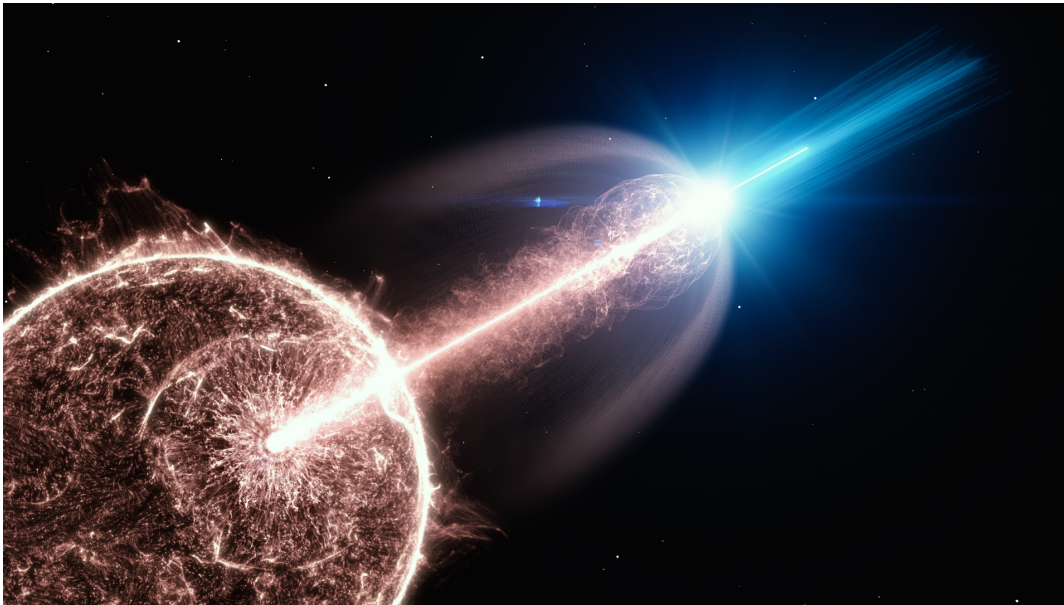
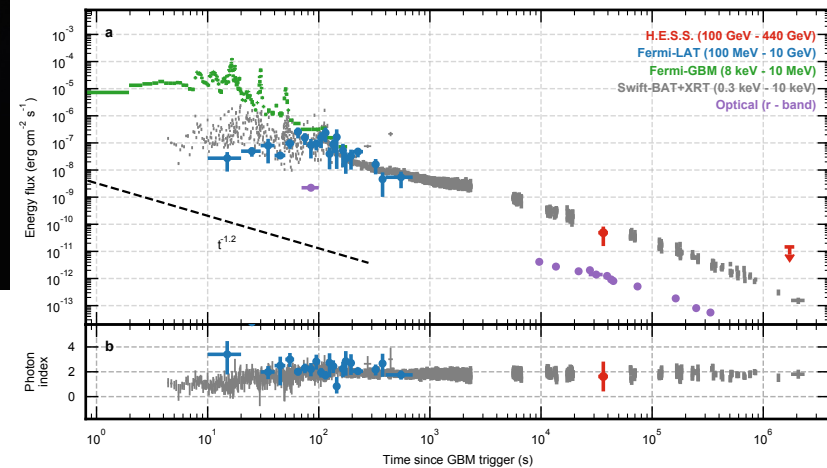


Gamma-Ray Emission from GRBs Afterglows- A Brief Overview

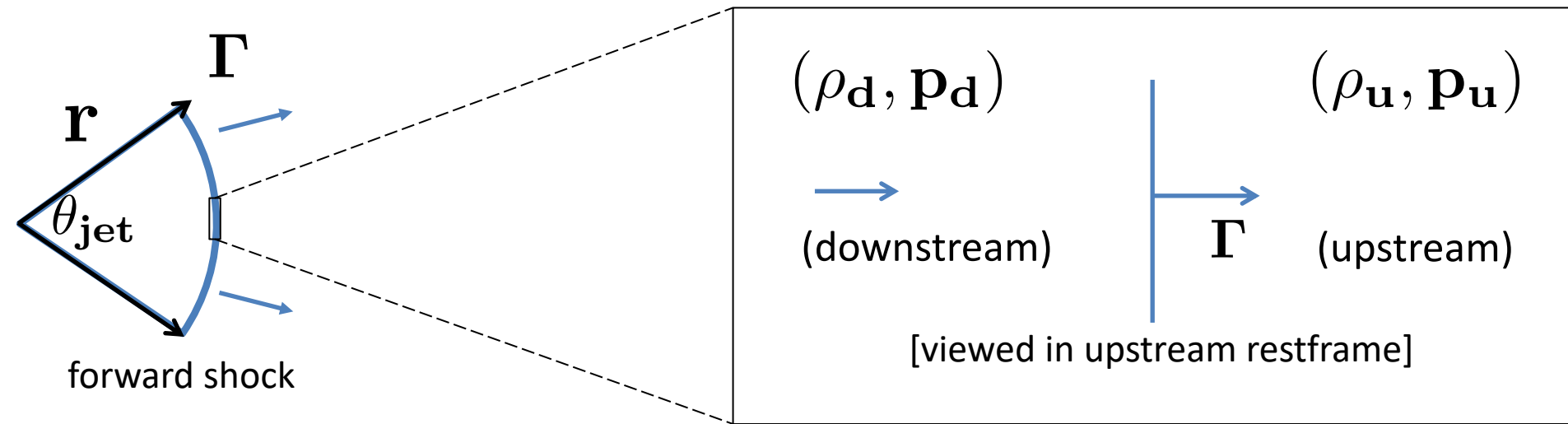


Caveat! The Gamma-Ray emission I will be focusing on here is the radiation observed during the “afterglow” phase of the GRB



[HESS Coll. Nature 2019]

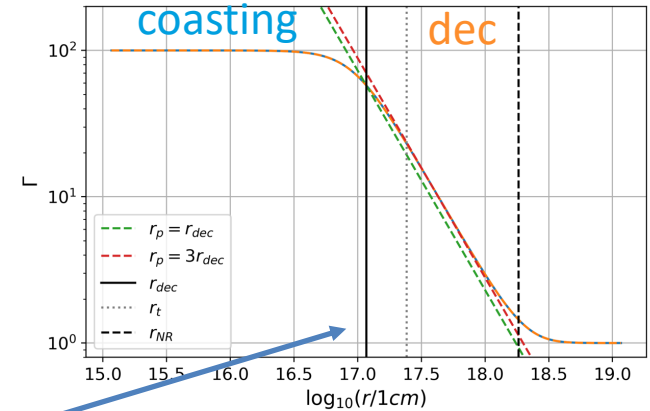
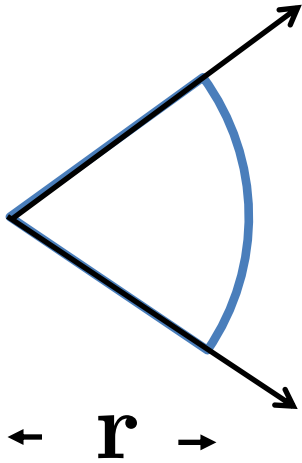
GRBs: Nature's Machines for Converting Rel. Ram Pressure into Gamma-Rays



