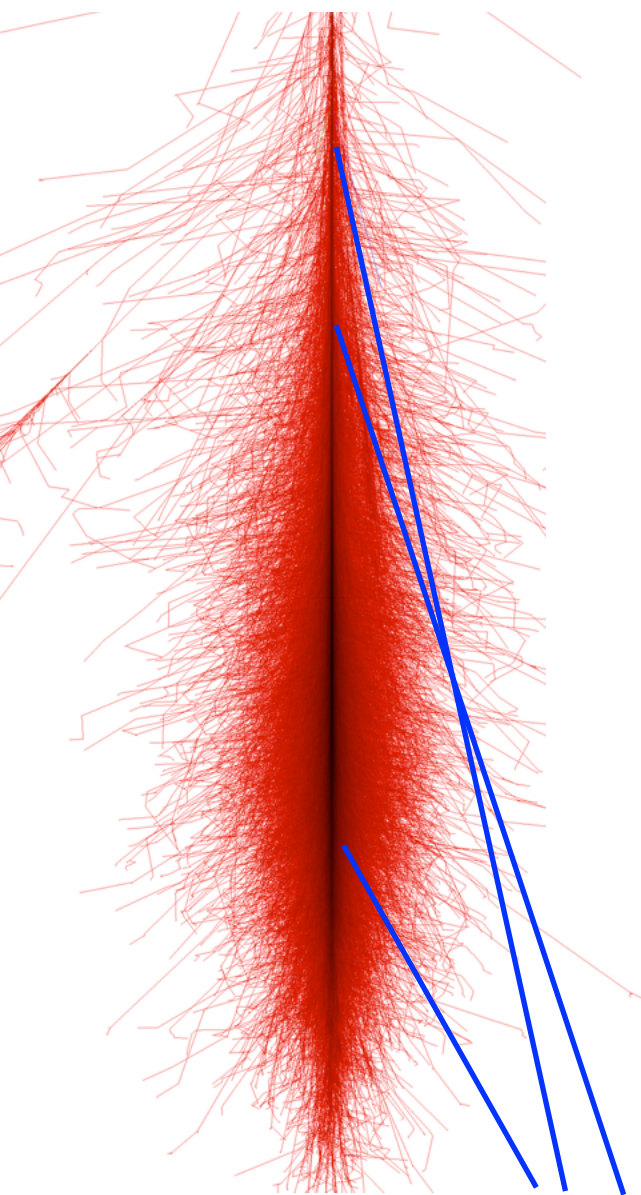
# CORSIKA

J.Knapp 2017



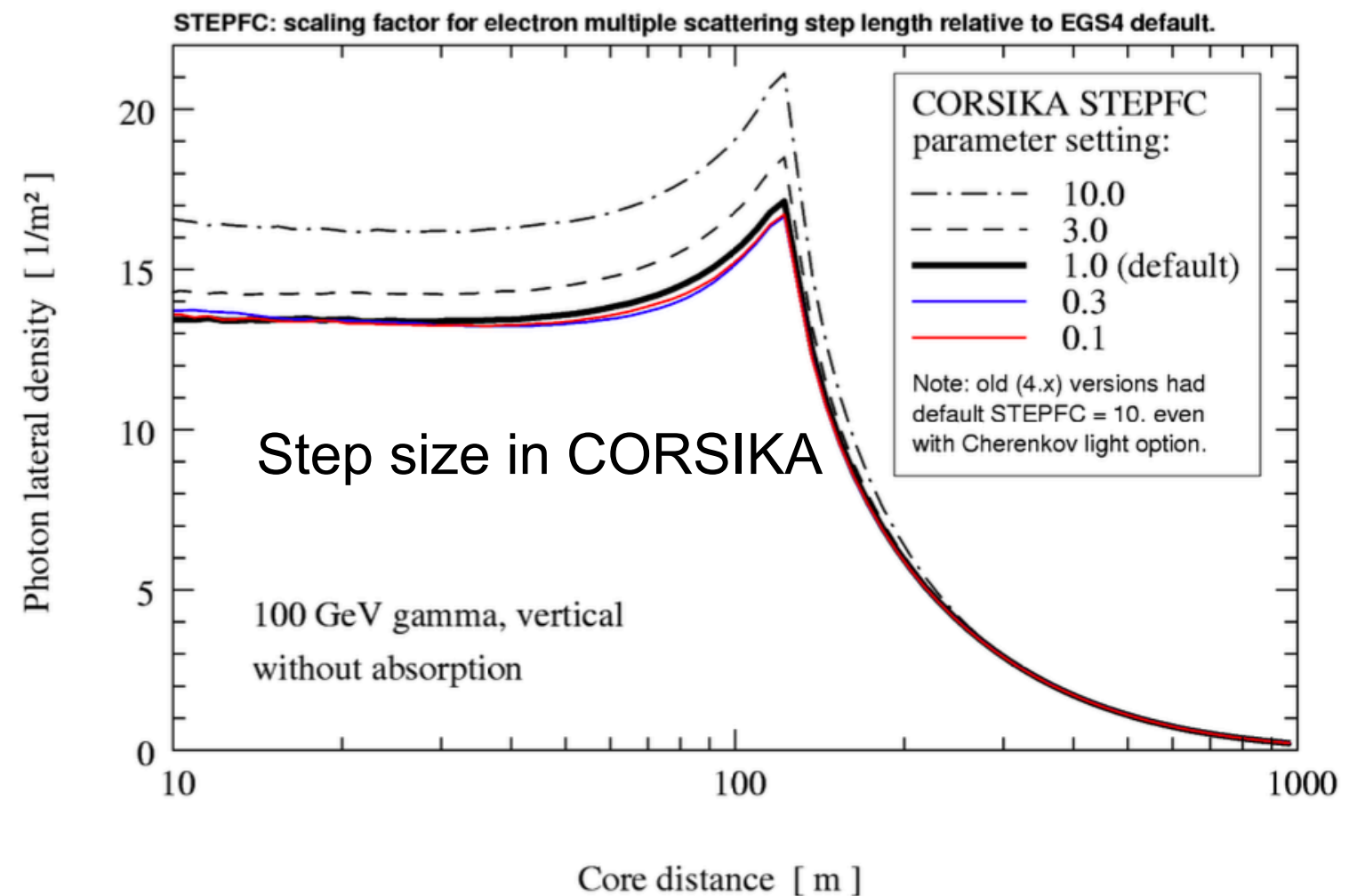
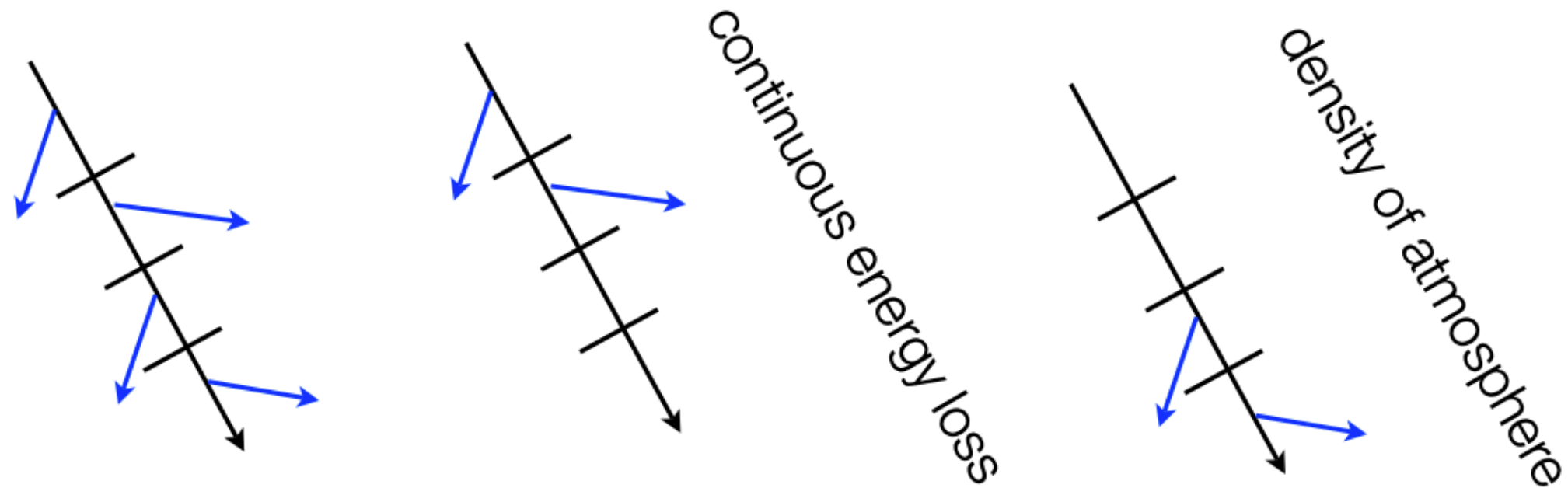
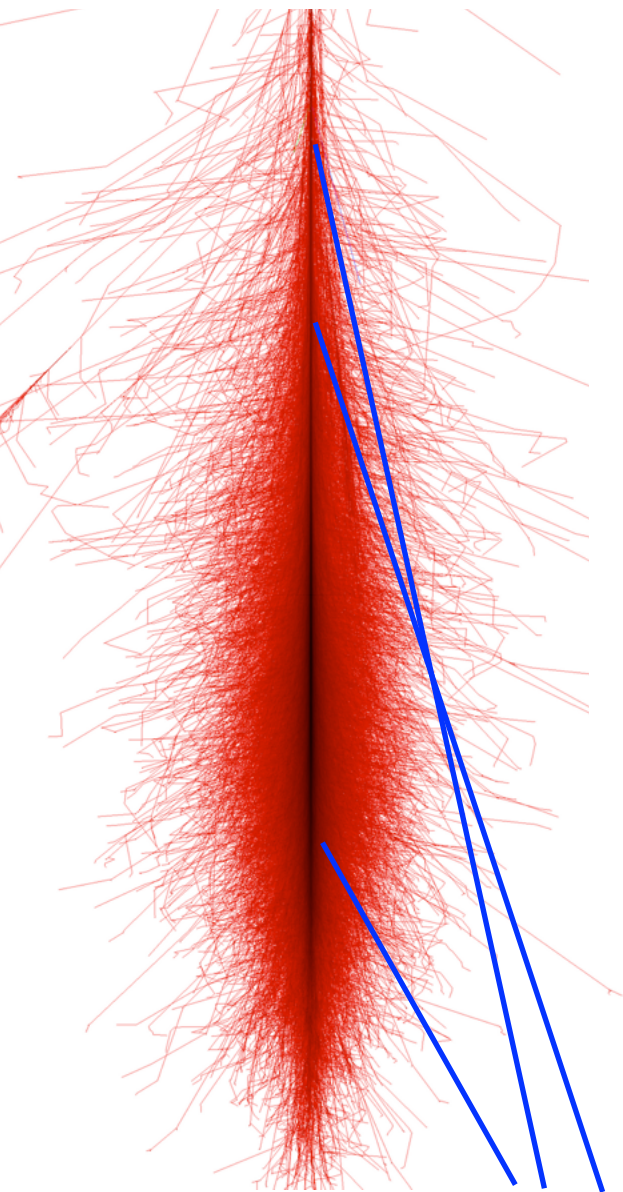
# Cherenkov emission in the simulations.

Large number of Cherenkov photons emitted.  
(100 TeV shower with typically 100 billion photons.)



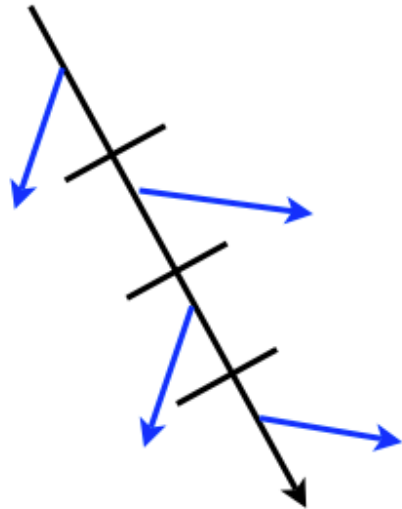
(ignoring generally wavelength dependence of refractive index)

# Cherenkov emission in the simulations.





# Bunches.



Not all emitted Cherenkov photons will lead to a detection.

Emit in **bunches**  
(non integer)

K.Bernlöhner

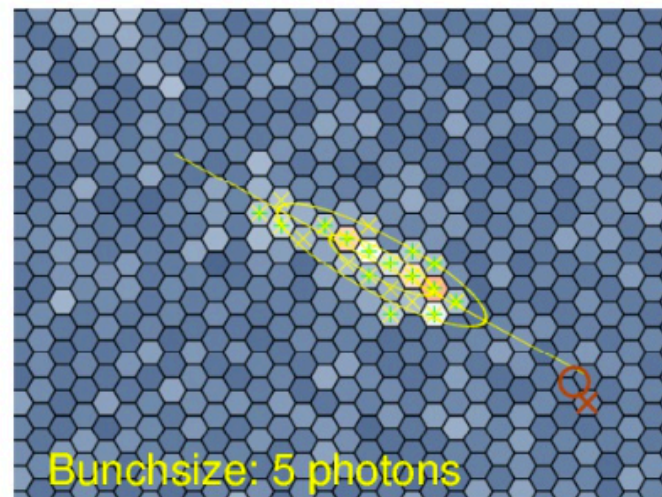
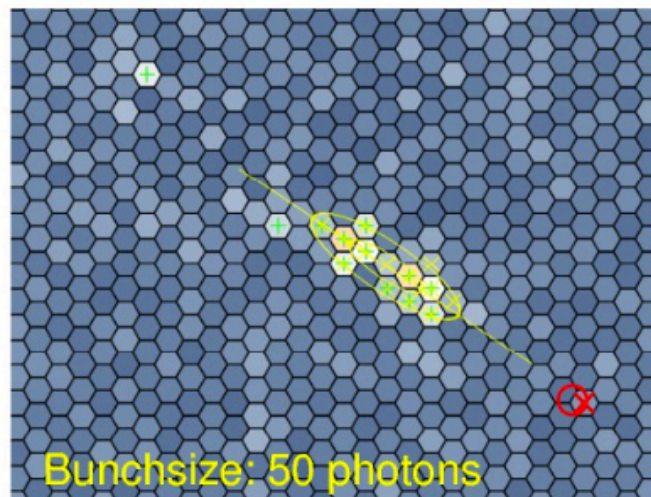
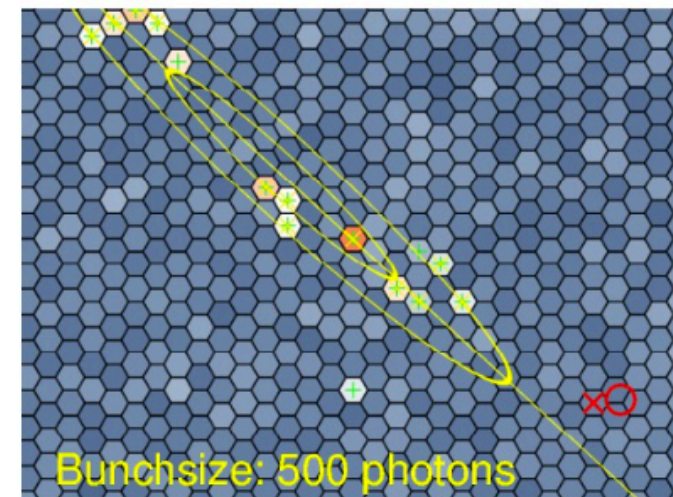


