Imaging Atmospheric Telescopes: Detection Principles

CTAO School 2024

Gernot Maier









What we want to measure.

- For each event.
 - identification (probability that it is a gamma ray)
 - energy
 - direction
 - time
 - (do not measure photon polarisation)

- (obviously we want to measure as many events with best possible precision)
- (replace "gamma ray" by the particle of interest)

Fluxes and spectra.

.. in general:

- low fluxes (10⁻¹⁰ photons/cm²/s)
- spectra with power-law like shape









Air showers are complicated: use Monte Carlo simulations.

Optical imaging. Photodetectors. Triggers. Readout.



TREES OF TREES

Atmosphere. Nature's calorimeter.

Atmosphere.

- composition: 78% N₂, 21% O₂, 0.9% Ar.
- **density** (isothermal approximation):

$$\rho_{\rm atm}(h) \approx \rho_0 {\rm e}^{-h/h_0}$$

 $ho_0 \approx 1.225 \text{ kg/m}^3$ scale height: $h_0 = RT/(\mu g) \approx 8.4 \text{ km}$

- (for air shower simulations: need to be better than isothermal approximation)
- actual matter traversed by air shower: slant depth / thickness

$$X_v(h) = \int_h^\infty \rho_{\rm atm}(z) \, \mathrm{d}z$$









Thickness vs zenith angle.

Anchordoqui et al. 2004



Flat earth.



Fig. 14. The average longitudinal Cherenkov emission profile as a function of distance from the observer (Cherenkov photons emitted in the wavelength range 300–600 nm per meter along the



Bremsstrahlung.

$$e + Z \rightarrow e + \gamma + Z$$

 $e + \gamma_{\text{virtual}} \rightarrow e + \gamma$

Pair production.

$$\gamma + Z \longrightarrow e^+ + e^- + Z$$

 $\gamma + \gamma_{\text{virtual}} \longrightarrow e^+ + e^-$

Energy losses of photons.



Particle Physics Review

Energy losses electrons.



Particle Physics Review

Radiation length.

characteristic amount of matter traversed by electrons/positrons or photons

mean distances over which a high-energy electron reduces its energy by a factor 1/e 7/9th of the mean free path for pair production for a high-energy photon

From fit to data (Dahl):

$$X_0 = rac{716.4 \ \mathrm{g \ cm^{-2}} A}{Z(Z+1) \ln(287/\sqrt{Z})}$$
mixtures: $1/X_0 = \sum_{w_j} w_j/X_j$ wi: fraction by weight

Air:
$$X_0 \approx 37 \,\mathrm{g/cm}^2$$

Scale variable frequently used:

$$t = x/X_0,$$

Radiation vs ionisation losses - Critical energy.

$$dE/dX = -\alpha(E) - E/X_0$$



Figure 34.13: Two definitions of the critical energy E_{e} .



Air: $E_c \approx 85 \,\mathrm{MeV}$

(introduced by Carlson & Oppenheimer 1937)



Simplification:

- one "electron-photon" particle
- initial energy E
- any interaction leads to two new particles of energy E/2
- characteristic splitting length X₀
- critical energy E_C

(introduced by Carlson & Oppenheimer 1937)



Shower development stops at

$$\frac{E}{2^n} = E_c$$

Maximum number of particles

$$N_{max} = 2^n$$
$$= 2^{\log_2 E/E_c}$$
$$= E/E_c$$

Shower maximum at

$$X_{max} \propto X_0 \log \frac{E}{E_C}$$





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Surprisingly good:

- X_{max} predictions quite good
- e/γ assumed to be 2, in reality closer to 1/6

Why is it a simplification?



Simplification:

- one "electron-photon" particle
- initial energy E
- any interaction leads to two new particles of energy E/2
- characteristic splitting length X₀
- critical energy E_C

Why is it a simplification?



Heitler model. Simplifications.

- particle interactions are stochastic processes
- atmosphere is complicated (e.g., density profile)
- analytical solutions insufficient -> Monte Carlo Methods



Simplification (what is wrong):

- Xo
 - one "electron-photon" particle
- initial energy E any interaction leads to two new
 - particles of energy E/2
- \times characteristic splitting length X_0
- x critical energy Ec

Any interaction leads to two new particles with E/2?



