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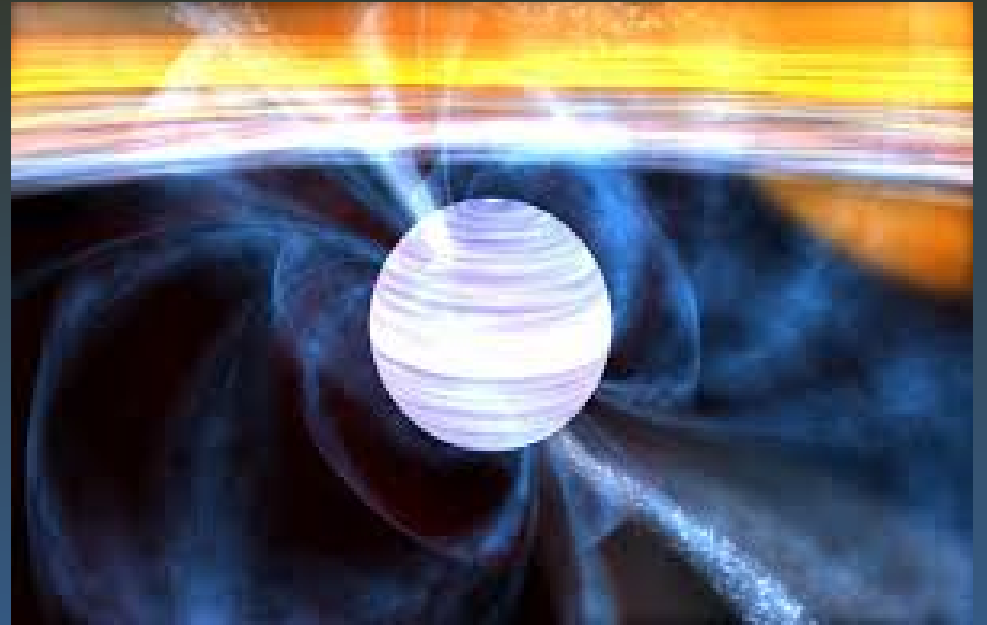
# A Luminosity Function for Millisecond Pulsars in Globular Clusters

With Francesca Calore (LAPTh), Silvia Manconi (LAPTh) and Gabrijela Zaharijas (UNG)

# Millisecond Pulsars

MilliSecond Pulsars (MSPs) are Pulsars with  $P < 30$  ms

- Observed for the first time in radio  
[DOI:10.1038/300615A0]
- We know around 300 MSPs, ~144 of which detected in gamma-rays