Image quality: good



poor

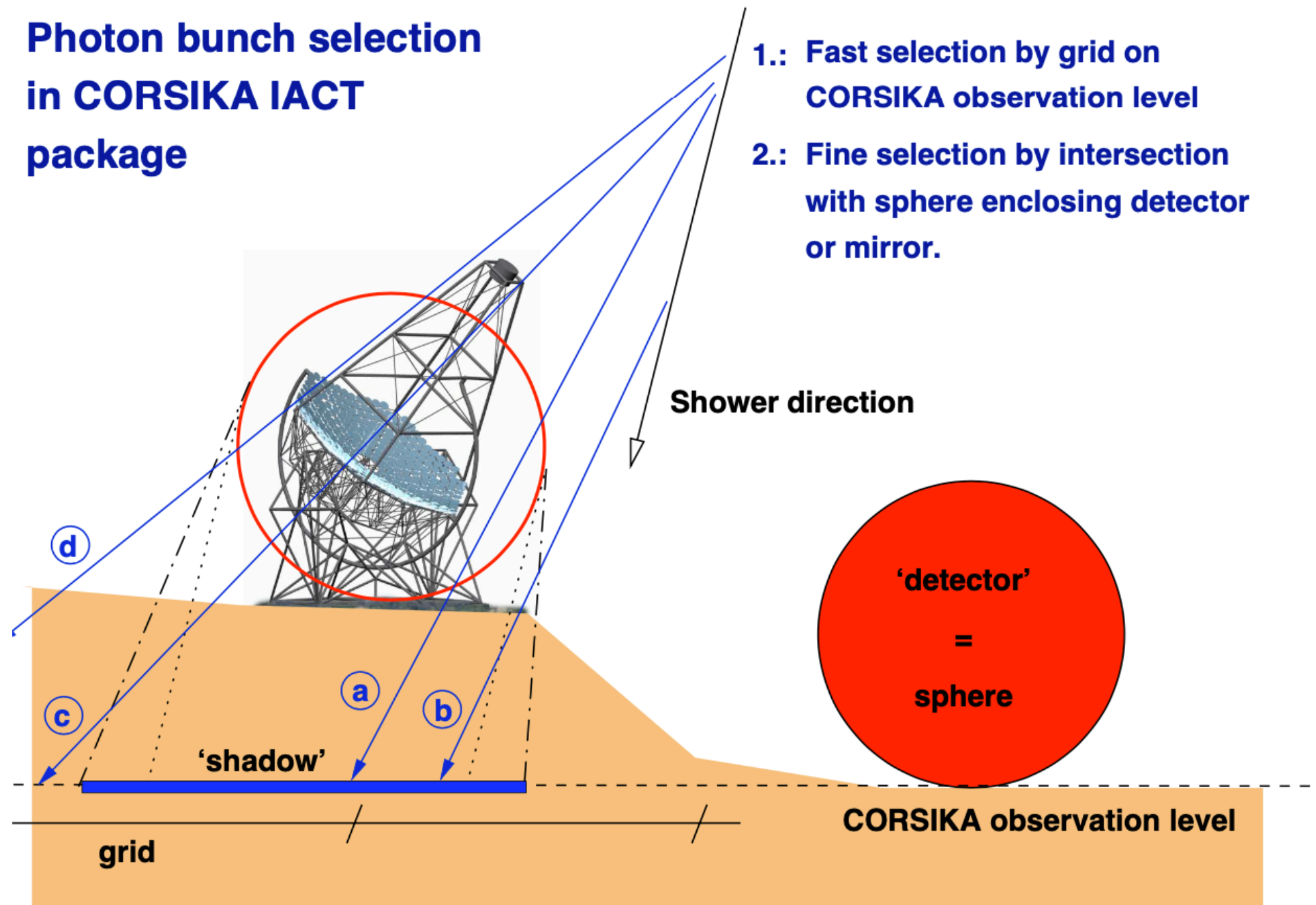


unusable



# Detector level.

## Photon bunch selection in CORSIKA IACT package



**TELESCOPE X Y Z R**

...

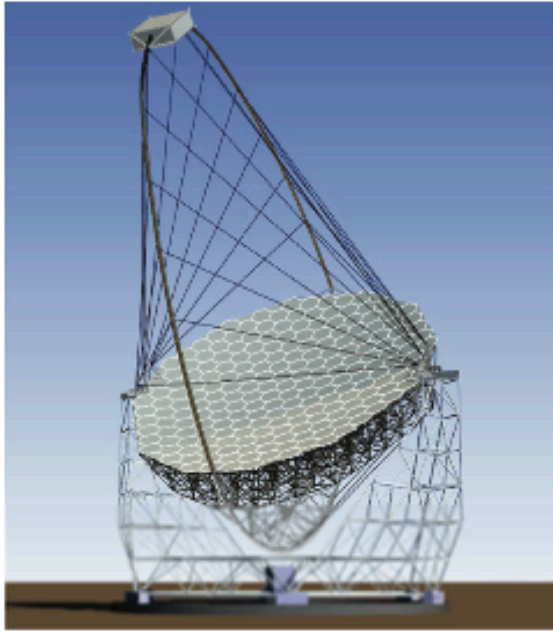
# Telescopes.



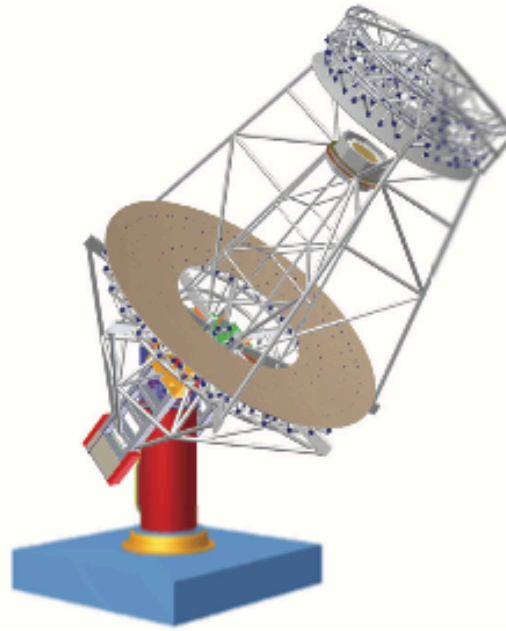
# Telescope Optics.

- imaging quality - optical point-spread function
- (non)isochronism
- costs

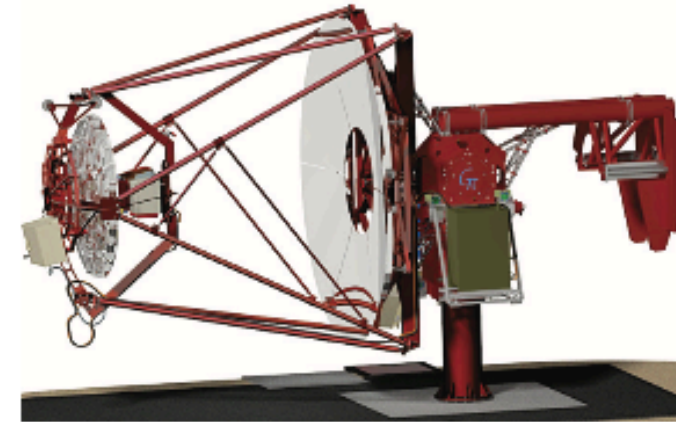
a



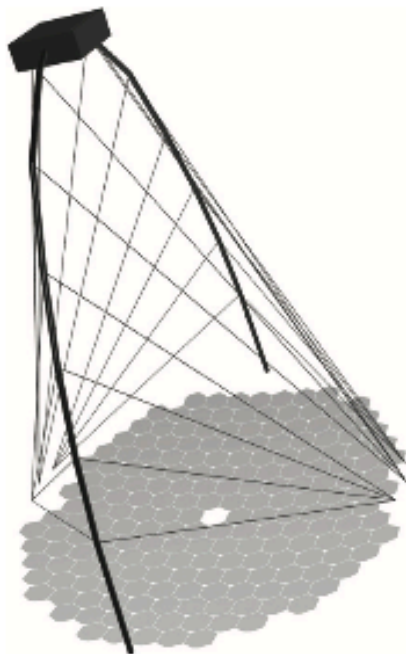
b



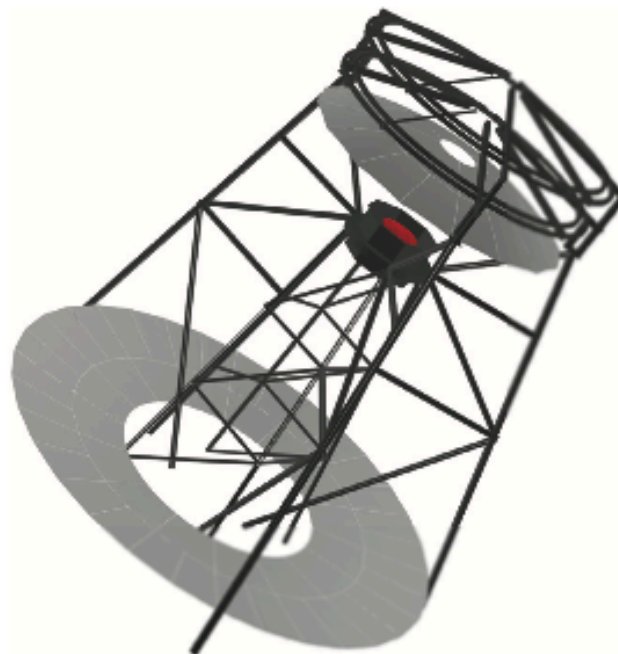
c Okumura+ (2016)



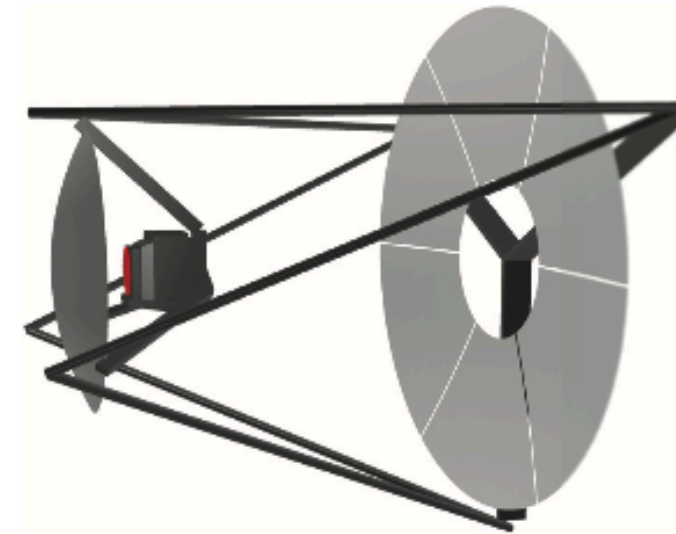
d



e



f



g

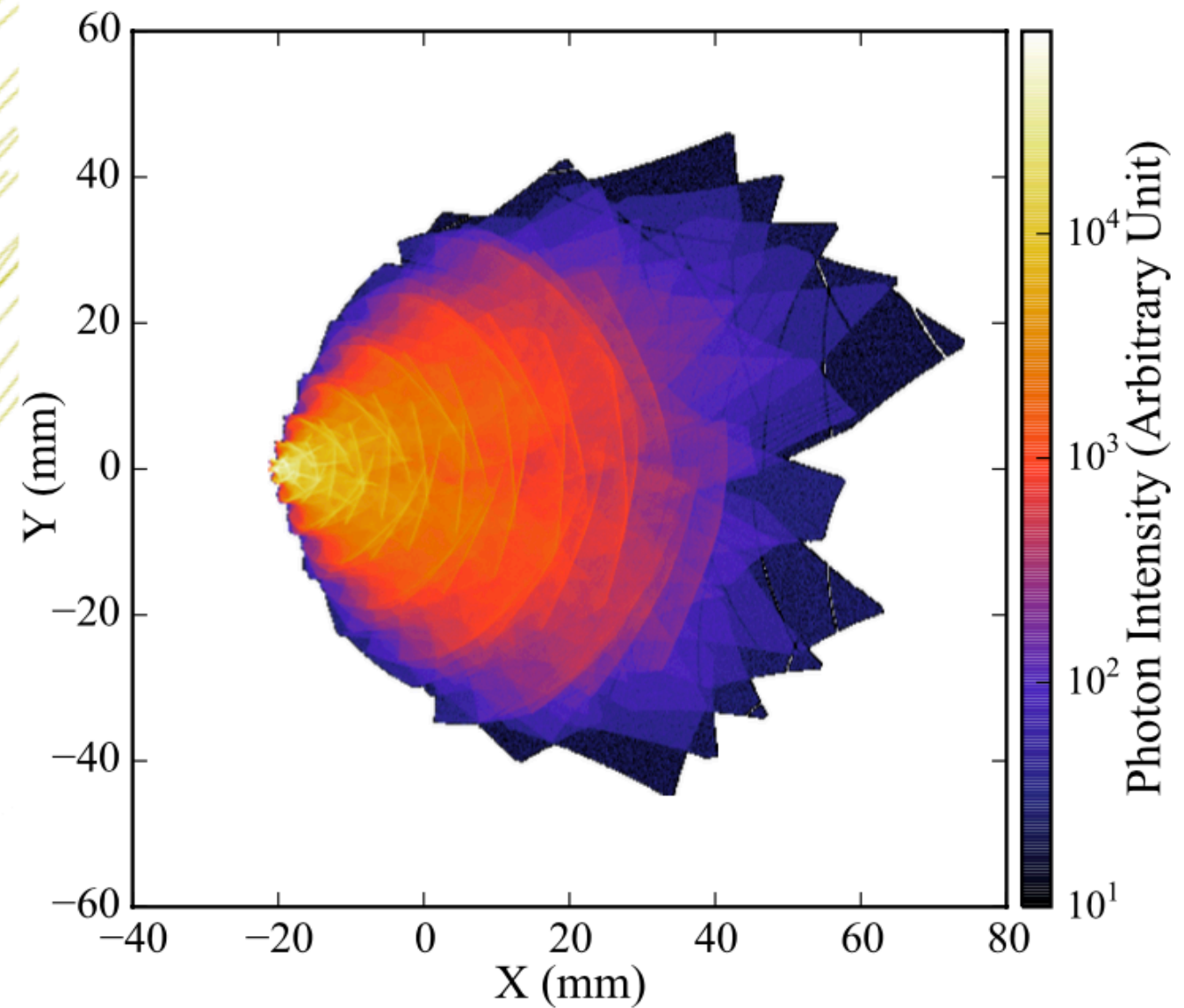
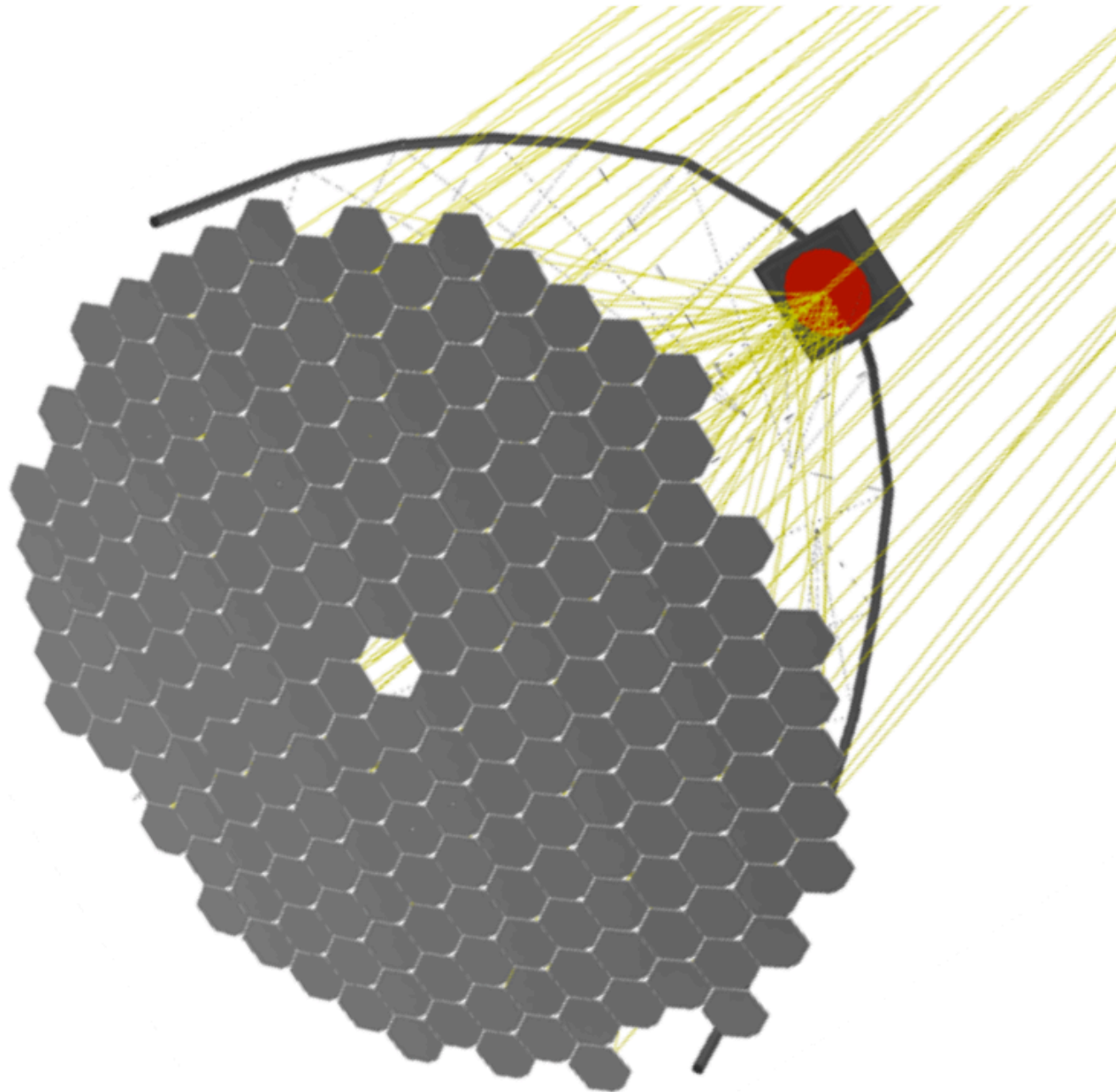
h