Figure 34.12: The normalized bremsstrahlung cross section $k d\sigma_{LPM}/dk$ in lead versus the fractional photon energy y = k/E. The vertical axis has units of photons per radiation length.



Figure 34.18: The normalized pair production cross section $d\sigma_{LPM}/dx$, versus fractional electron energy x = E/k.

Longitudinal development.



Electron longitudinal development.



Non-EM particles in gamma-ray showers.



Pair production cross section with 1/m² term.

Air showers. Primary Hadrons.

Why do we care?

Hadronic showers.

 different secondaries, transverse momentum, resonances, QCD color flows, string fragmentation, jet production, pomerons, parton densities, ... this is complicated...

^t.K[±] $\rightarrow \mu^{\pm} + \nu$

- absolute necessity of good models (LHC!).
- QGSJet, Epos, Sibyl, FLUKA, URQMD, ...
- basic picture from simplified model:
 - produce pions, muons, e⁻/e^{+,} γ's

Energy flow.

J.Knapp 2017

Pions - decay vs interaction.



Heitler Matthews Model.



from Cazon 2018

Simplification:

- neutral pions decay immediately (initiate electromagnetic shower)
- charged pions interact and initiate secondary cascade
- cascade stops of $E = E_{decay}$
- each charged pions produces one muon during decays
- muons don't interact

Can get some basic predictions, e.g.

$$N_{\mu} = \left(\frac{E_{\circ}}{\xi_{\rm c}^{\pi}}\right)^{\beta} \approx 10^4 \left(\frac{E_{\circ}}{1 \,\,{\rm PeV}}\right)^{0.85}$$

$$\frac{E_{\rm em}}{E_{\rm o}} = \frac{E_{\rm o} - N_{\mu}\xi_{\rm c}^{\pi}}{E_{\rm o}} = 1 - \left(\frac{E_{\rm o}}{\xi_{\rm c}^{\pi}}\right)^{\beta - 1}$$

~ 70% (at energies relevant for CTA)

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Superposition model.

Proton-induced shower

$$N_{\rm max} = E_0/E_c$$

$$X_{\rm max} \sim \lambda_{\rm eff} \ln(E_0)$$

$$N_{\mu} = \left(\frac{E_0}{E_{\rm dec}}\right)^{\alpha} \qquad \qquad \alpha \approx 0.9$$

Assumption: nucleus of mass A and energy E_0 corresponds to A nucleons (protons) of energy $E_n = E_0/A$

$$N_{\max}^{A} = A\left(\frac{E_{0}}{AE_{c}}\right) = N_{\max}$$
$$X_{\max}^{A} \sim \lambda_{\text{eff}} \ln(E_{0}/A)$$
$$N_{\mu}^{A} = A\left(\frac{E_{0}}{AE_{\text{dec}}}\right)^{\alpha} = A^{1-\alpha}N_{\mu}$$

Many more muons compared to protons: He: 3.5x; Fe 37x
Gamma vs protons.









Irreducible background from hadronic showers?



Irreducible background from hadronic showers?



Single Pion Dominated Events.



Dan Parsons (see also Maier & Knapp 2007)

DESY. | IACT Detection Principles | Gernot Maier



Air showers. Lateral extension.

Lateral extension of electromagnetic showers.

determined by multiple Coulomb scattering

(and not opening angle of pair production / Bremsstrahlung)

Scatter angle distribution not Gaussian (as expected by central limit theorem) single scattering important, as cross section falls off too slowly with 1/0⁴

Molière's Theory for multiple scatter. For air showers: Kamata & Nishimura (1959) and Greisen (1956) Implementation in air shower codes non-trivial (check EGS manual on multiple scatter)

Note: different lateral distributions for each particle type (electrons, photons, ...)

Multiple Scattering

Hanson et al 1951

Molière's theory and the issue in academic publishing

Cherenkov light.

Cherenkov Light.

- polarisation of dielectric medium by charged particle
- constructive interference when particle is faster than the emitted radiation (c/n)
- emission in a cone with respect to the particle direction

Cherenkov condition: $n\beta>1$

Cherenkov.

You can get a Nobel prize for your PhD...

Foundation archive.