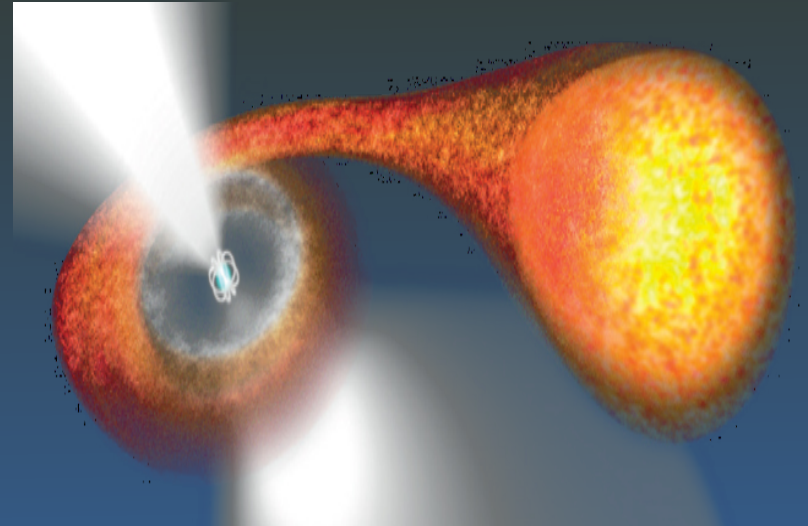


<https://svs.gsfc.nasa.gov/10144/>

# MSP Formation History

MSPs are considered recycled objects

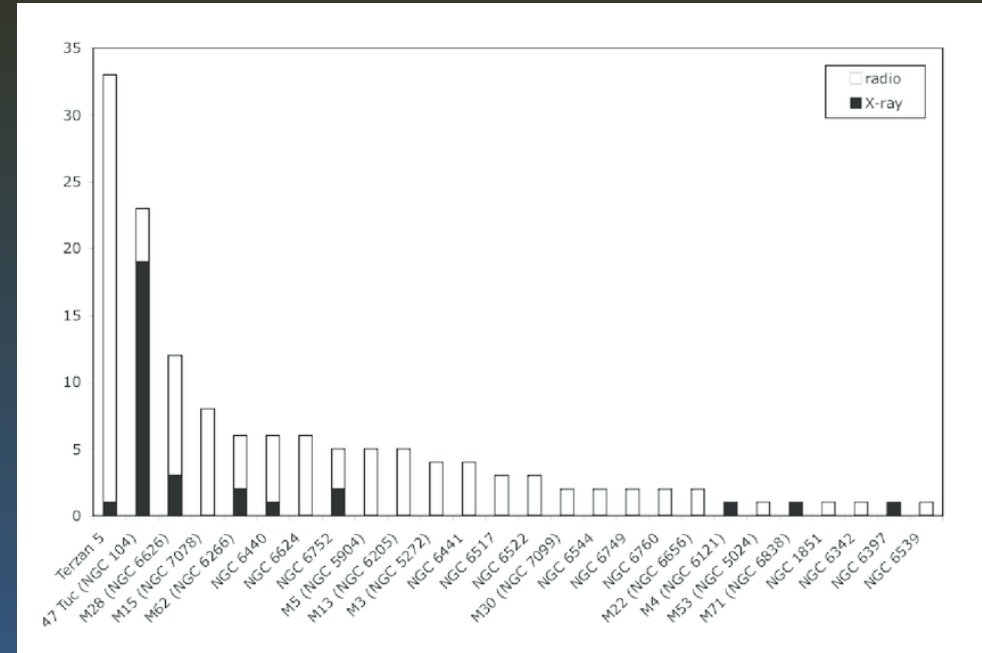
- They are likely related to Low-Mass X-Ray Binaries (LMXB)
- Observations of widows and accreting Neutron Stars (NS) support of this theory



[https://cerncourier.com/wp-content/uploads/2013/10/CCast1\\_09\\_13.jpg](https://cerncourier.com/wp-content/uploads/2013/10/CCast1_09_13.jpg)

# MSPs and Globular Clusters

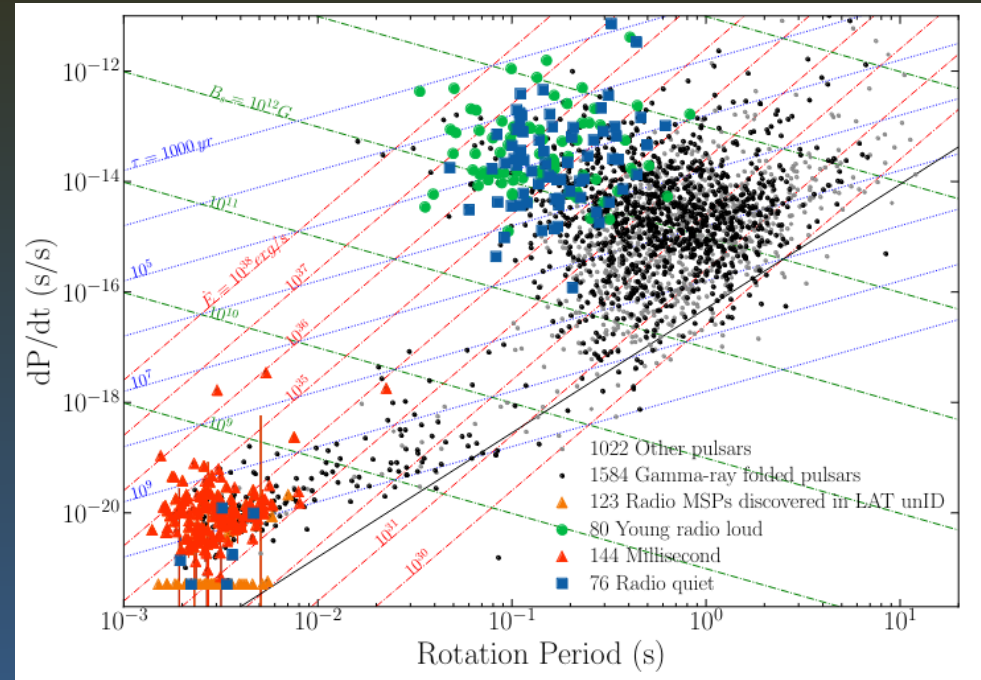
- Globular Clusters (GCs) are rich in MSPs
- Most (~40%) MSPs are found in GCs (similar to LMXBs)
- In GCs LMXBs may be formed by tidal capture
- In GCs pulsars formed from Core Collapse Super Novae (CCSN) can escape
- MSPs in GCs are detected in radio separately