- Not actually isotropic outflows, but can be considered as “quasi-isotropic” since $\theta_{\text{jet}} > 1/\Gamma$
- Isotropic equivalent energy in gamma-rays, E_{iso} , up to 10^{54} erg, close to Gravitational binding energy limit
- Extremely efficient emitters in terms of converting kinetic energy flux to radiation

Temporal Compression of Signal

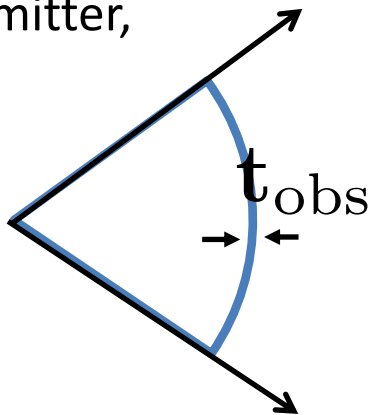
For a constant density medium, during the deceleration phase,



[Plot Courtesy of M. Klinger]

$$R_{\text{dec}} \approx 10^{17} \left(\frac{E_{\text{iso}}}{10^{53} \text{ erg}} \right)^{1/3} \left(\frac{n}{1 \text{ cm}^{-3}} \right)^{-1/3} \left(\frac{\Gamma}{100} \right)^{-2/3} \text{ cm}$$

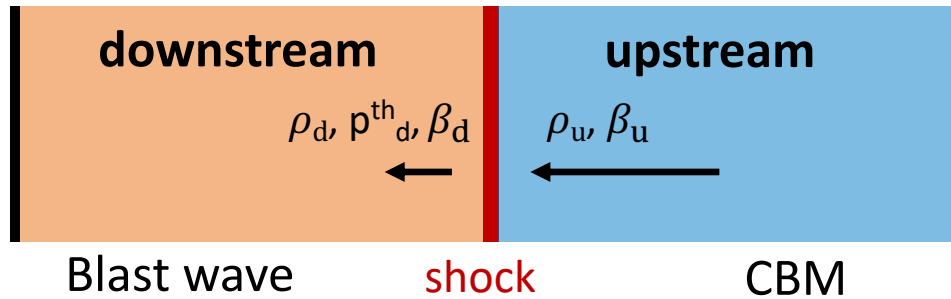
Since radiation is emitted by a relativistically moving emitter,



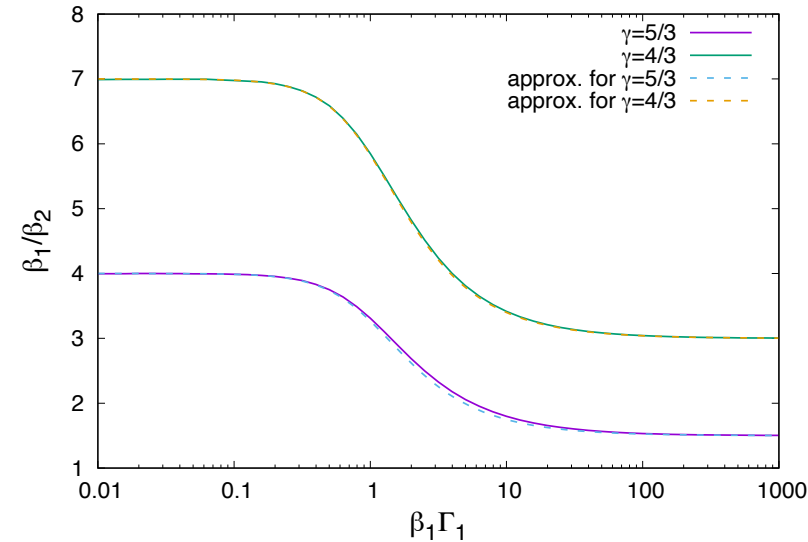
$$ct_{\text{obs}} = (1 - \beta)r$$

$$t_{\text{dec}}^{\text{obs}} \approx \frac{R}{c\Gamma^2} = 300 \left(\frac{R}{10^{17} \text{ cm}} \right) \left(\frac{\Gamma}{100} \right)^{-2} \text{ s}$$

Rel. Hydro Shock- Downstream Partition of the Upstream Ram Pressure



[viewed in shock restframe]



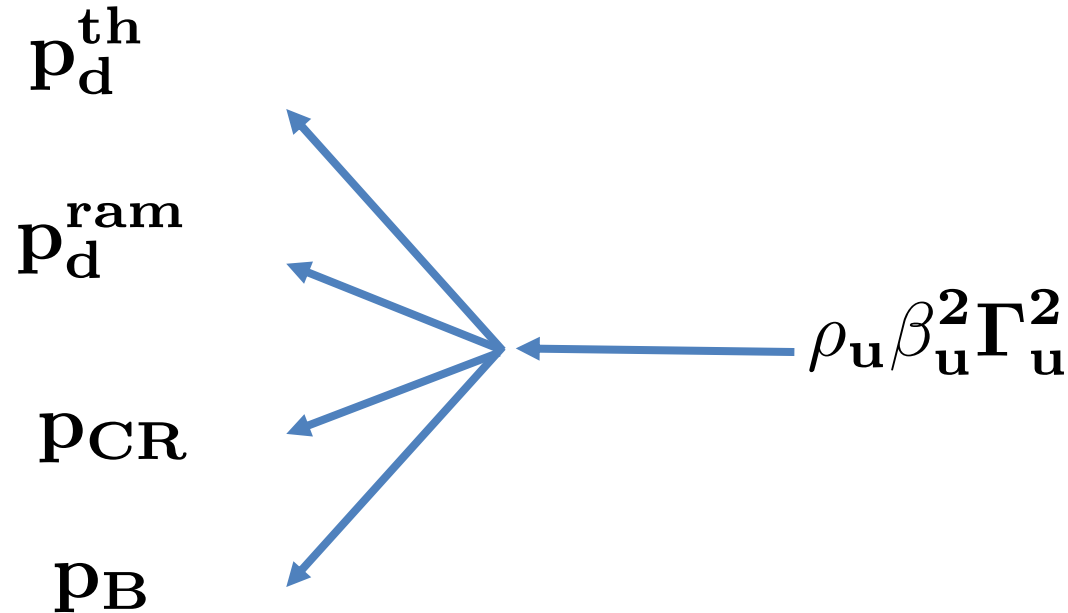
$$p_d^{th} = \frac{2}{3} \rho_u \beta_u^2 \Gamma_u^2$$

$$w_d \beta_d^2 \Gamma_d^2 = \frac{1}{3} \rho_u \beta_u^2 \Gamma_u^2$$

$$\rho_u \beta_u^2 \Gamma_u^2$$

Diagram showing the partitioning of the upstream ram pressure $\rho_u \beta_u^2 \Gamma_u^2$ into thermal pressure p_d^{th} and downstream kinetic energy $w_d \beta_d^2 \Gamma_d^2$. Blue arrows point from the upstream ram pressure term to the two equations above.