 $\exists \mathbf{r} \times \mathbf{i} \vee \rangle$ physics > arXiv:1101.4535

Physics > History and Philosophy of Phy

Pavel Alekseyevich Cherenkov The Nobel Prize in Physics 1958

Born: 28 July 1904, Novaya Chigla, Russia

Died: 6 January 1990, USSR (now Russia)

Affiliation at the time of the award: P.N. Lebedev Physical Institute, Moscow, USSR (now Russia)

Prize motivation: "for the discovery and the interpretation of the Cherenkov effect"

Prize share: 1/3

The Discovery of Cherenkov Radiation and its use in the detection of extensive air showers

A A Watson

Cascades of charged r atmosphere: these 'ex arrival direction distril

[Submitted on 24 Jan 2011]

the intensity of radiation found using a technique, called 'quenching', in which the dark-adapted eye was used with a graded wedge to provide calibration of the light intensity. These were difficult and delicate experiments requiring high levels of both patience and experimental skill. Cherenkov discovered that light was emitted even when the vessel contained only sulphuric acid, the solvent for the uranyl salt. He went on to demonstrate that the light was observed in a range of different solvents. In a moving obituary [4], which mentions only briefly Cherenkov's considerable post-war contributions to accelerator physics, Chudakov writes "The phenomenon was not and probably could not have been discovered earlier by someone more experienced in physics than Cherenkov was in the 1930s. To determine the nature of the faint blue light produced in different liquids by gamma rays from a radioactive source seemed to require a young fellow from a rural area, inexperienced but with immense patience and vigour".

Observation of polarization was an important clue to the eventual interpretation but the critical breakthrough was Cherenkov's discovery in 1936 that the radiation was emitted asymmetrically only in the forward direction with respect to the direction of the incoming γ -ray beam [5], at an angle

Cherenkov emission.

Cherenkov condition: $n\beta>1$

light is emitted along a cone with half opening angle θ : $\cos \Theta = \frac{1}{n\beta}$

good approximation: $\Theta_c \approx \sqrt{2(n-1)}$ radians

number of Cherenkov photons per path length x:

$$\frac{dN}{dx} = 2\pi\alpha z^2 \int_{\lambda_1}^{\lambda_2} \left(1 - \frac{1}{n^2\beta^2}\right) \frac{d\lambda}{\lambda^2} = 2\pi\alpha z^2 \int_{\lambda_1}^{\lambda_2} \sin^2\Theta \frac{d\lambda}{\lambda^2}$$

eta = v/c n = refractive index z = charge λ = wavelength lpha = 1/137

Index of refraction.

refractive index in air scales with density: n=1+0.000283~
ho(h)/
ho(0)

(additional dependency on pressure, temperature, water vapour content)

Current simulations use n(450 nm).

Cherenkov angle vs electron energy

Thresholds for Cherenkov emission: Electrons: 20 MeV at sea level / 35 MeV at 10 km Muons: 4.5 GeV at sea level / 8 GeV at 10 km

DESY.

refractive index in air scales with density

 $n = 1 + 0.000283 \ \rho(h) / \rho(0)$

refractive index in air scales with density

 $n = 1 + 0.000283 \ \rho(h) / \rho(0)$

~1.3 deg at sea level

refractive index in air scales with density

refractive index in air scales with density

 $n = 1 + 0.000283 \ \rho(h) / \rho(0)$

Lateral distributions.

Lateral distributions.

Lateral distributions

10¹

500

distance to shower [m]

Lateral distributions vs shower development.

T. Hassan et al./Astroparticle Physics 93 (2017) 76-85

Cherenkov photon arrival time.

Proton vs Gamma-ray showers

Imaging Technique - Air Showers

Stereoscopy.

Seasonal changes - density vs height.

Refractive index only (same density profile).

K. Bernlöhr / Astroparticle Physics 12 (2000) 255-268

Different atmospheric profiles.

K. Bernlöhr / Astroparticle Physics 12 (2000) 255-268

No absorption applied.
Propagation of Cherenkov light.

molecular absorption bands

• molecular (Rayleigh) scattering

aerosol (Mie) scattering & absorption

- current simulations: scattered == absorbed
- clouds not covered here.

Atmospheric extinction.



DESY. | IACT Detection Principles | Gernot Maier

Atmospheric Extinction.



Cherenkov spectrum after extinction.



Scattered == absorbed?







Snell's law:

$$\sin(\theta_2) = \frac{n_1}{n_2} \cdot \sin(\theta_1)$$

https://britastro.org/2019/atmospheric-refraction



Cherenkov light is emitted in the atmosphere





Geomagnetic field.