[https://www.researchgate.net/figure/A-histogram-of-radio-and-X-ray-detected-millisecond-pulsars-in-globular-clusters\\_fig1\\_45921190](https://www.researchgate.net/figure/A-histogram-of-radio-and-X-ray-detected-millisecond-pulsars-in-globular-clusters_fig1_45921190)

# MSPs in Gamma-Rays

- 144 MSPs have been detected in gamma-rays
- They make up most of the gamma-ray emission from GCs
- MSPs represent nearly half of the gamma-ray emitting Pulsars currently detected

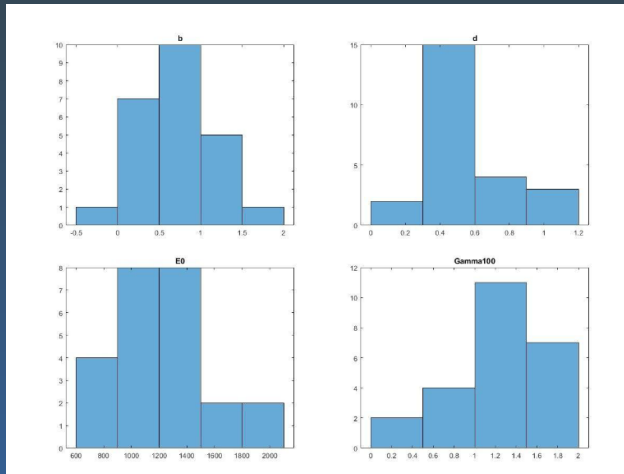


Arxiv:2307.11132

# MSPs Gamma-Ray Spectrum

- Pulsars' Spectral Energy Distributions (SEDs) are well represented by the Power Law Exponential Cutoff 4 (PLEC4) distribution, given as:

$$\frac{dN}{dE} = N_0 \left( \frac{E}{E_0} \right)^{-\Gamma + \frac{d}{b}} \exp \left( d/b^2 \left( 1 - \left( \frac{E}{E_0} \right)^b \right) \right)$$



The means are:

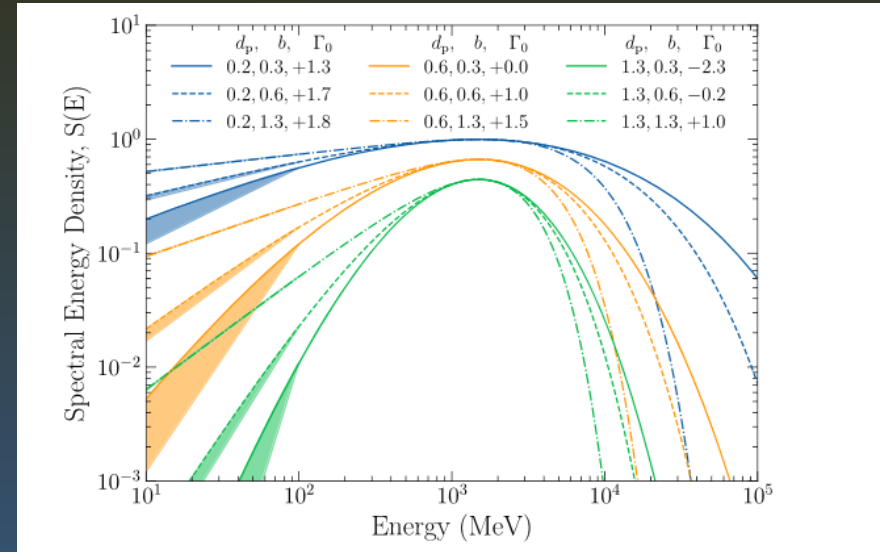
$$d = 0.5473 \pm 0.2625$$

$$b = 0.7132 \pm 0.4491$$

$$\Gamma = 1.907 \pm 0.8052$$

$$E_0 = (1.209 \pm 0.3076)$$

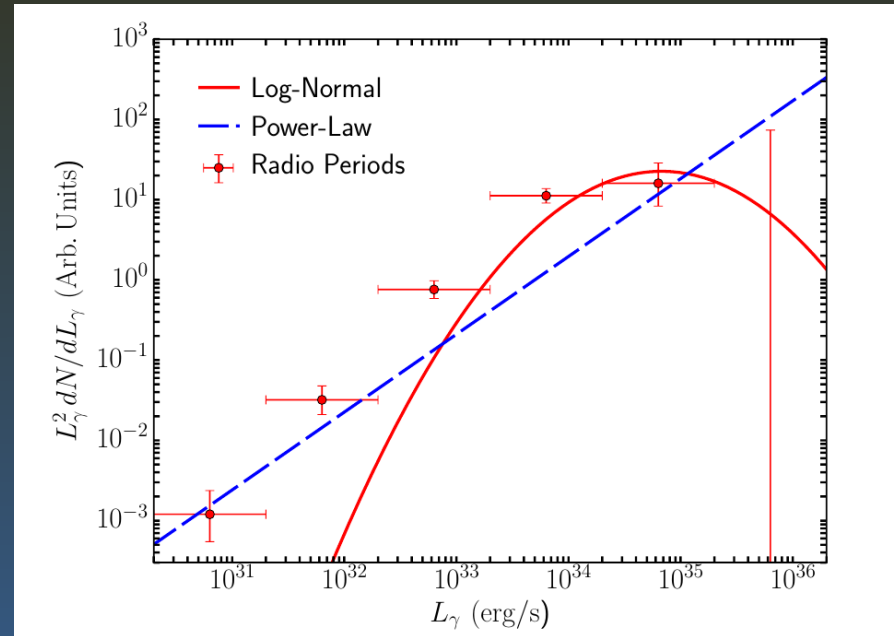
GeV



Arxiv: 2307.11132

# MSPs in GCs: Past Studies

- [Arxiv: 1606.09250] found a luminosity function for MSPs in GCs
- They consider 157 gamma-ray emitting GCs
- They use the relationship between Stellar Encounter Rate and number of MSPs



# MSPs in GCs: Past Studies

- This luminosity function underestimate the number of MSPs in GCs
- A linear relation between stellar encounter rate and the number of MSPs is assumed
- We want a luminosity function that uses the information on MSPs' spectra
- It finds 12 MSPs in Terzan 5
- We know of at least 49 MSPs in Terzan 5 [Arxiv: 2403.17799]



# On this Project

## Goal:

- To find a Luminosity Function for MSPs in GCs

## Methodology:

- Bayesian Inference with Nested Sampling algorithm to find the parameters of the luminosity function
- GCs' SEDs are obtained through FermiPy

## Members:

- Francesca Calore (LAPTh)
- Silvia Manconi (LAPTh)
- Francesco Xotta (UNG)
- Gabrijela Zaharijas (UNG)