Rel. MHD Shock- Downstream Partition of the Upstream Ram Pressure



$$\varepsilon = \frac{p}{\rho_u \beta_u^2 \Gamma_u^2}$$

- ① ε - key parameters which we don't a priori know, but which we may probe with observations

Relativistic MHD Shocks

Downstream magnetic field partition of upstream ram pressure:

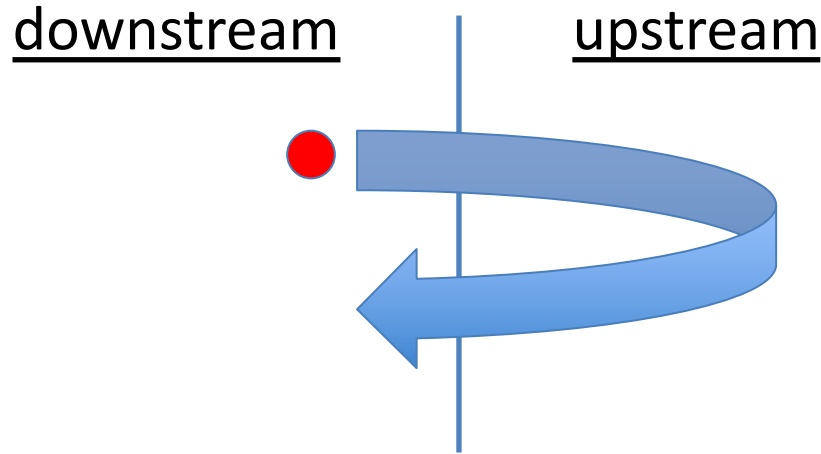
$$\varepsilon_B = \frac{U_B}{\rho_u \beta_u^2 \Gamma_u^2}$$

For

$$\varepsilon_B = 0.1 \quad n_u = 1 \text{ cm}^{-3} \quad \beta_u \Gamma_u = 10$$
$$B \approx 0.6 \text{ G}$$

$$\varepsilon_B = 10^{-5} \quad n_u = 1 \text{ cm}^{-3} \quad \beta_u \Gamma_u = 10$$
$$B \approx 6 \text{ mG}$$

Particle Acceleration and Magnetic Turbulence



$$\begin{aligned}t_{\text{acc.}} &= \Delta t_{\text{cyc}} (\mathbf{E} / \Delta \mathbf{E}_{\text{cyc}}) \\ &= t_{\text{scat}} / \beta^2\end{aligned}$$

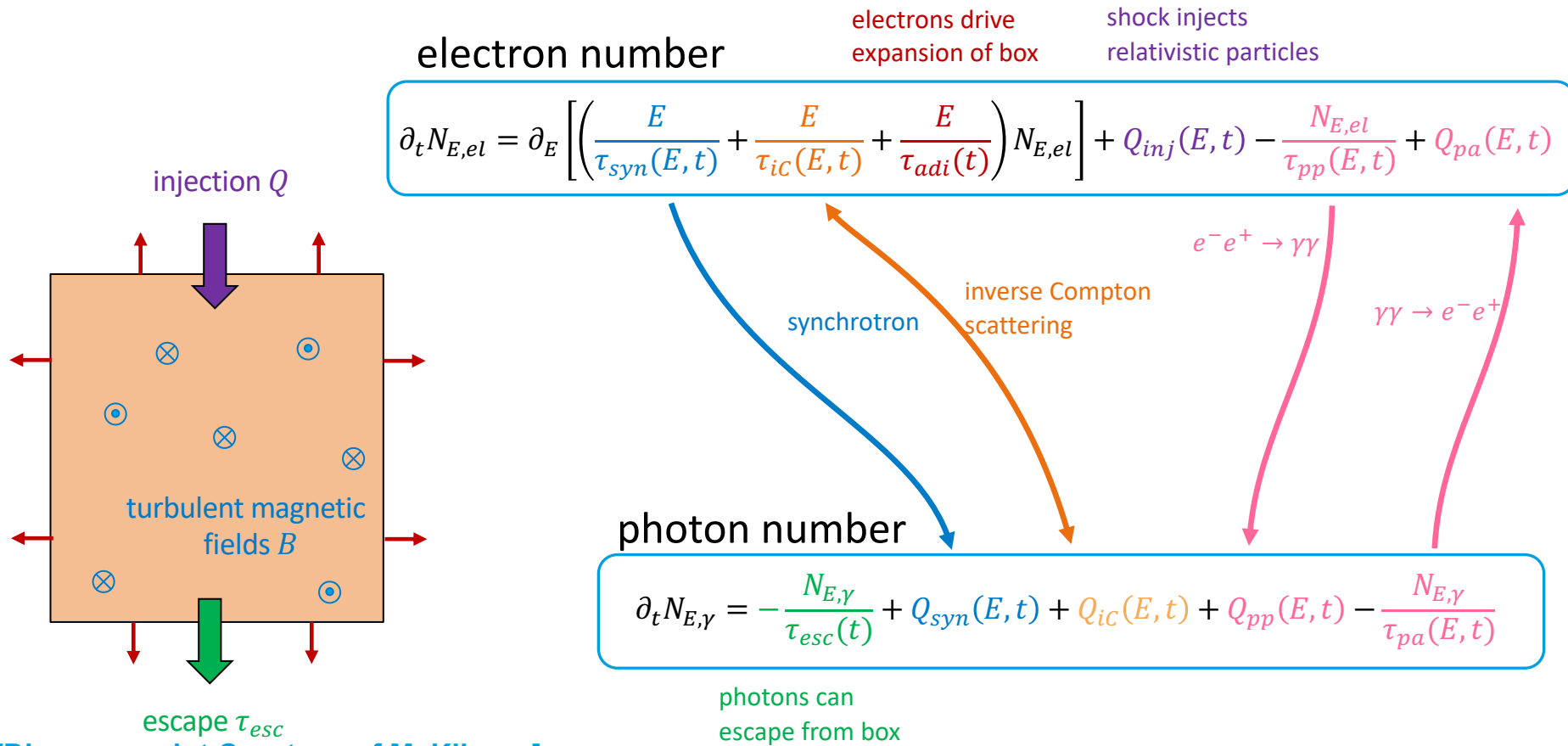
- Isotropisation is caused by magnetic turbulence, its rate is described by the scattering time, which in Larmor time units is η

$$t_{\text{scat}} = \eta \frac{R_{\text{lar}}}{c}$$

- Scattering agent velocity β dictates energy gain each crossing cycle

② η - key parameter which again we don't a priori know, but which we may probe with observations

One Zone Model (Spectral)



[Diagram + plot Courtesy of M. Klinger]