Geomagnetic field.









from K.Bernlöhr

Magnetic field normal to shower direction.

ALMA 22°59'56"S, 67°45'39"W - Magnetic Field [µT]

S.C. Commichau et al. / Nuclear Instruments and Methods in Physics Research A 595 (2008) 572-586



Thesis M.Krause

Geomagnetic field - impact on image reconstruction.



 $^{\circ}$ 450 GeV γ -rays, 100 m impact parameter, ZA = 40°, Az = 0° and 180°,

S.C. Commichau et al. / Nuclear Instruments and Methods in Physics Research A 595 (2008) 572-586

Geomagnetic field - impact on sensitivity.



Looking North - Looking South

(using analysis techniques ignoring the impact of the geomag. field on the shower development)

Geomagnetic field - 10 y change in declination.



Summary - Cherenkov photons on the ground.



First detectors



Backgrounds.

Fluorescence.

- fluorescence emission from deexcitation of N₂ states (290-430 nm)
- less efficient light emission for 1 GeV electron near ground: 30 photons from Cherenkov light vs 4 photons from fluorescence light (per m track length)
- longer time profile: microseconds vs 10s of nanoseconds





Fluorescence.



Night sky background.



Impact of high night-sky-background light levels.



T. Hassan et al./Astroparticle Physics 93 (2017) 76-85

Muons.



Direct Cherenkov Light (not a background).

$$\frac{dN}{dx} = 2\pi\alpha z^2 \int_{\lambda_1}^{\lambda_2} \left(1 - \frac{1}{n^2\beta^2}\right) \frac{d\lambda}{\lambda^2} = 2\pi\alpha z^2 \int_{\lambda_1}^{\lambda_2} \sin^2\Theta \frac{d\lambda}{\lambda^2}$$



D.B. Kieda et al. | Astroparticle Physics 15 (2001) 287-303

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D.B. Kieda et al. | Astroparticle Physics 15 (2001) 287-303

Simulations.

CORSIKA. sim_telarray.

(others packages exist)



ICRC 1990.

AIR SHOWER SIMULATIONS FOR KASCADE

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Abstract

A detailed simulation program for extensive air showers and first results are presented. The mass composition of cosmic rays with $E_0 \ge 10^{15} eV$ can be determined by measuring electrons, muons and hadrons simultaneously with the KASCADE detector.



https://www.iap.kit.edu/corsika/



CORSIKA 7





Cherenkov emission in the simulations.

Large number of Cherenkov photons emitted. (100 TeV shower with typically 100 billion photons.



hone everal 105

Cherenkov emission in the simulations.



Bunches.



Not all emitted Cherenkov photons will lead to a detection. Emit in **bunches** (non integer)



sim_telarray manual

Detector level.



- a: recorded photon bunch
- b: not recorded because not intersecting sphere
- c: recorded (not in 'shadow' but hitting a shadow grid cell)
- d: not recorded because not hitting a shadow grid cell



Telescopes.



Telescope Optics.

- imaging quality optical point-spread function
- (non)isochronism
- costs



Ray tracing and optical PSF.



Optical point-spread function.



HESS 2 (K. Bernlöhr 2006)



Time spread - mirror design


Parabolic vs Davis Cotton vs Intermediate design

- optical point-spread function:
 - Davis-Cotton with smaller radial PSF than parabolic (especially with increased off-axis angles)
 - transverse direction PSF very similar
- timing
 - parabolic mirror essentially isochronous
 - 12-m Davis Cotton: top-hat time distribution of 3.6 ns (1.05 ns rms)
- CTA MSTs are following an intermediate design using a dish between Davis-Cotton and parabolic
 - almost DC-like PSF with a time spread of 0.41 ns rms

Mirror reflectivity.



Light concentrators.





Figure 5 – Camera window transmission as a function of wavelength and incident angle for the SST camera.

Cameras.

K.Bernlöhr



Telescopes and Camera types











Quantum and photodetector efficiencies.



Efficiencies.



Trigger and readout - oversimplified.



Single photo electron response.



Telescopes and Camera types













Air showers are complicated: use Monte Carlo simulations.



VERITAS Events

Typical readout rate: 350 Hz Signal rate from a strong source 0.3 Hz

a y-ray

about every 100th event is



(each frame 2 ns long)

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