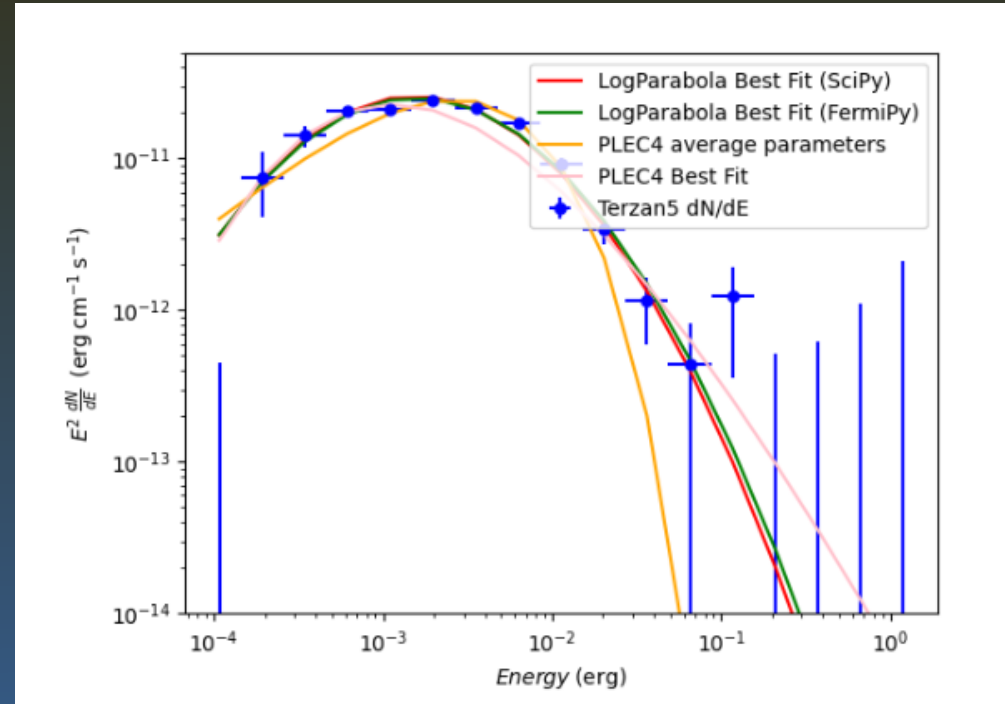
# MSPs in GCs: Terzan5

- Find average parameters of PLEC4 for MSPs

We then consider Terzan5, the richest GC in MSPs, we check:

- That it can be fit to the PLEC4 distribution
- How its spectrum compares to the PLEC4 with average MSP parameters

We obtain the flux of Terzan 5 using FermiPy



Fit of Terzan 5 to a LogParabola and to a PLEC4

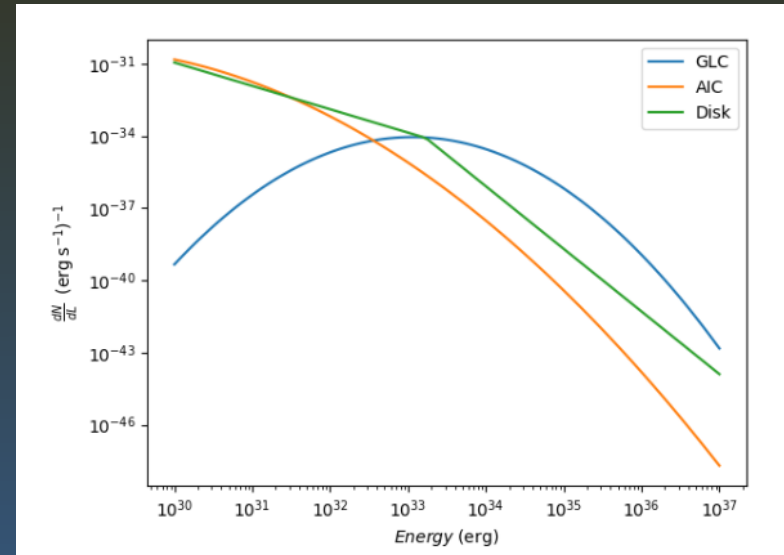
# MSPs in GCs: Expected Result

- We wish to find a luminosity function for the 0.1-100 GeV bin
- We consider the Log-Normal distribution:

$$\frac{dN}{dL}(L; L_0, \sigma) \propto \frac{\log_{10} e}{\sigma \sqrt{2\pi} L} \exp\left(-\frac{(\log_{10} L - \log_{10} L_0)^2}{2\sigma^2}\right)$$