Note the absence of spatial information in these transport equations

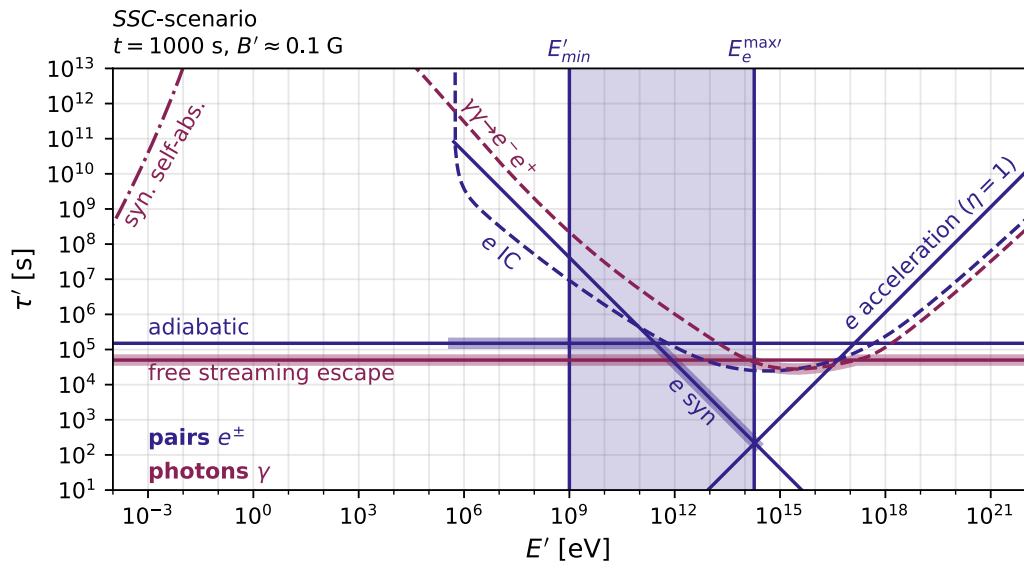
Electron Spectrum Produced in Sources

Steady state

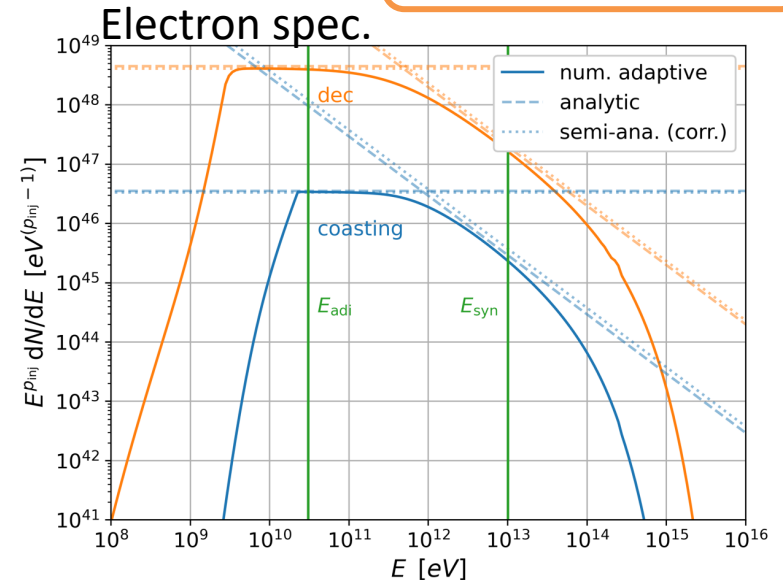
$$\frac{\partial \mathbf{n}_p}{\partial t} = -\nabla_{\mathbf{p}} \cdot \left(-\frac{\mathbf{p}}{\tau_{\text{loss}}(\mathbf{p})} \mathbf{n}_p \right) + \mathbf{Q}$$

$$\tau_{\text{loss}} = \left(\tau_{\text{adi}}^{-1} + \tau_{\text{sync}}^{-1} + \tau_{\text{IC}}^{-1} \right)^{-1}$$

$$\mathbf{n}_p \approx \mathbf{Q} \tau_{\text{loss}}$$

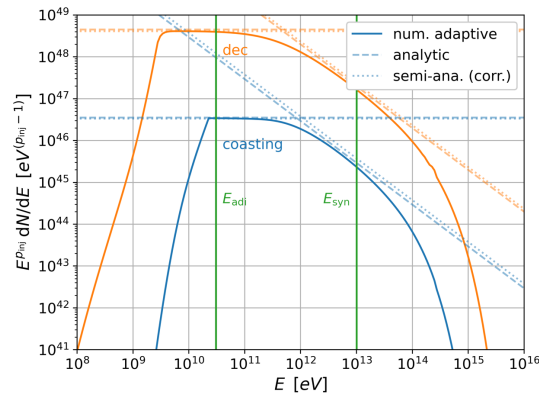


Andrew Taylor

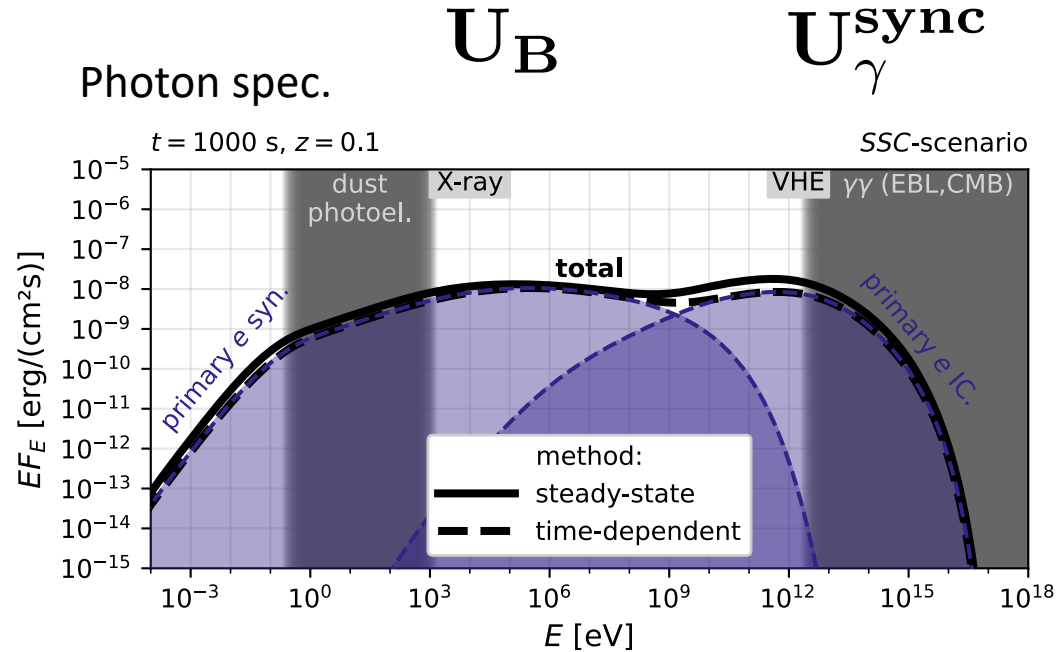


Afterglow GRB SED- Expected from SSC Model

Electron spec.