i



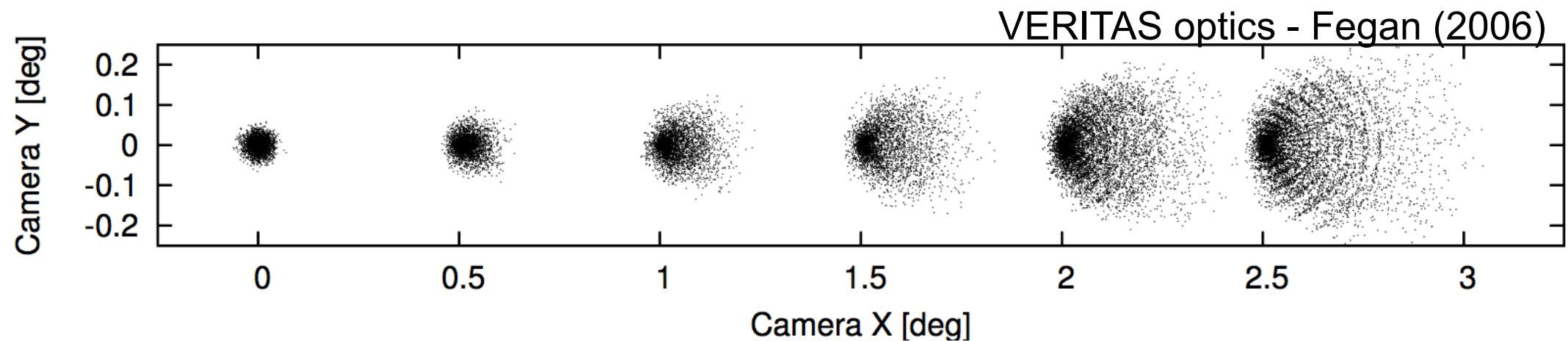
# Ray tracing and optical PSF.

By Koji Noda

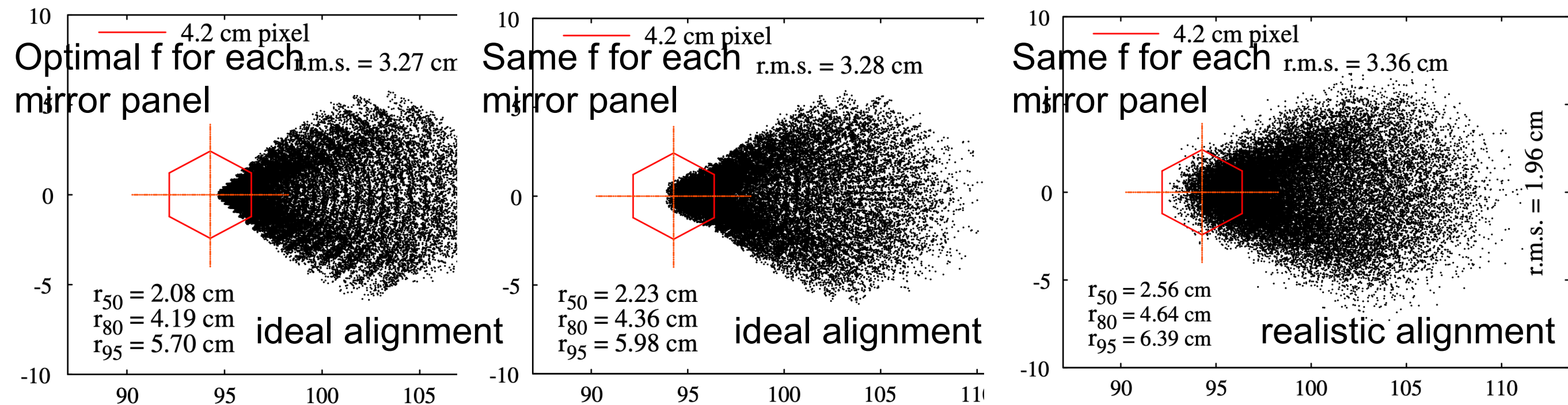




# Optical point-spread function.

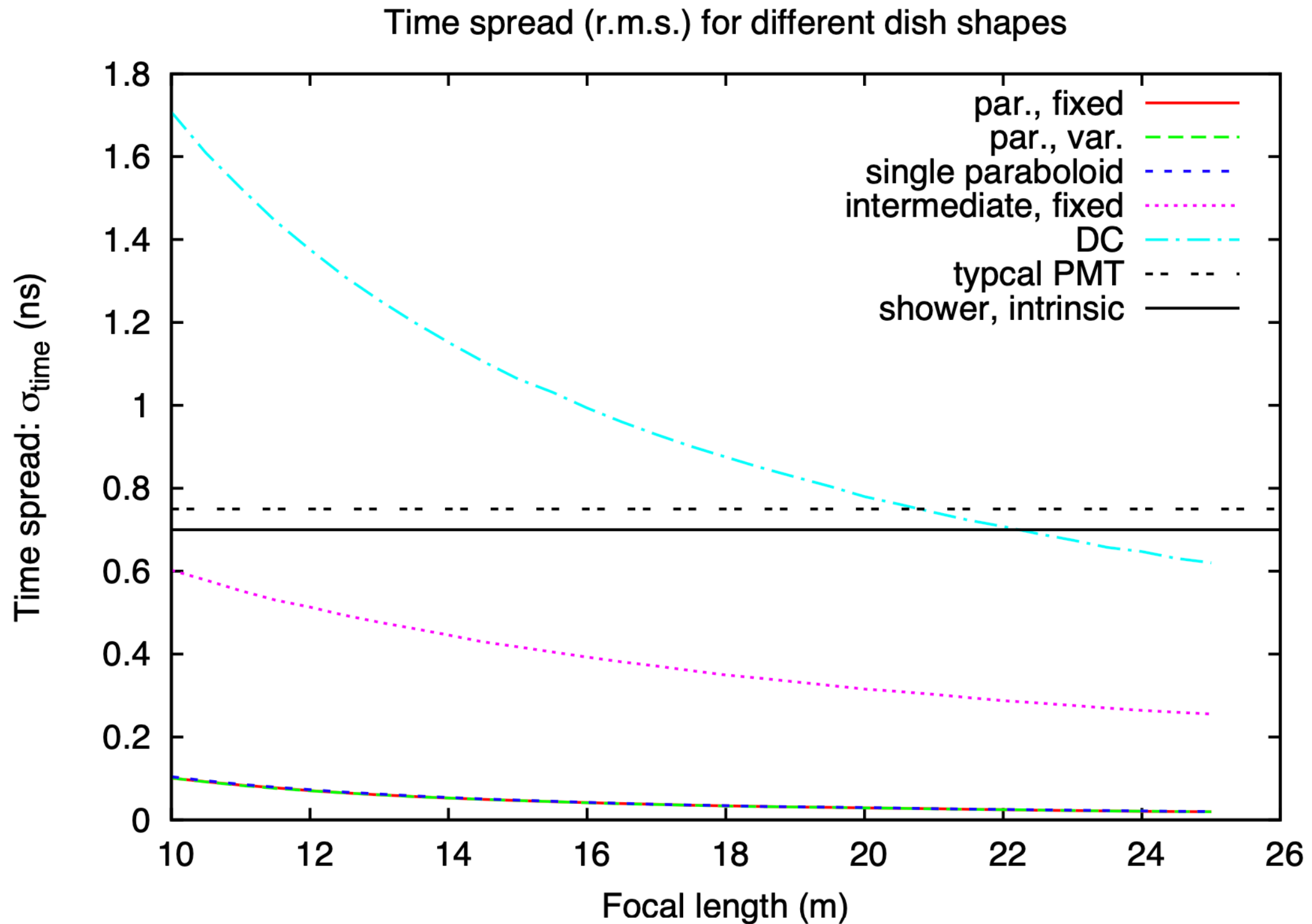


HESS 2 (K. Bernlöhr 2006)



# Time spread - mirror design

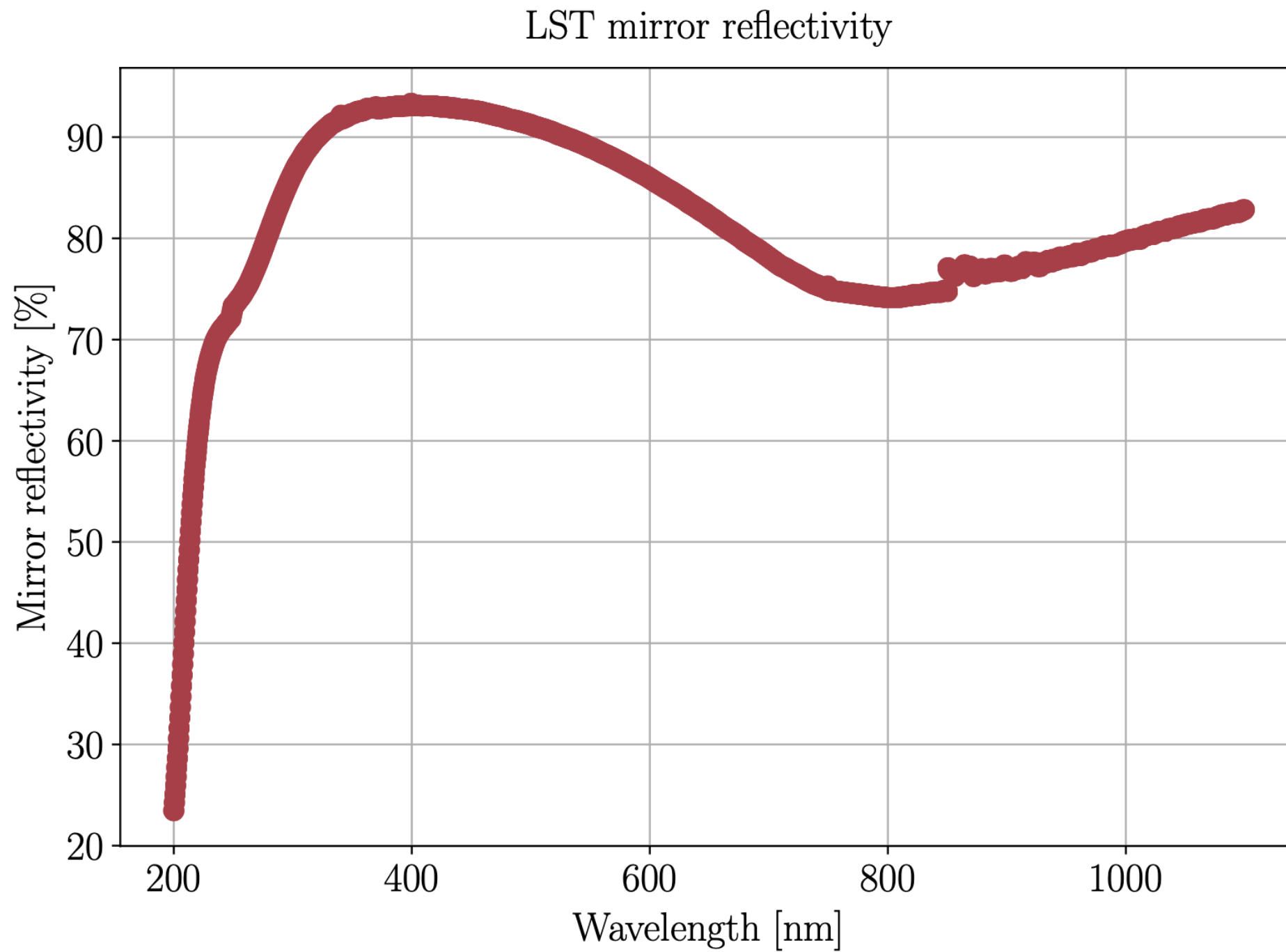
K.Bernlöhner  
(internal note 2009)