A Luminosity Function tells the relative number of MSPs with a given luminosity

- GLC:  $L_0 = 8.8 \times 10^{33} \text{ erg s}^{-1}$ ,  $\sigma = 0.62$
- AIC:  $L_0 = 4.3 \times 10^{30} \text{ erg s}^{-1}$ ,  $\sigma = 0.94$
- DISK:  $L_b = 1.7 \times 10^{33} \text{ erg s}^{-1}$ ,  $n_1 = 0.97$ ,  $n_2 = 2.60$



Comparison of three benchmark luminosity functions, two of which (GLC and AIC) use a Log-Normal luminosity function, while the third (Disk) uses a Broken-Power Law luminosity function

# MSPs in GCs: Procedure

Given N GCs, we have N+2 free parameters:

- $N_l$  with  $l=1, \dots, N$ : number of MSPs in the  $l$ -th GC
- $L_0$
- $\sigma$

We follow the steps below:

- We sample for each GC  $N_l$  MSPs' luminosities from the luminosity function
- We find the normalization of the PLEC4 with average MSPs parameters

$$F_i \equiv \int k_i \times \frac{dN}{dE}(E) \times E dE \equiv \frac{L_i}{4\pi d_{GC}^2}$$

- We compute the  $\chi^2$

$$\chi_k^2 = \left( \frac{F_{MSP} - F_{GC}}{\Delta F_{GC}} \right)_k^2$$

- We minimize it to find the best parameters using a Nested Sampling Algorithm

Sample  $N_l$  MSPs,  
 $l=1, \dots, N$

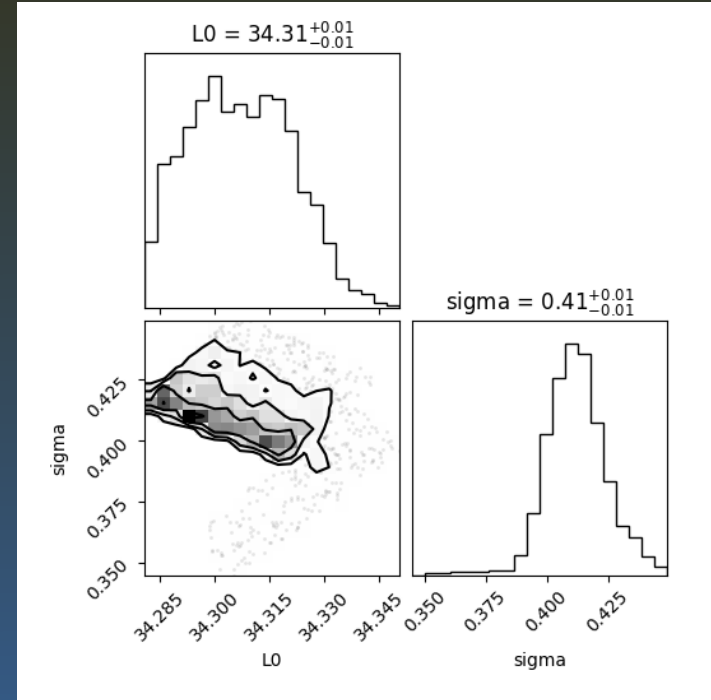
Find their spectrum

Compute  $\chi^2$

Minimize  $\chi^2$

# MSPs in GCs: Some Results

- Here we assume the same relationship of [Arxiv: 1606.09250], but use our method



# MSPs in GCs: Prospects

In the future, we intend to make the following changes:

- Sample every PLEC4 parameter instead of just the normalization
- Consider possible relationship to the Stellar Encounter Rate
- Consider the number of MSPs detected in Globular Clusters

The background is a deep, dark blue space filled with numerous small, white stars of varying sizes. Two prominent, bright purple light streaks, resembling comets or nebulae, sweep across the scene from the top-left and bottom-right corners towards the center. A single, larger, bright blue-white star is positioned near the center of the frame, directly below the text.

Thank You!

# MSPs in GCs: Sampling

- Example of Sampling of MSPs
- The number of MSPs however can be very small, leading to big uncertainties in the  $\chi^2$