$$n_p \approx Q \tau_{\text{loss}}$$



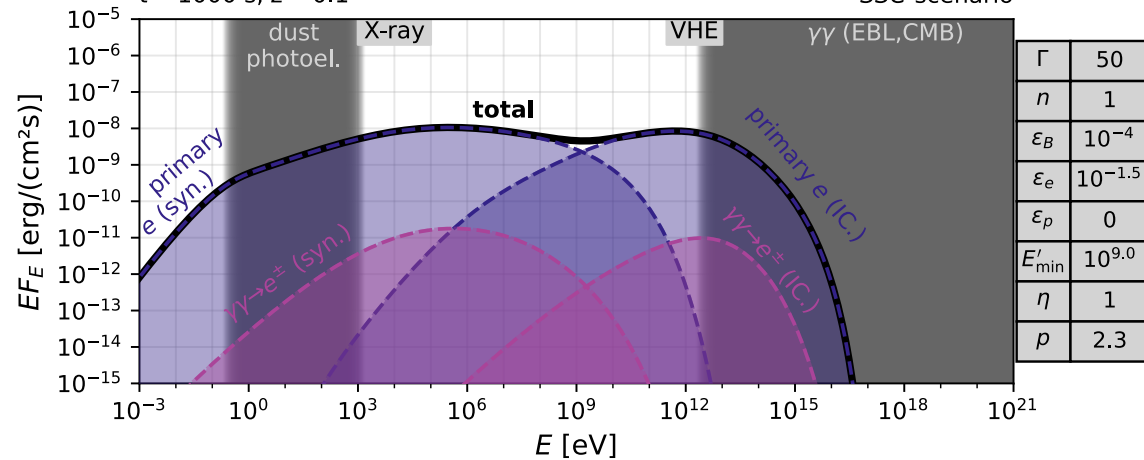
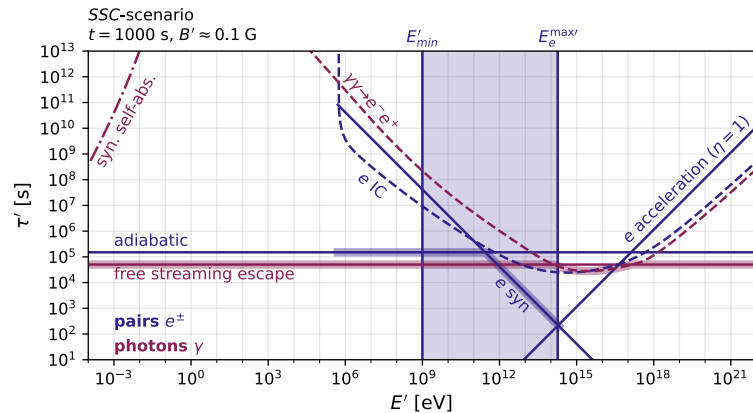
The "steady-state" approximation provides a reasonable description for the spectrum \rightarrow ie. \sim agrees with the full time-dependent result

Afterglow GRB SED- Expected from SSC Model

Photon spec.

$t = 1000 \text{ s}, z = 0.1$

SSC-scenario



Note- to get IC peak to sit at a comparable level to the synchrotron peak requires a “triple point” in the cooling time plot to exist

[Klinger et al. MNRAS 520 (2023)]

Note curvature of SSC spectrum in the VHE band

Where is the signature of ϵ^{th} ? results above/in most others works, set the thermal particles components to 0, is this realistic?

Is $\eta=1$ realistic?

Electron Acceleration with Cooling

$$t_{\text{acc}} = \eta \frac{R_{\text{lar}}}{c\beta^2}$$

$$t_{\text{cool}} = \frac{9}{8\pi\alpha} \left(\frac{U_{\text{Bcrit}}}{U_{\text{B}}} \right) \left(\frac{h}{E_e} \right)$$

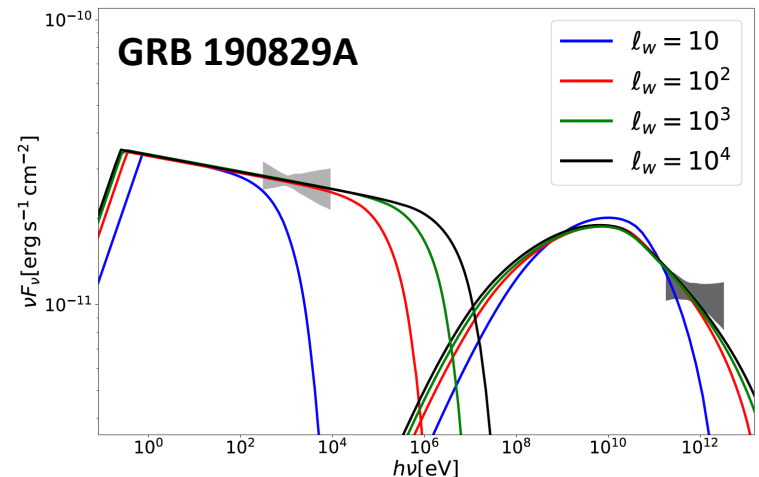
$$B_{\text{crit}} = 4 \times 10^{13} \text{ G}$$

$$E_e^{\text{max}} = \left(\frac{\eta^{-1/2}}{\alpha^{1/2} (B/B_{\text{crit}})^{1/2}} \right) m_e c^2$$

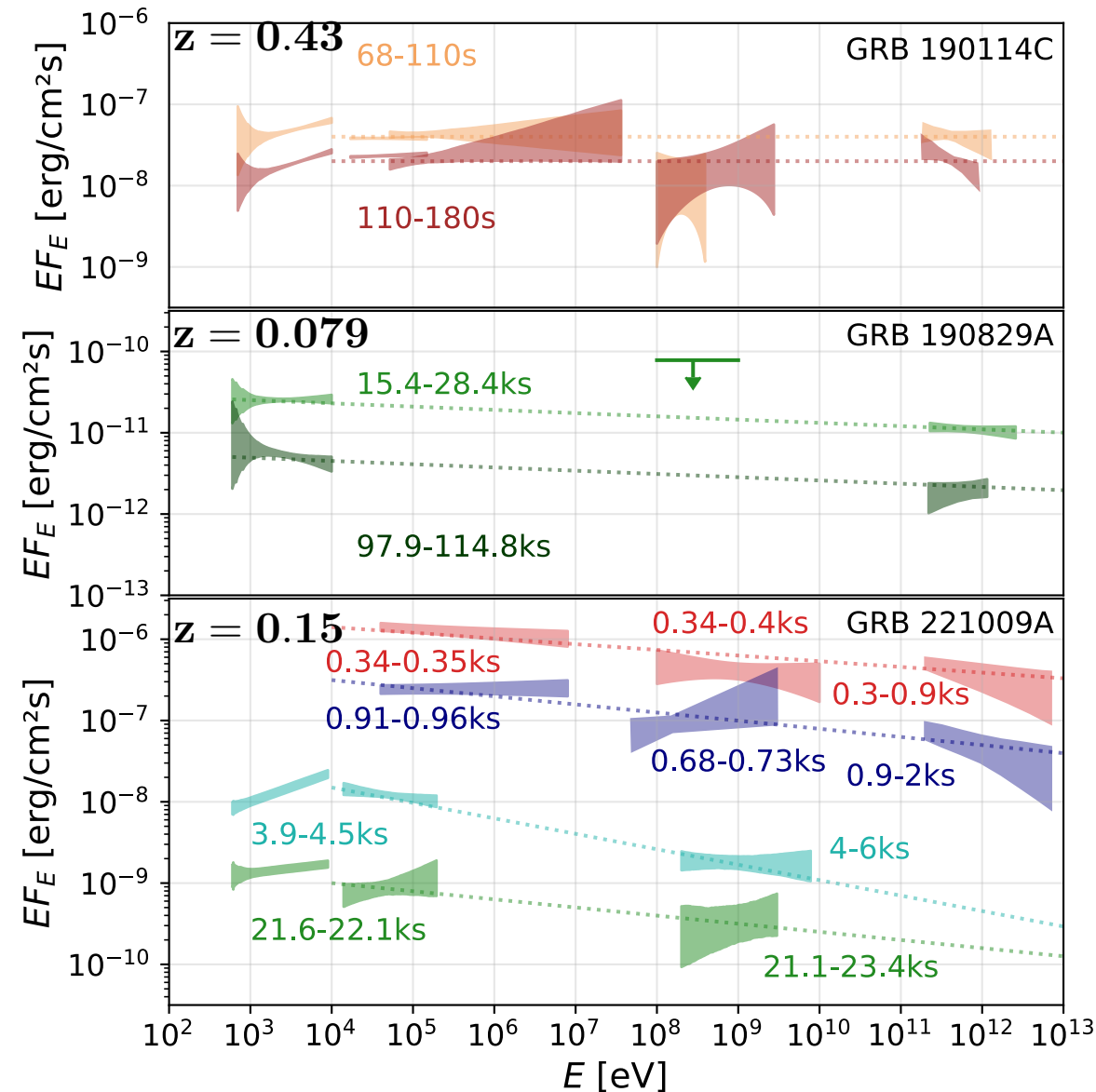
Maximum synchrotron energy tells us how efficient accelerator is!