# Parabolic vs Davis Cotton vs Intermediate design

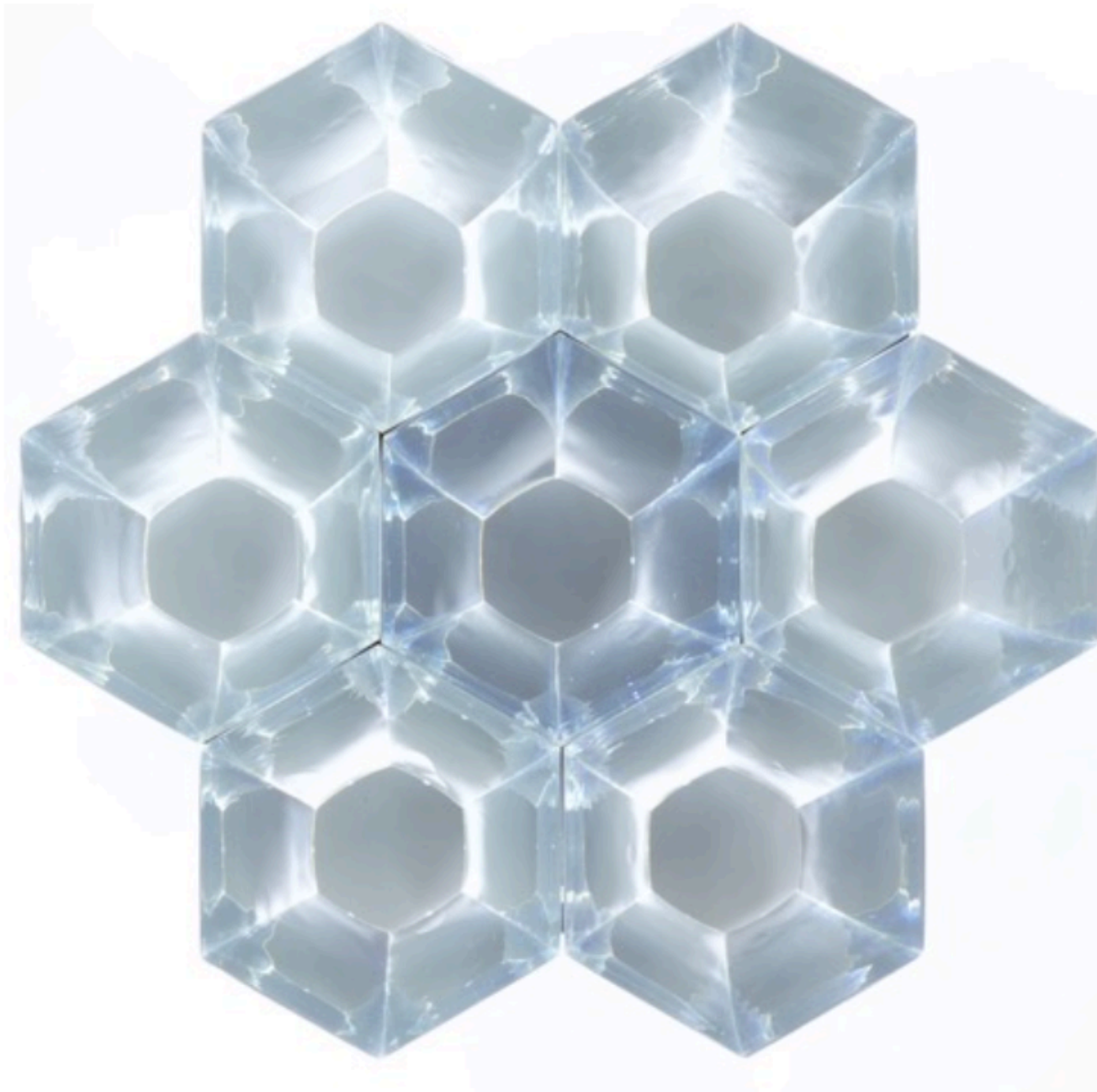
- optical point-spread function:
  - Davis-Cotton with smaller radial PSF than parabolic (especially with increased off-axis angles)
  - transverse direction PSF very similar
- timing
  - parabolic mirror essentially isochronous
  - 12-m Davis Cotton: top-hat time distribution of 3.6 ns (1.05 ns rms)
- CTA MSTs are following an intermediate design using a dish between Davis-Cotton and parabolic
  - almost DC-like PSF with a time spread of 0.41 ns rms

# Mirror reflectivity.

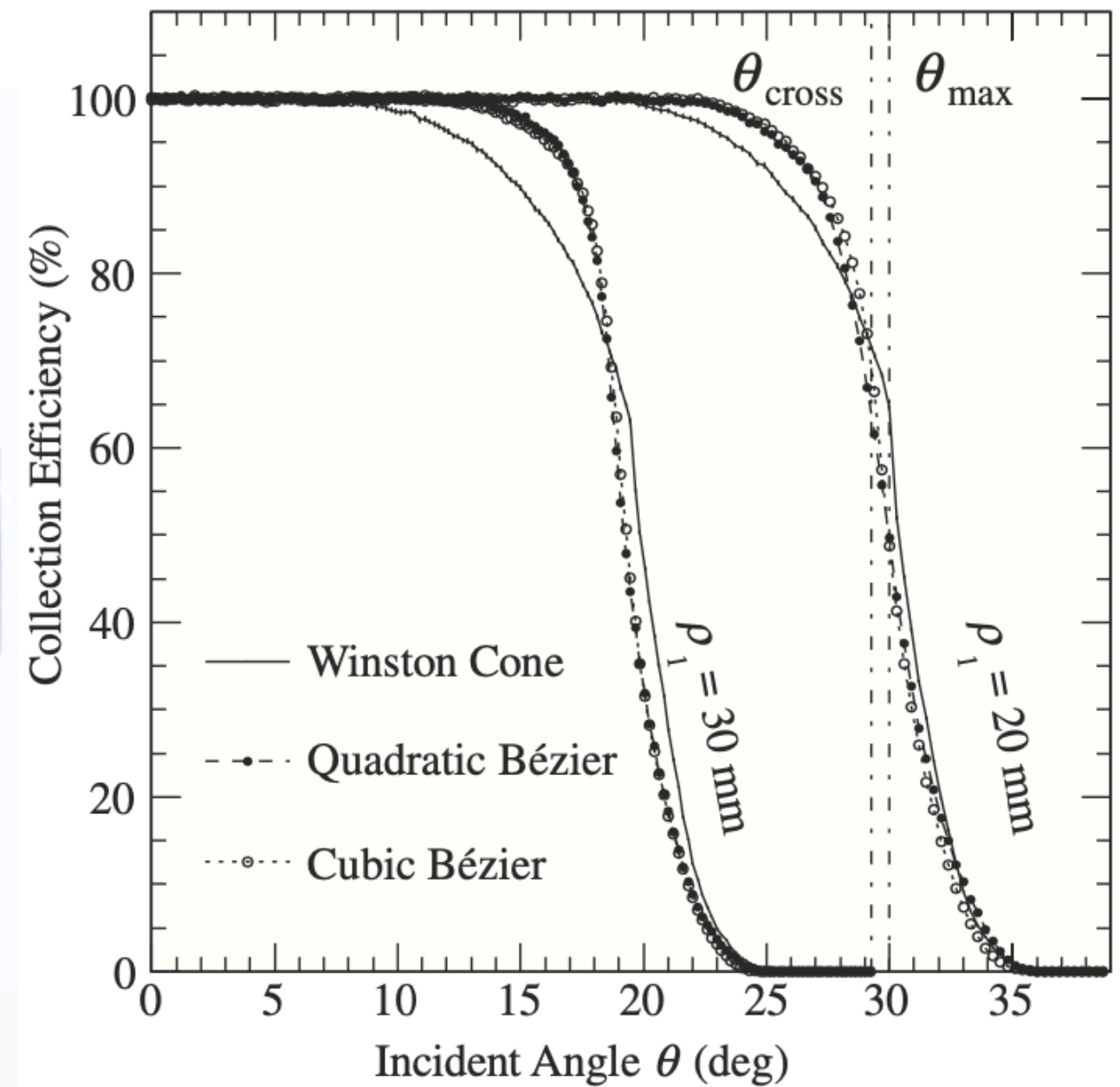




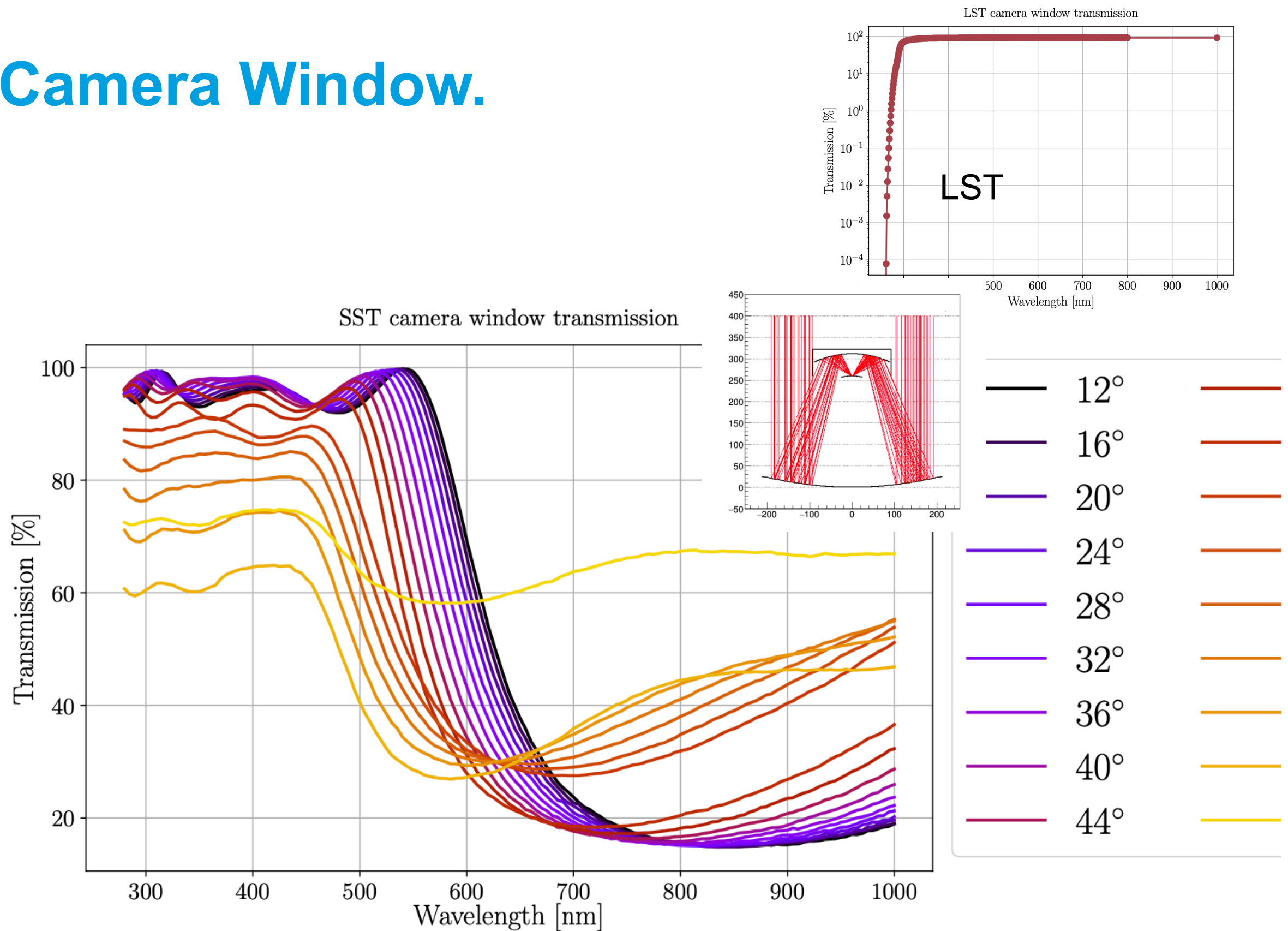
# Light concentrators.



Okumura (2012)