$$E_{\gamma}^{\text{sync}} \approx \frac{9}{4} \eta^{-1} \beta^2 \frac{m_e}{\alpha}$$

[Huang et al. Ap J 925, (2022)]



VHE GRB SED- Lessons Learnt Since 2018



- Striking how flat the MWL photon spectra are!
- The SSC model predicts a curved spectrum which may be contradiction with these observations

[MAGIC Coll. Nature 2019]

[HESS Coll. Science 2021]

[LHAASO Coll., Science 2023]

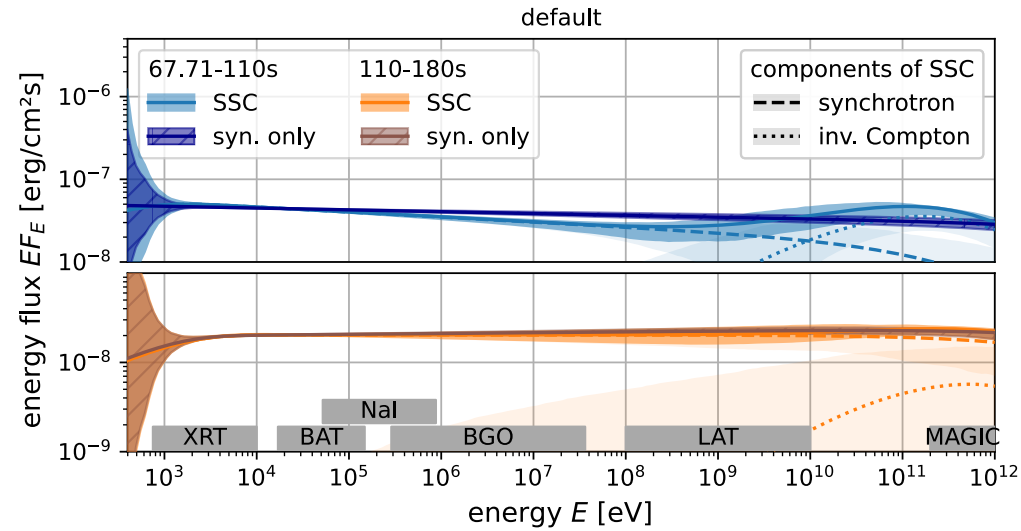
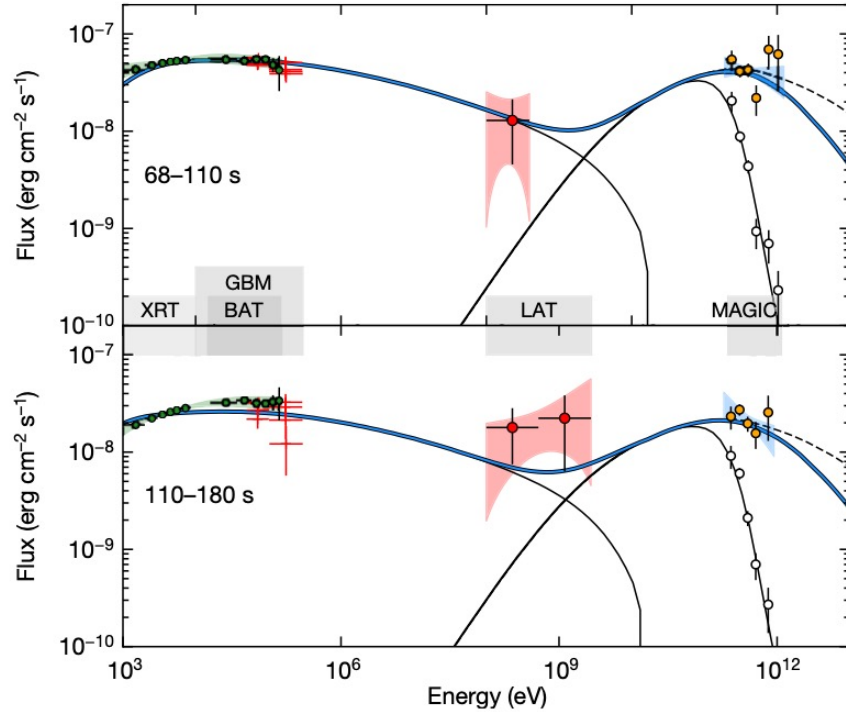
[Klinger et al. arxiv:2403.13902]

Statistical Tests- A Spectral Model Fit for GRB 190114C

[MAGIC Coll. Nature 2019]

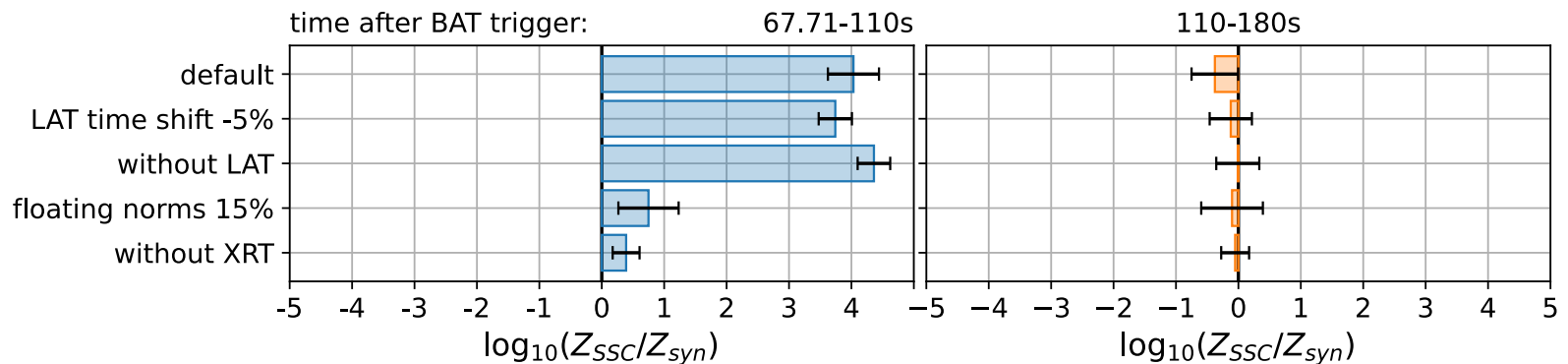
GRB 190114C

[Klinger et al. MNRAS 520 (2023)]

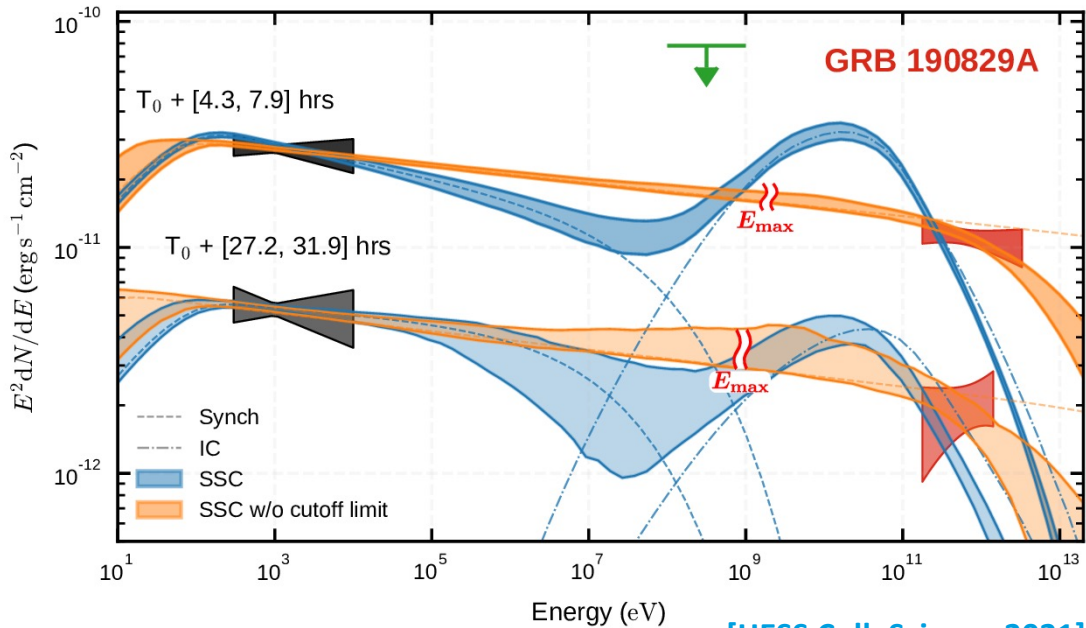


[Fermi+Swift. ApJ 890 (2020)]

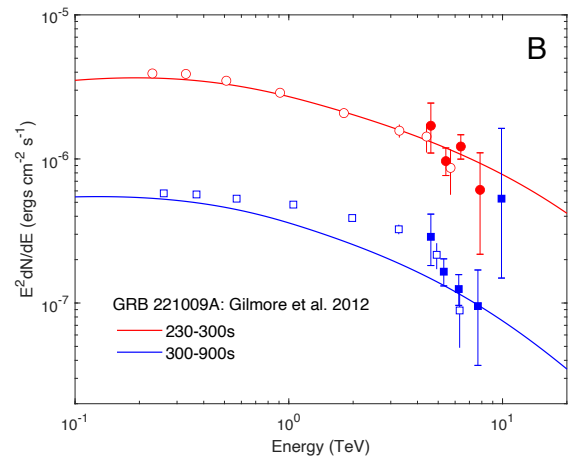
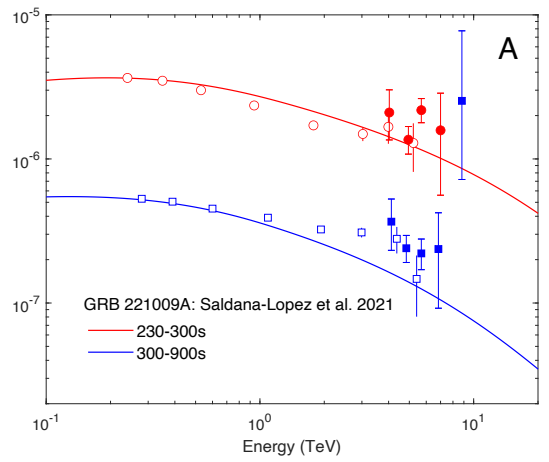
Bayes factor for new component



Statistical Tests- Spectral Model Fits other GRB



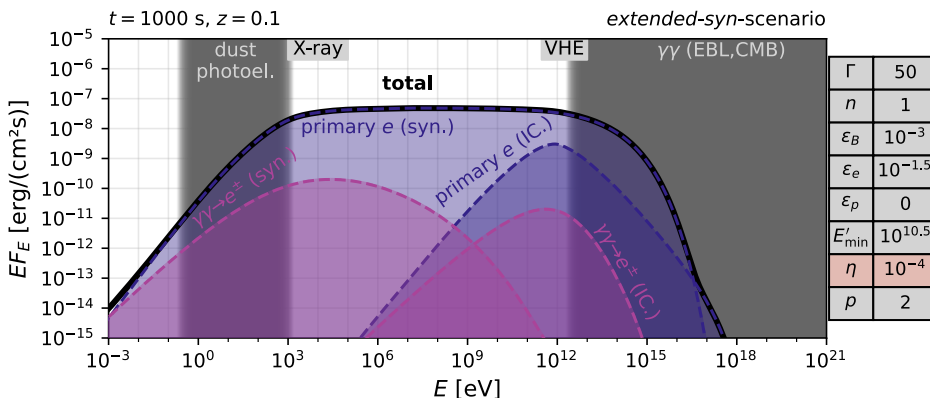
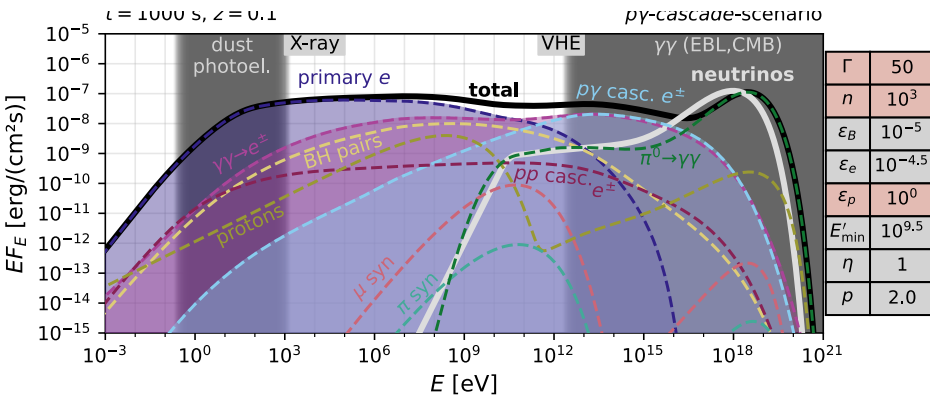
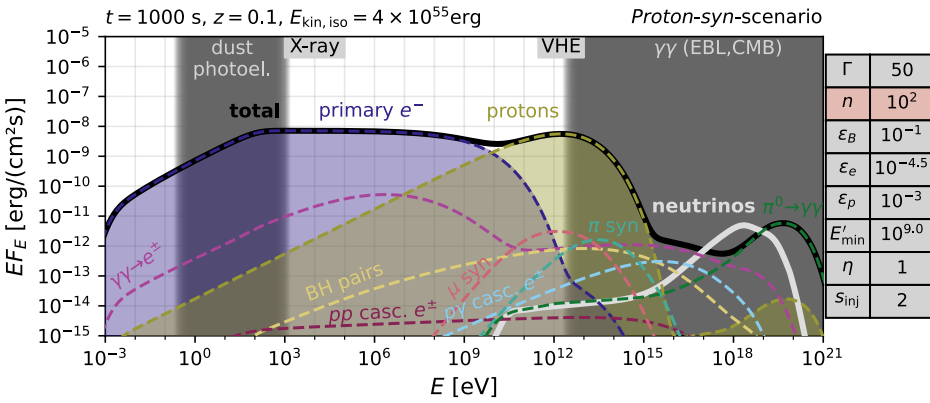
GRB 190829A
[15-28 ks]