# Camera Window.

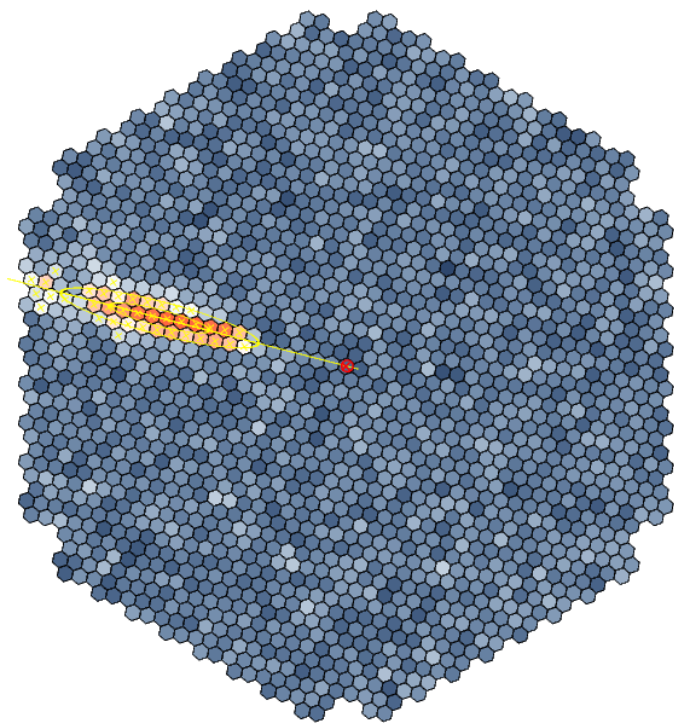


**Figure 5** – Camera window transmission as a function of wavelength and incident angle for the SST camera.

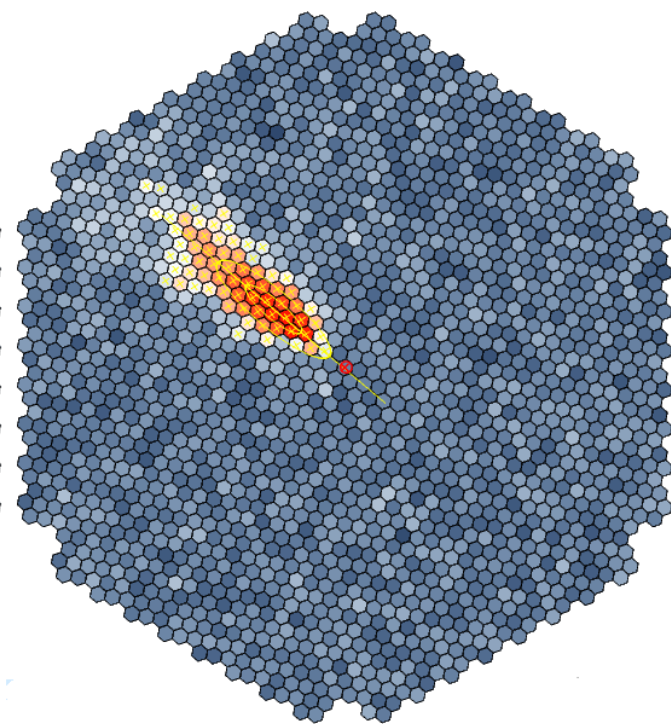


# Cameras.

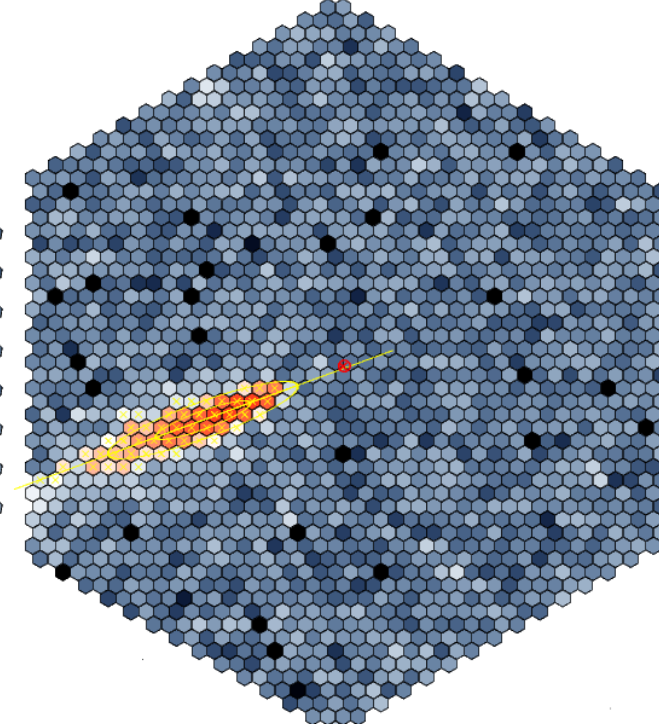
K.Bernlöhr



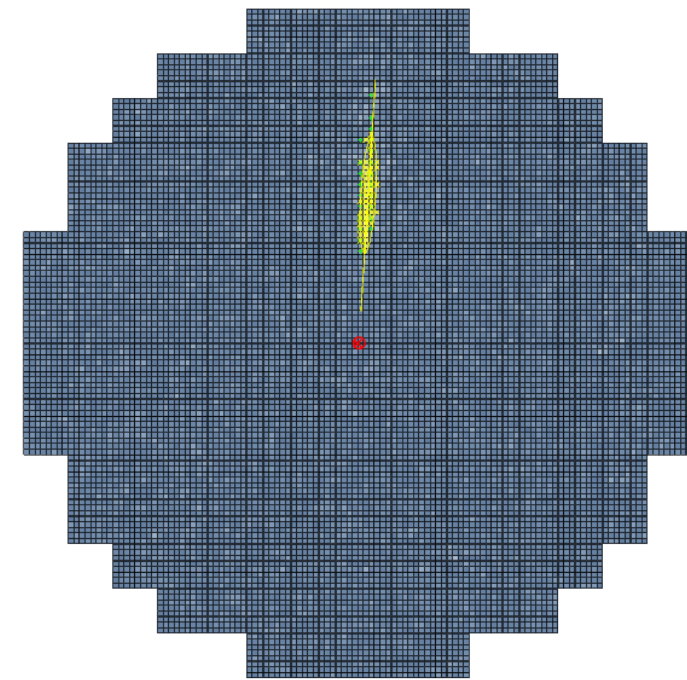
LST



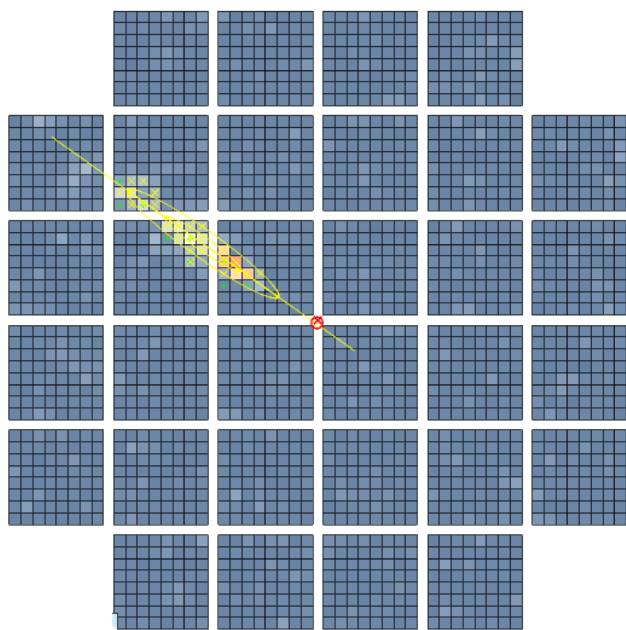
NectarCam



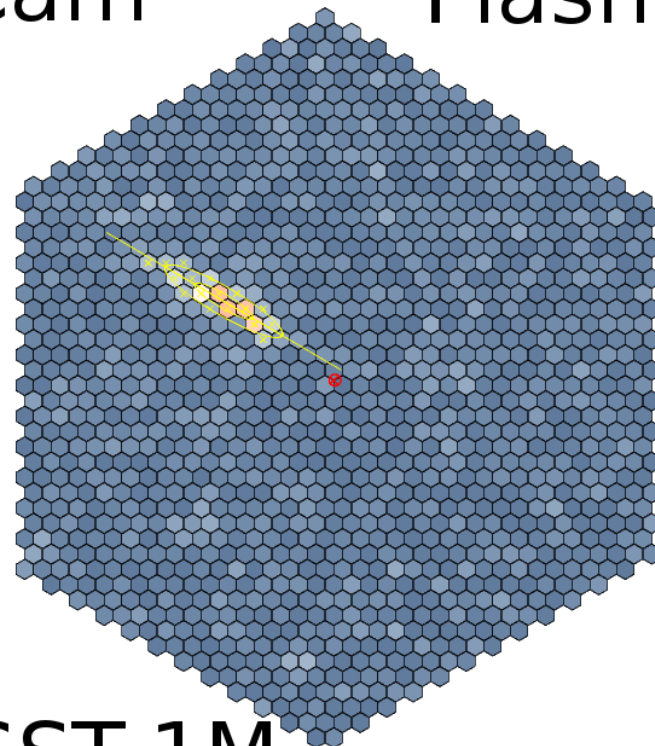
FlashCam



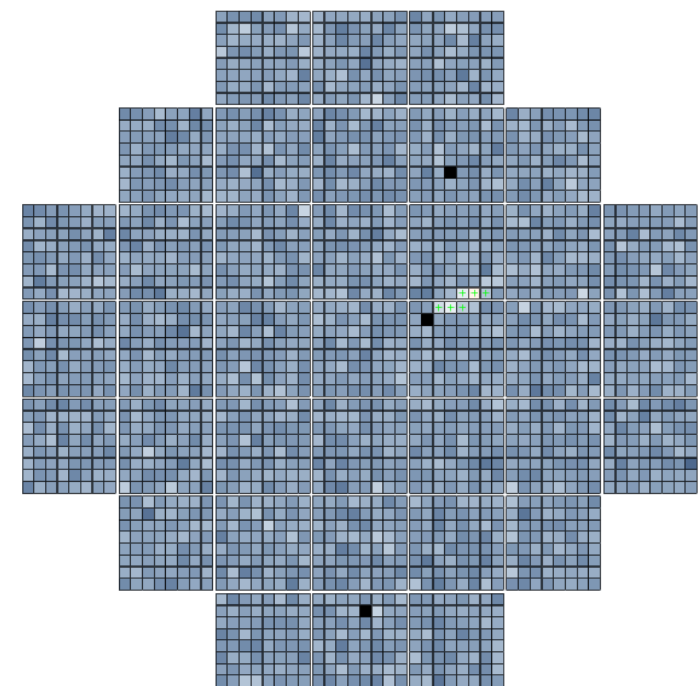
SCT



CHEC



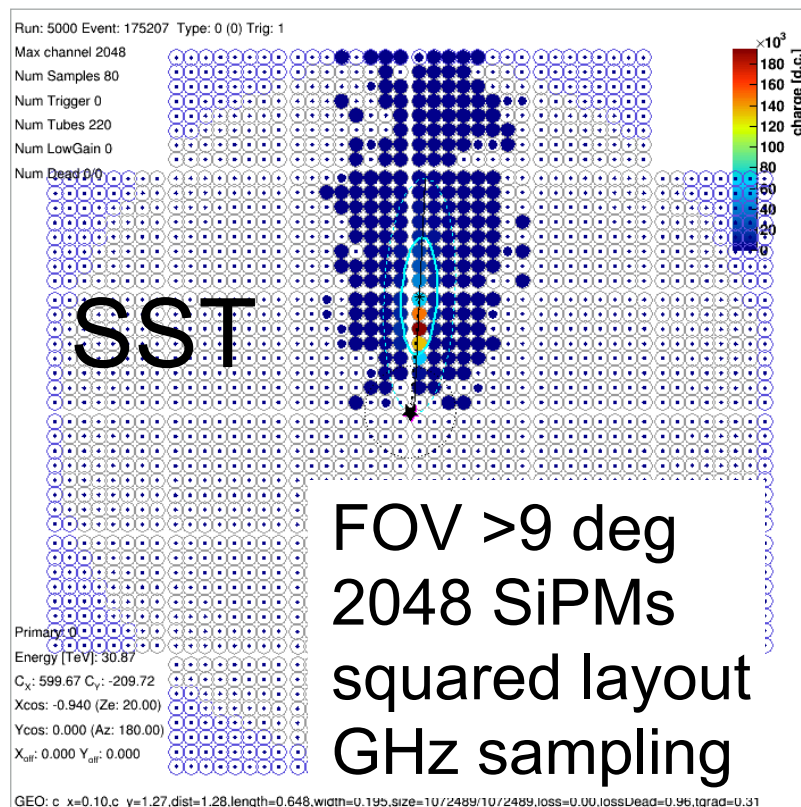
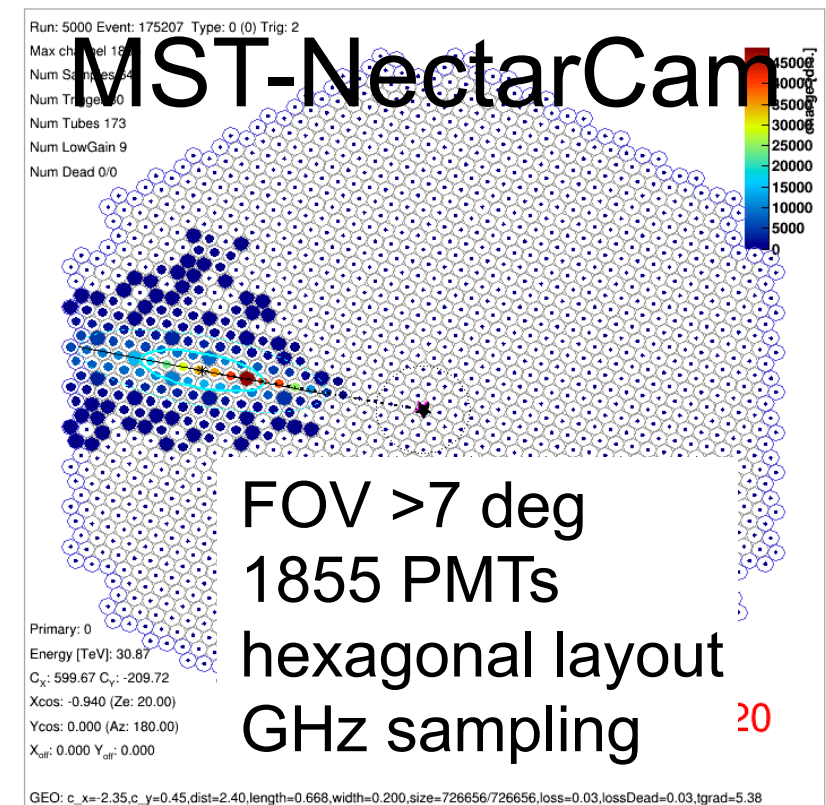
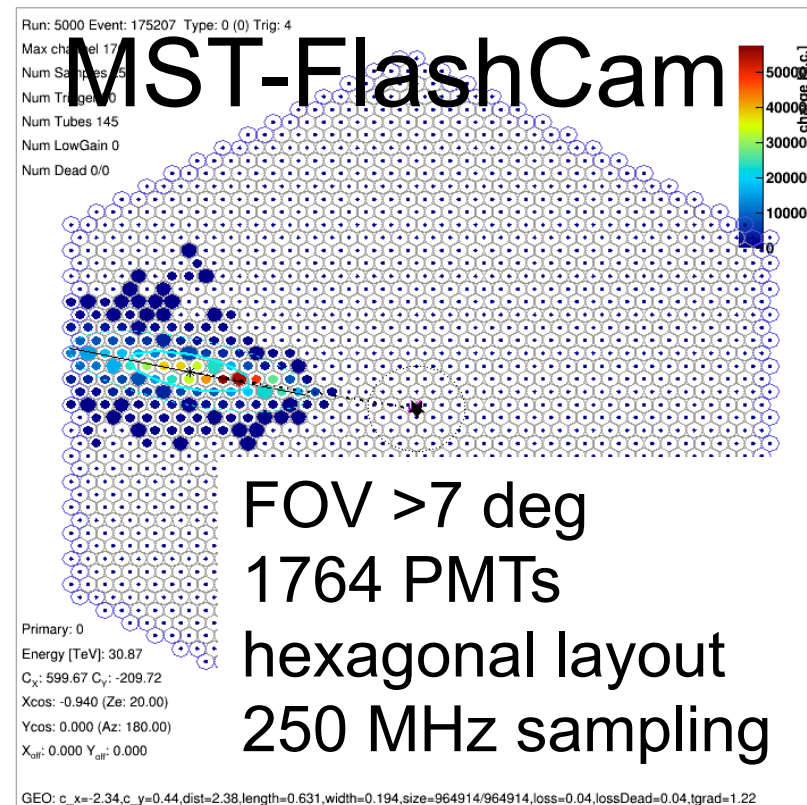
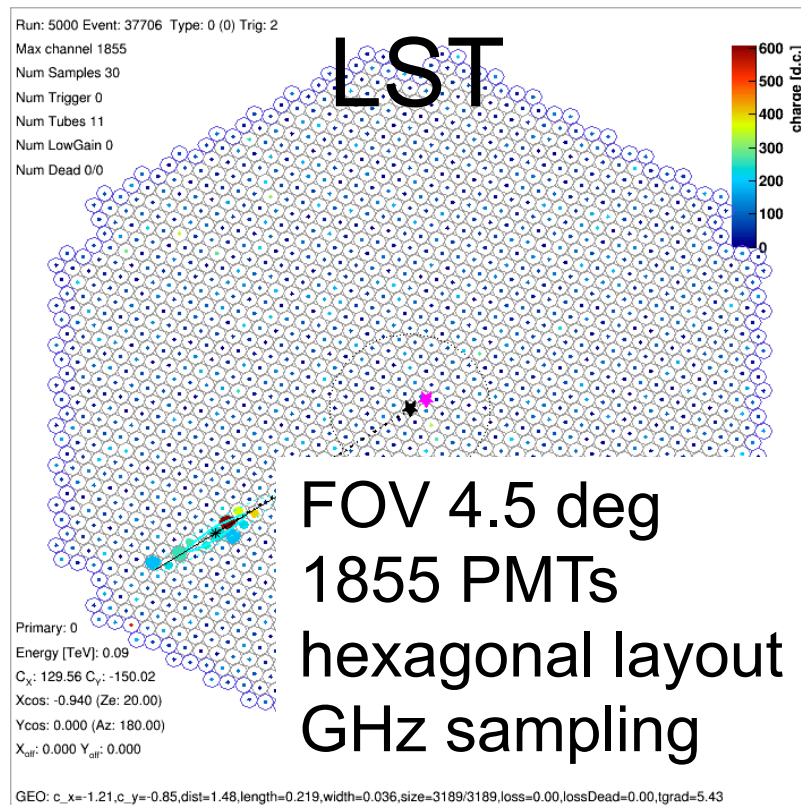
SST-1M



ASTRI



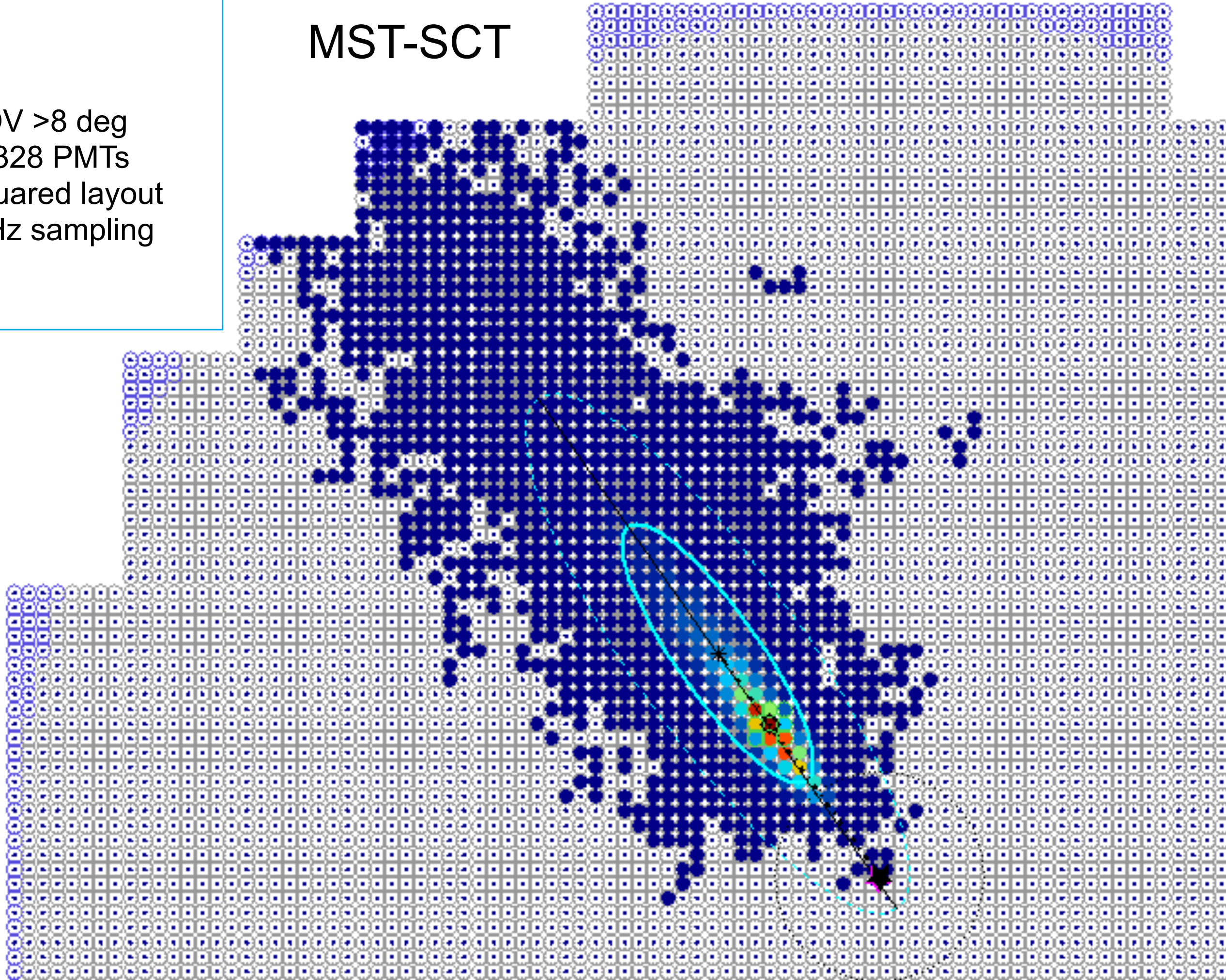
# Telescopes and Camera types



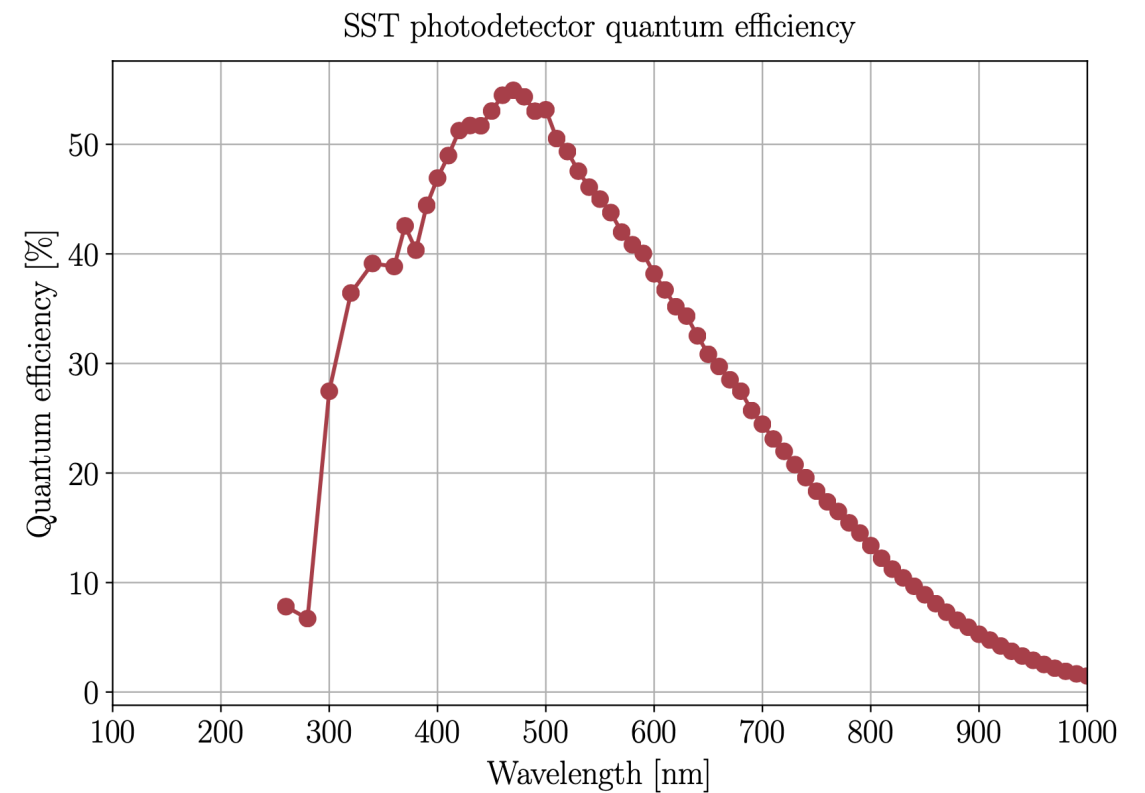
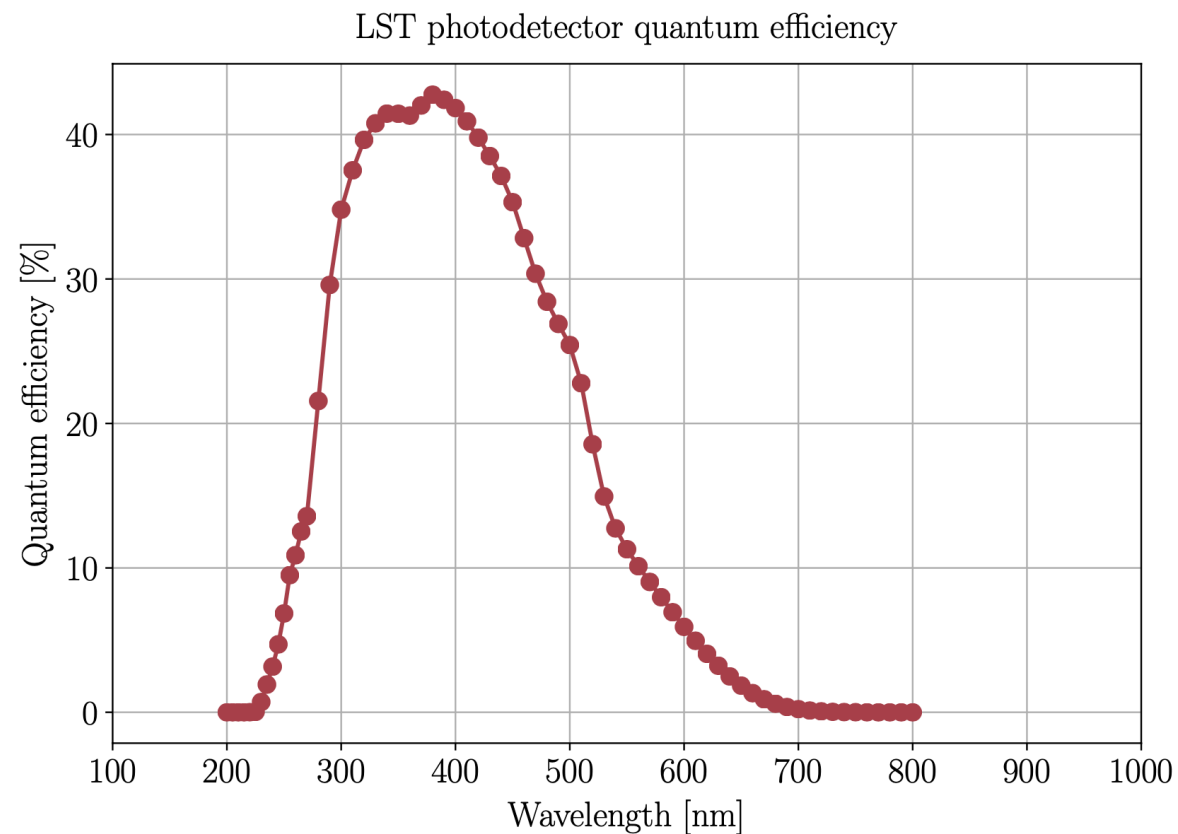


# MST-SCT

FOV >8 deg  
11328 PMTs  
squared layout  
GHz sampling

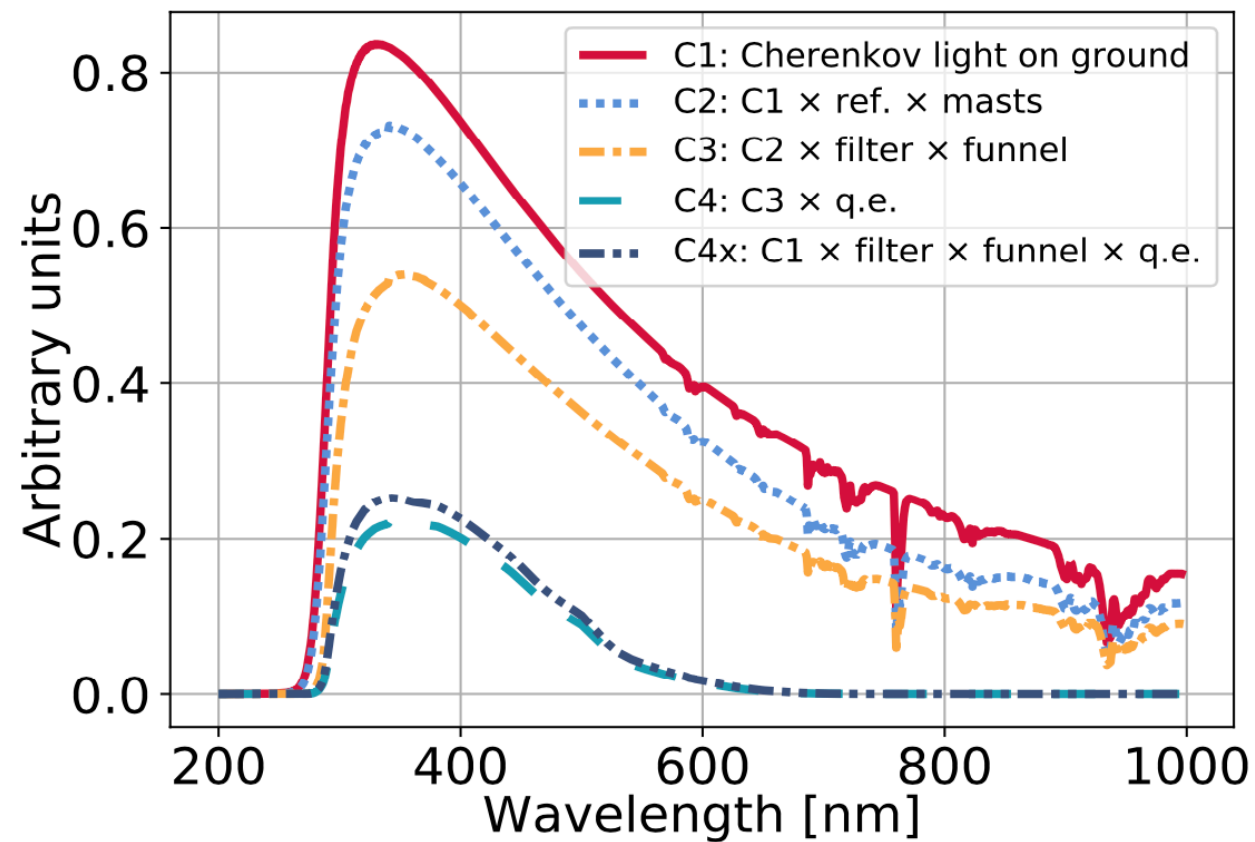


# Quantum and photodetector efficiencies.

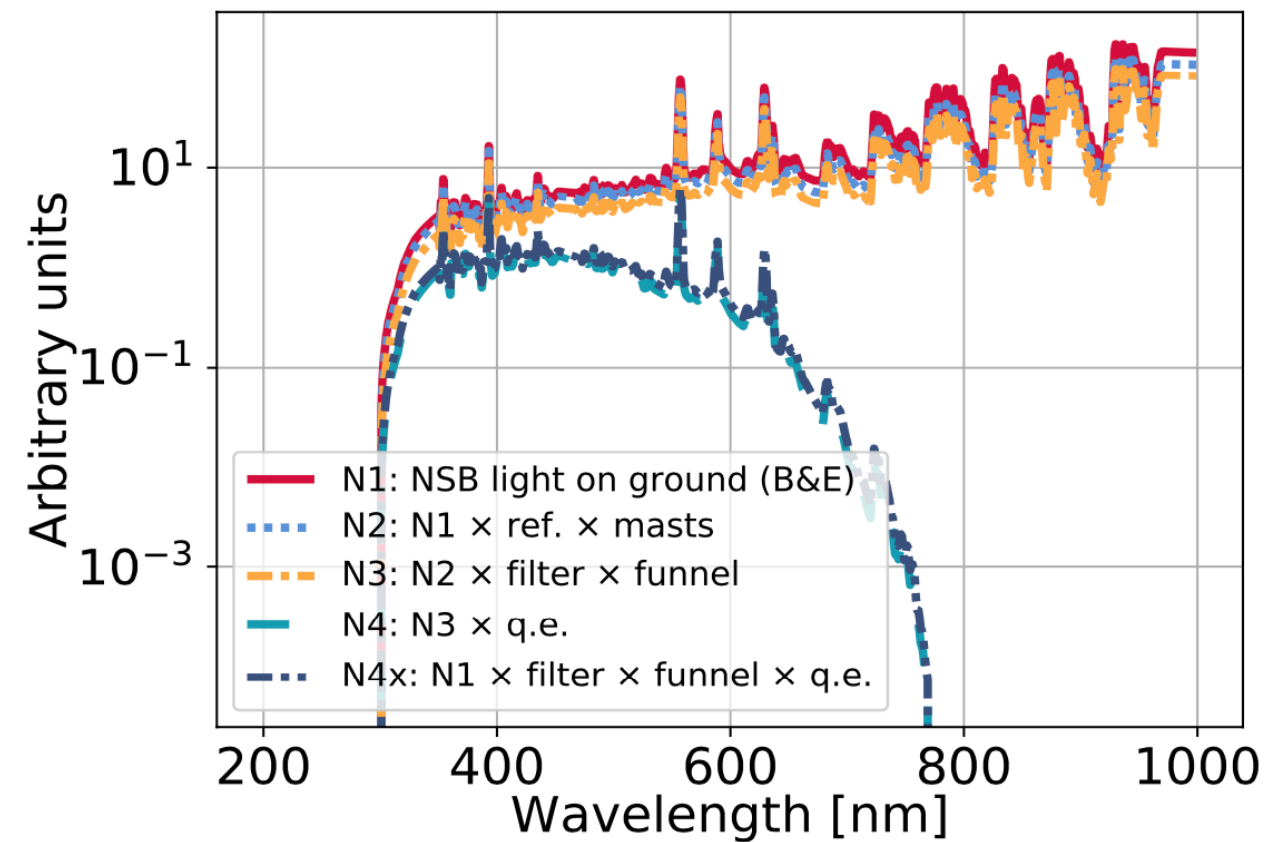


# Efficiencies.

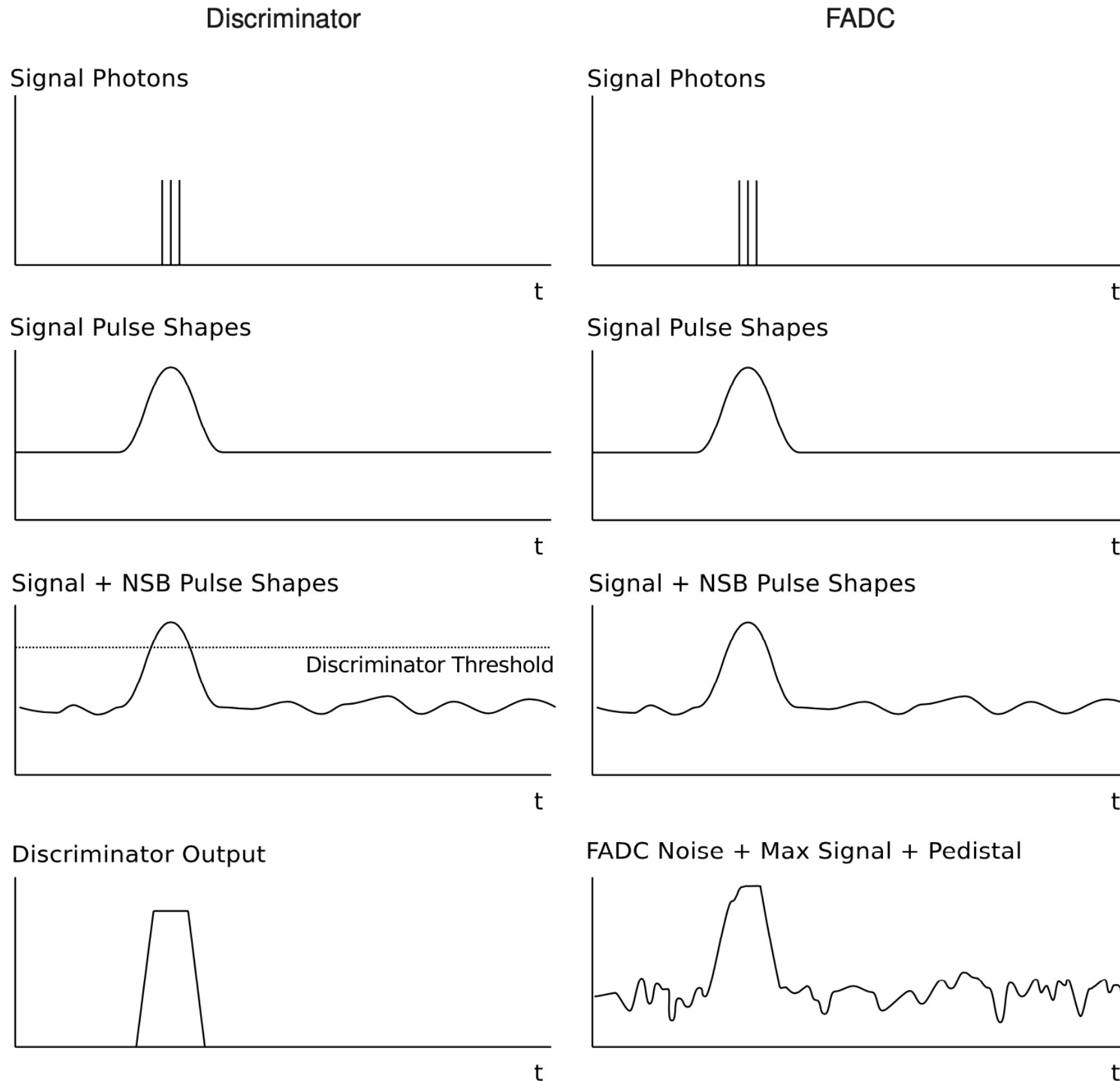
LST-prototype response to Cherenkov



LST-prototype response to NSB

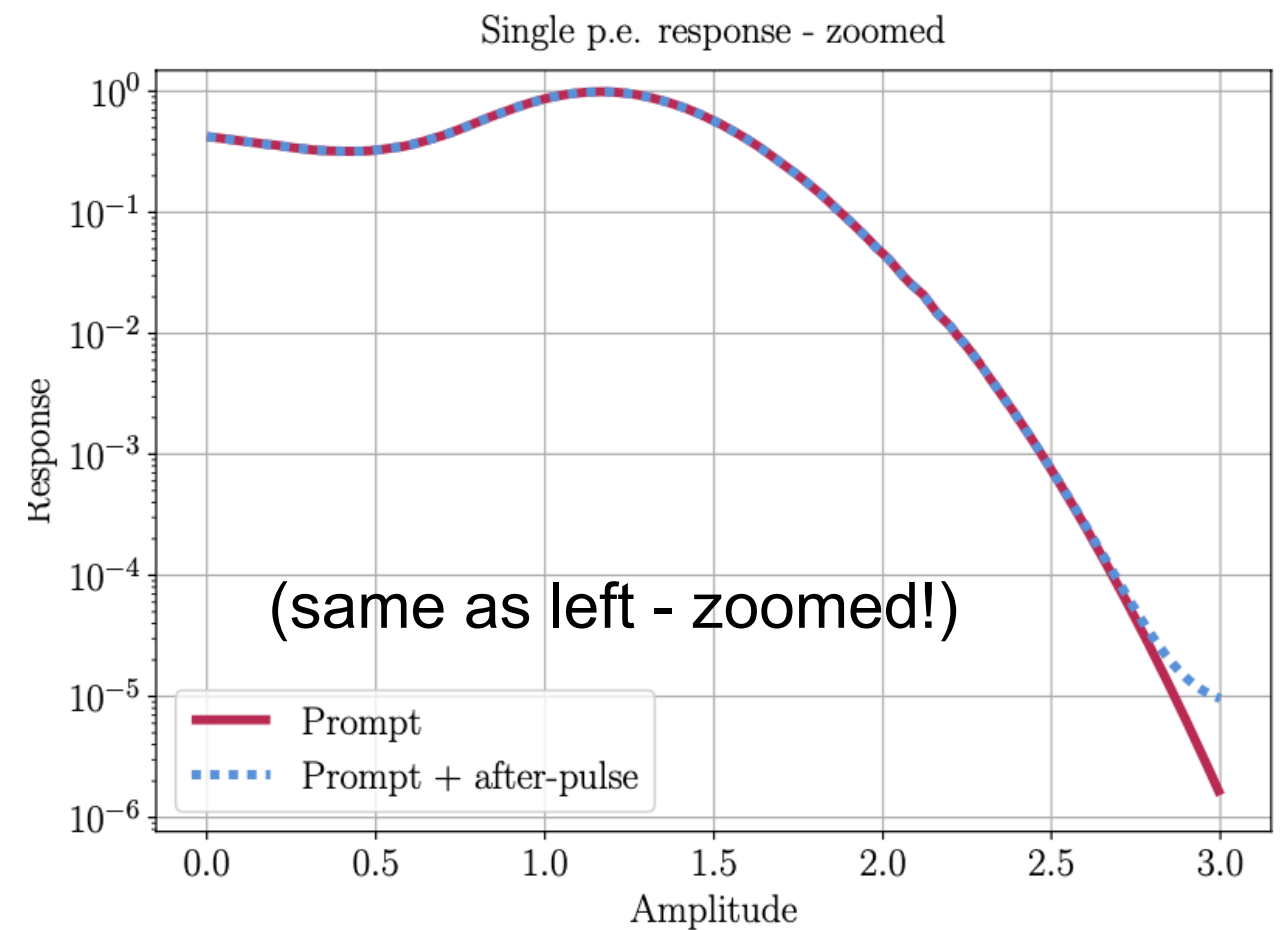
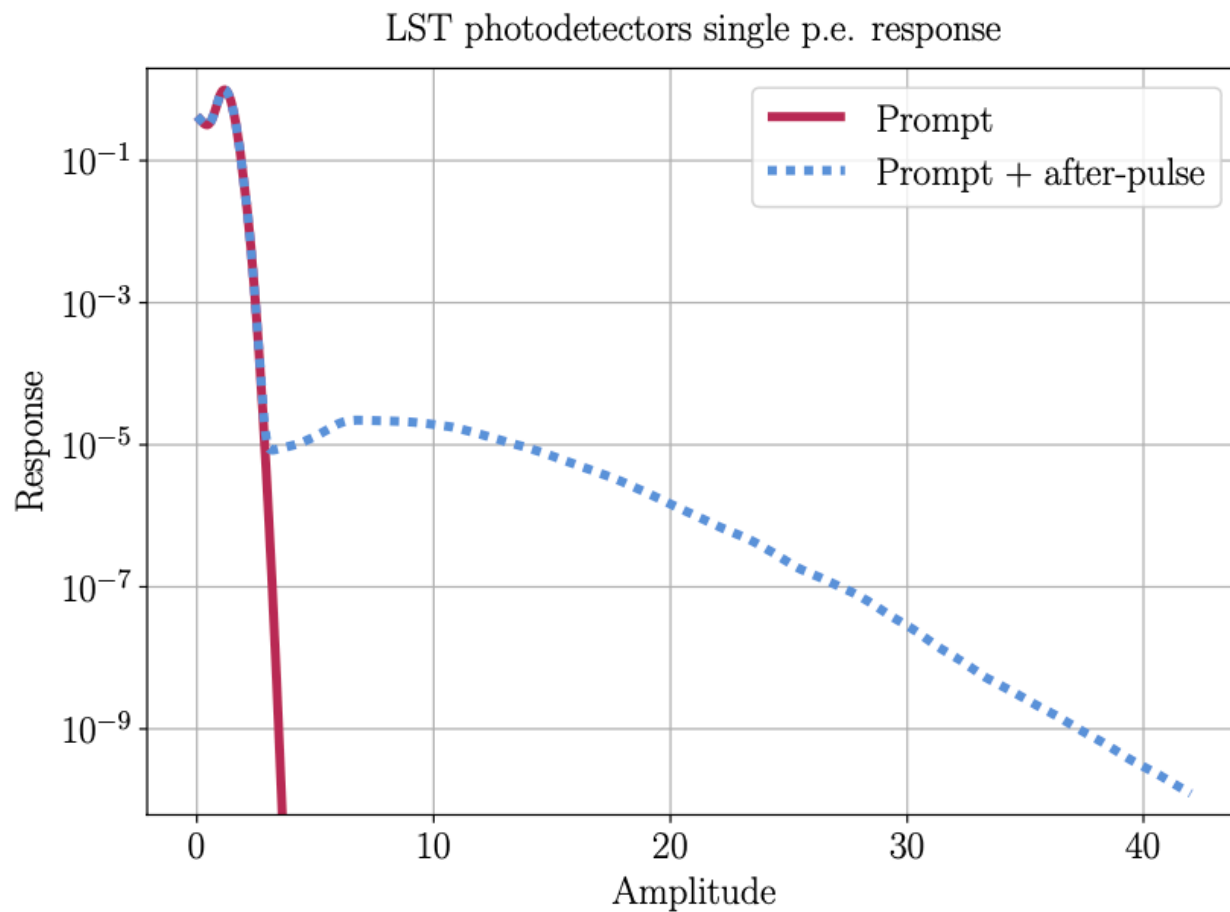


# Trigger and readout - oversimplified.

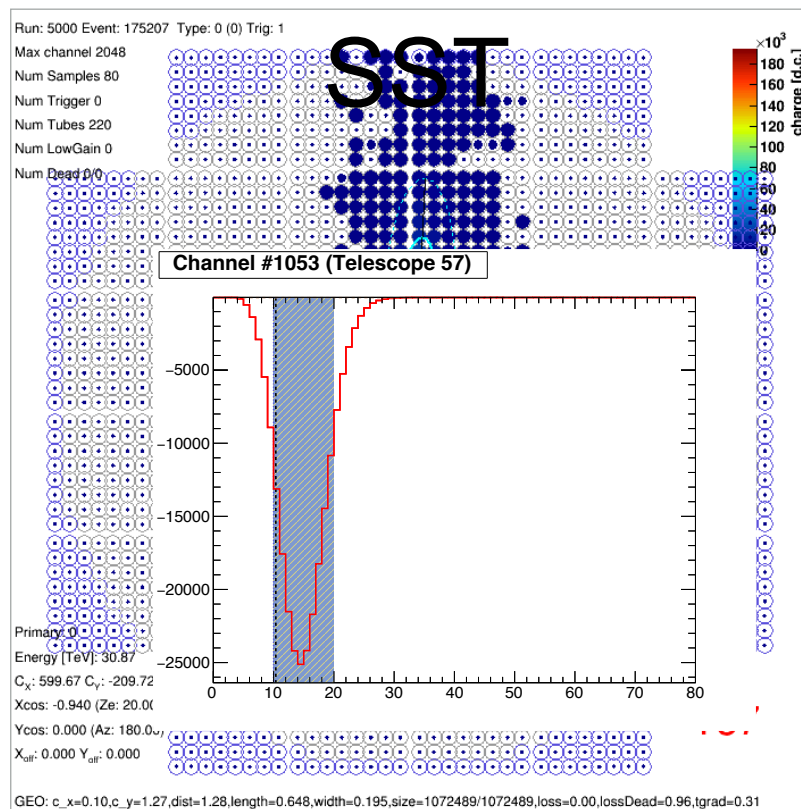
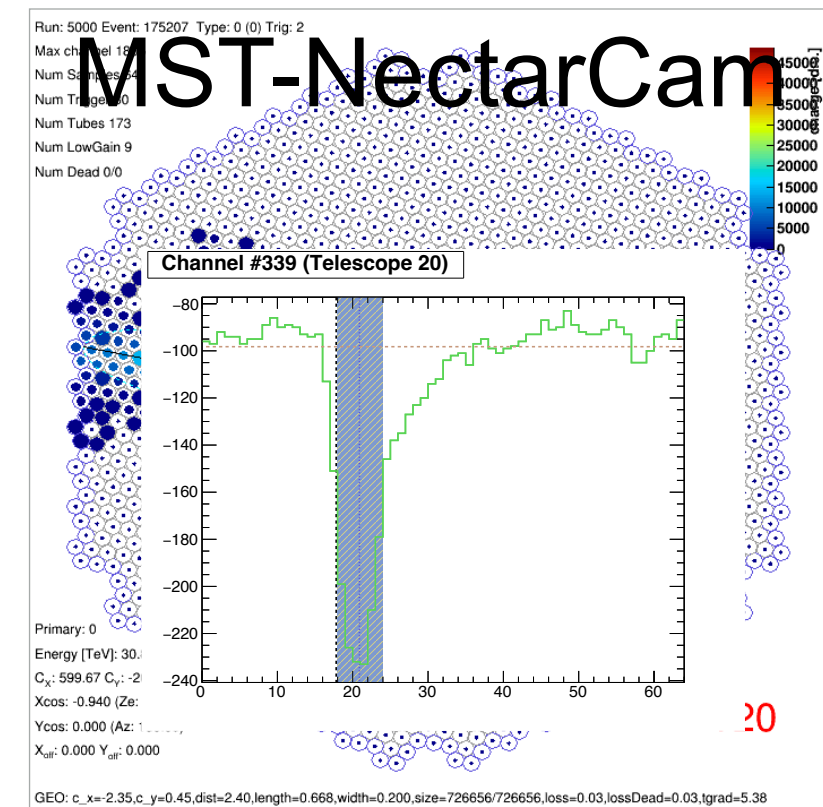
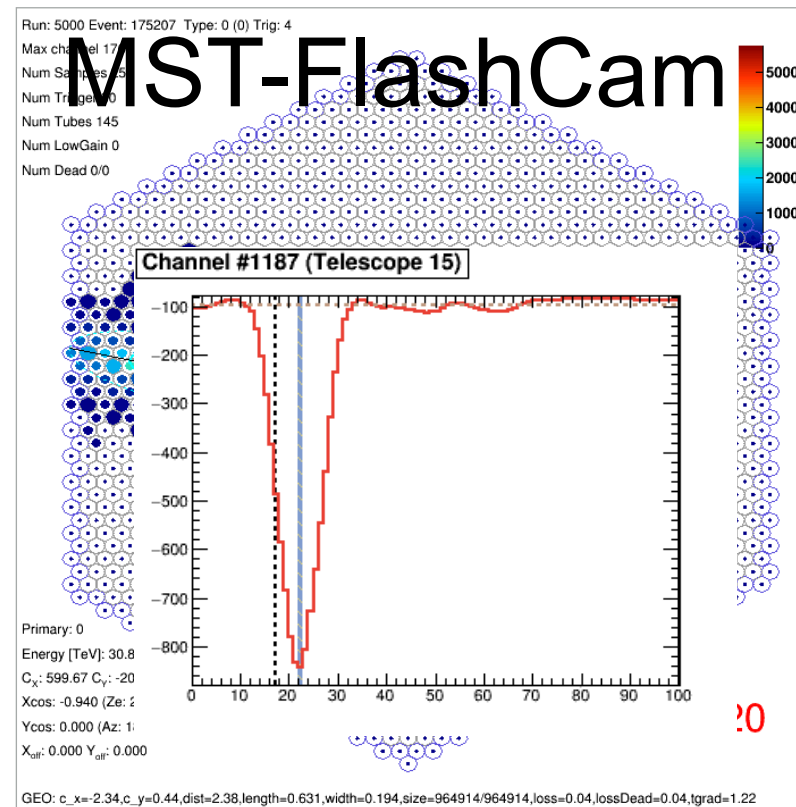
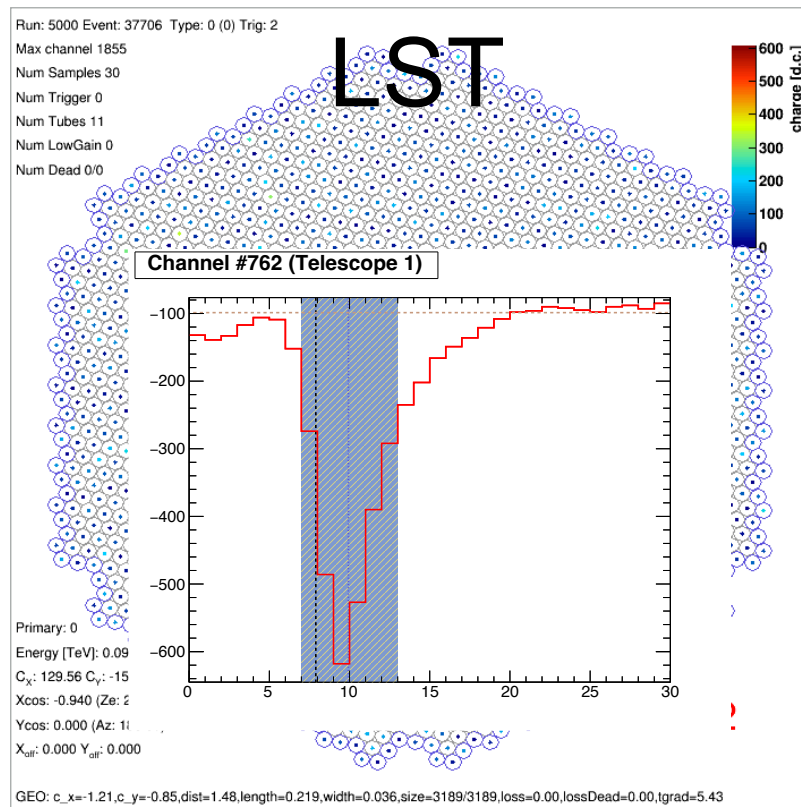


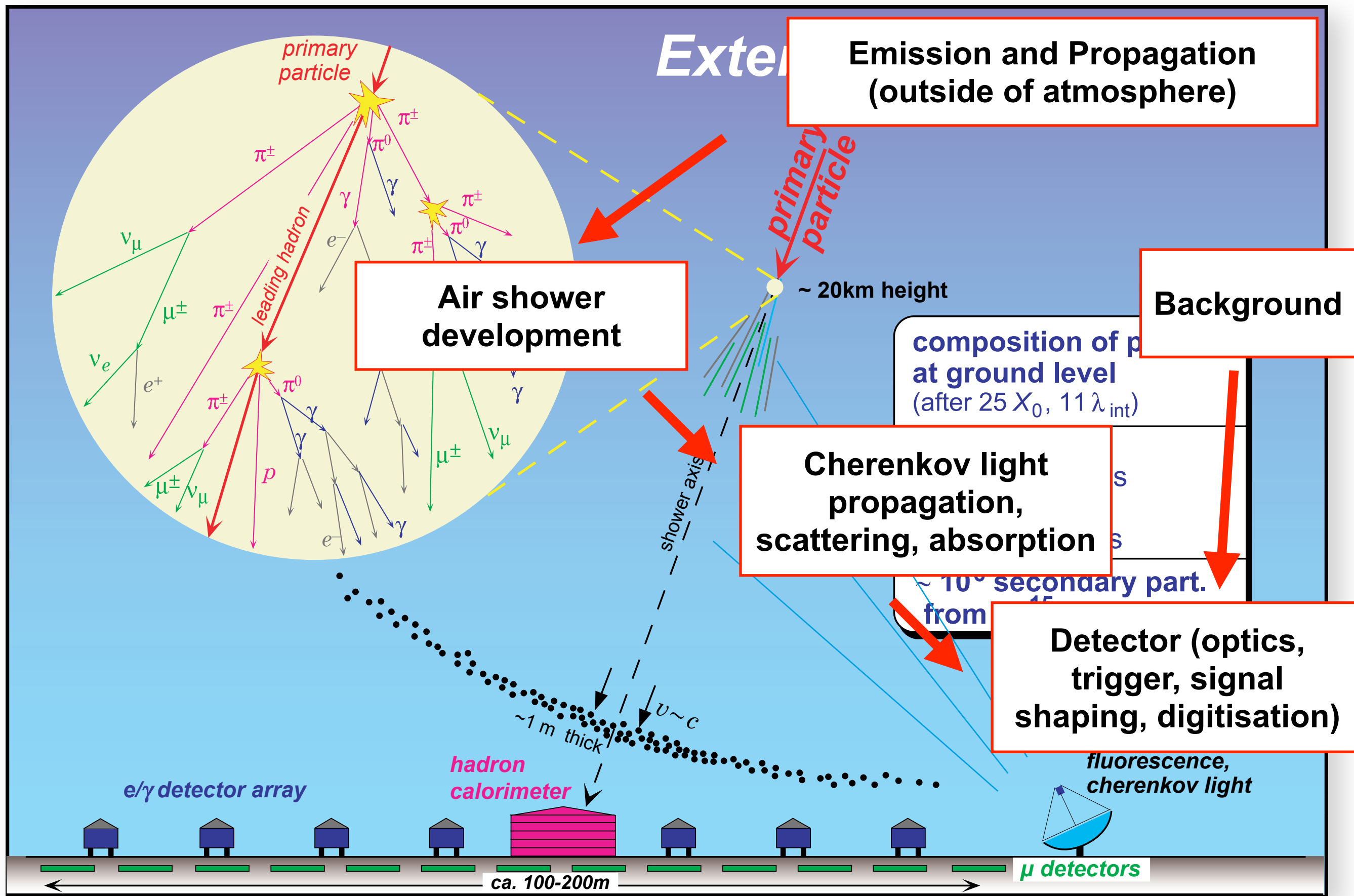


# Single photo electron response.



# Telescopes and Camera types





Air showers are complicated: use Monte Carlo simulations.





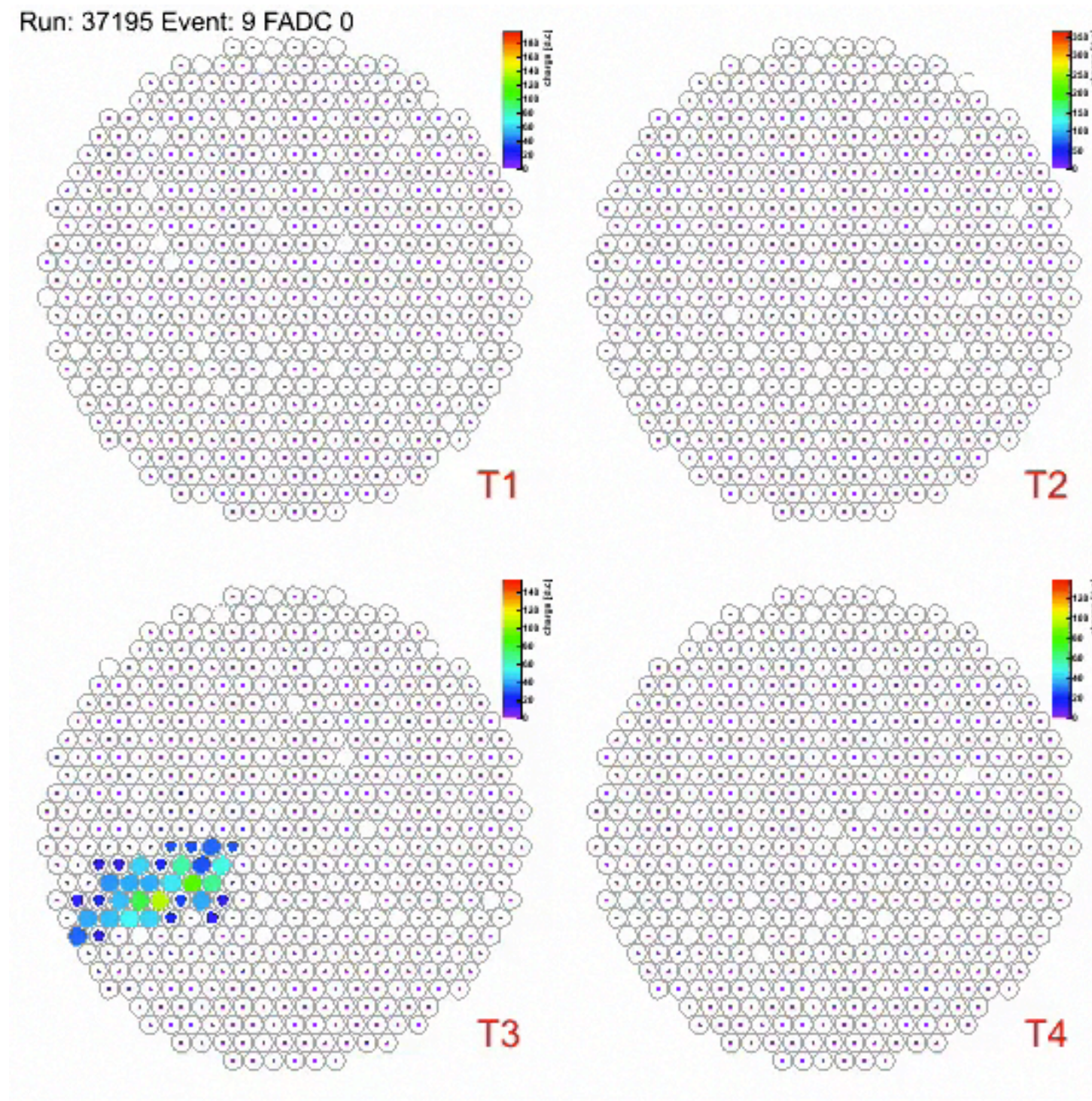




# VERITAS Events

Typical readout rate: 350 Hz  
Signal rate from a strong source 0.3 Hz

event display VERITAS



about every 100th event is a  $\gamma$ -ray

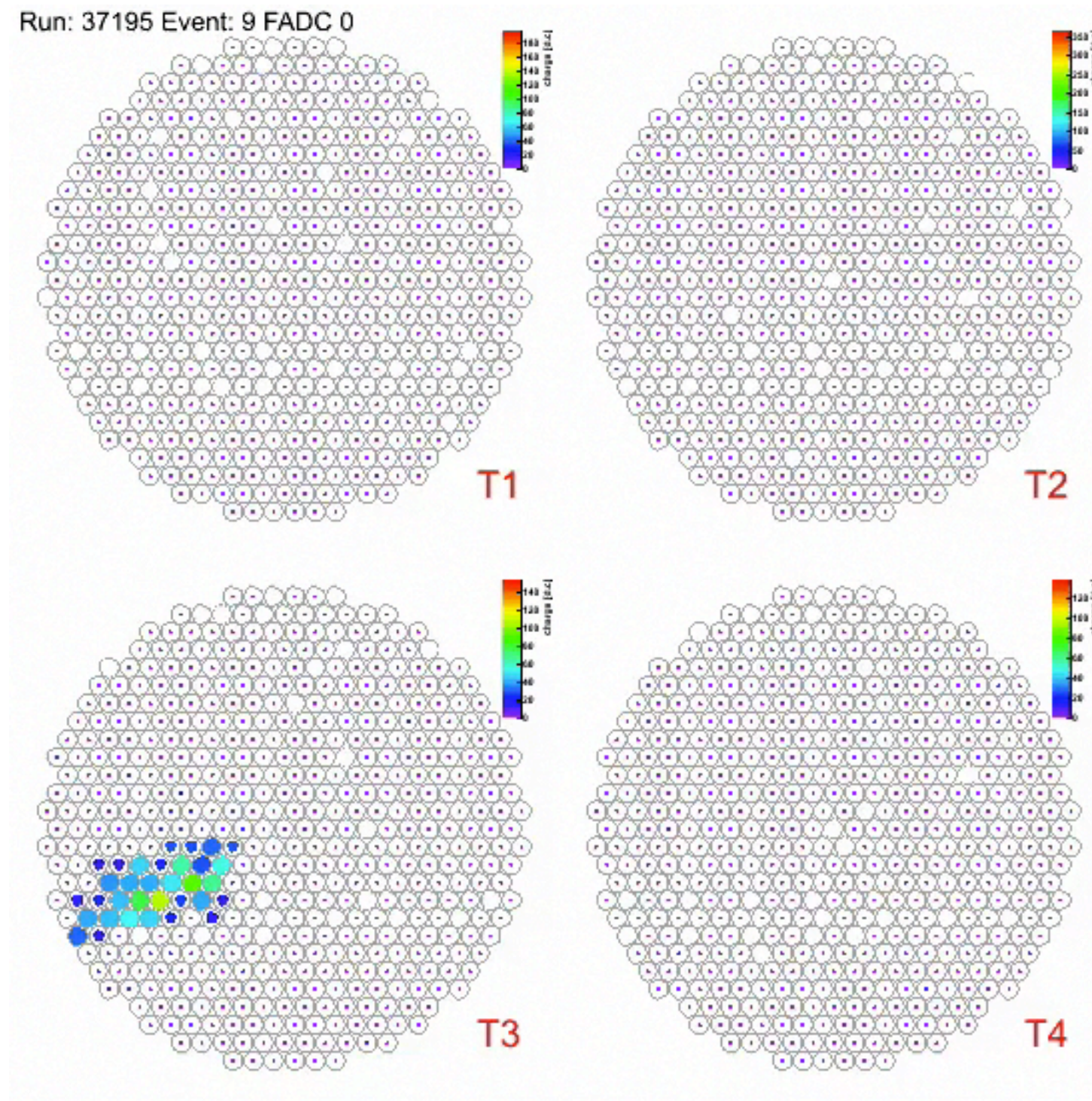
(each frame 2 ns long)



# VERITAS Events

Typical readout rate: 350 Hz  
Signal rate from a strong source 0.3 Hz

event display VERITAS



about every 100th event is a  $\gamma$ -ray

(each frame 2 ns long)