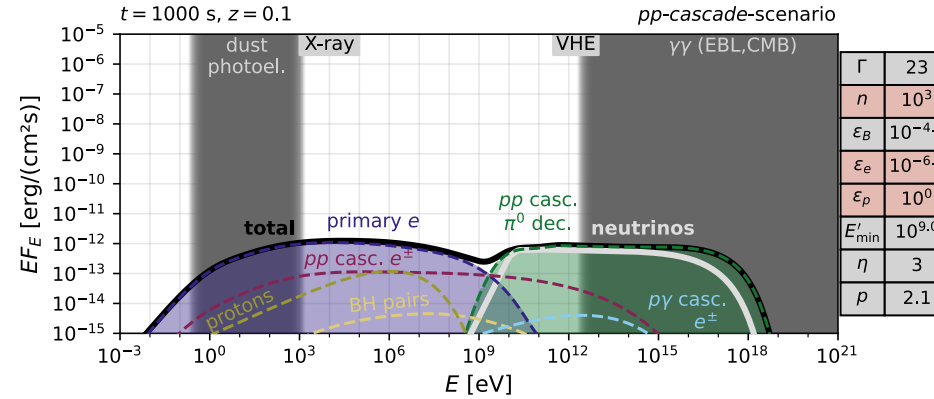
GRB 221009A
[0.2-0.9 ks]

[LHAASO Coll. Science 2023]

Alternative 1-Zone Scenarios?



Before raising the number of degrees of freedom, other parts of parameter space should first be explored



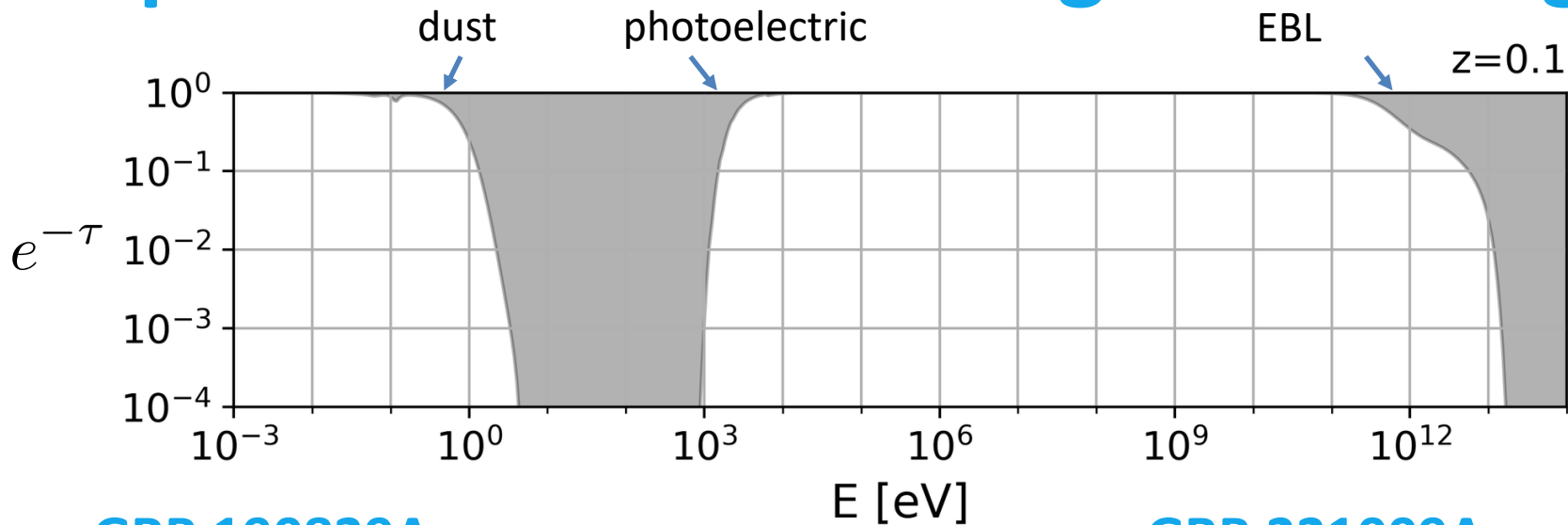
Each scenario requires rather extreme parameter values (see highlighted box)

[Klinger et al., arxiv:2403.13902

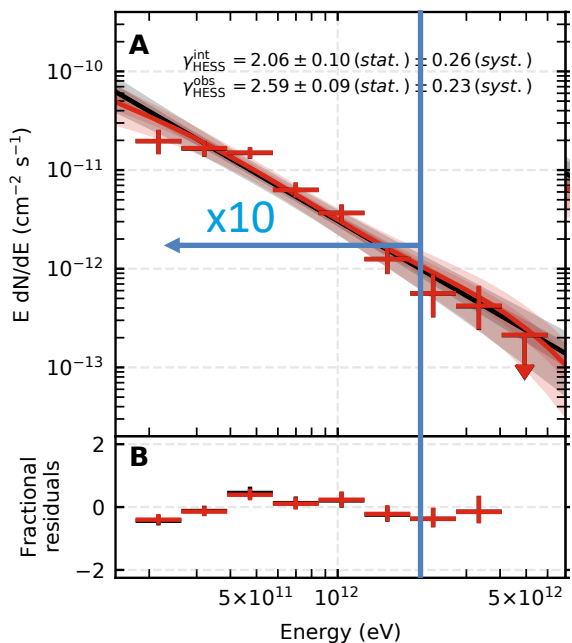
[Khangulyan et al., Ap. J. 914 (2021)]

[Isravel et al., Ap. J 955 (2023)]

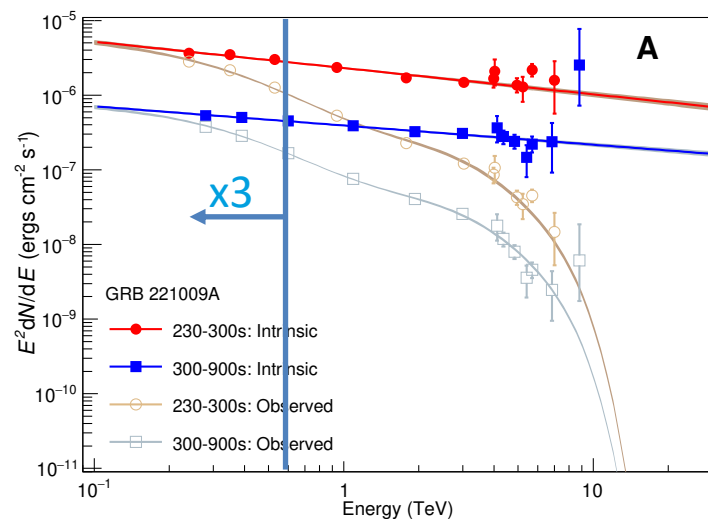
Importance of Minimising EBL Damage



GRB 190829A



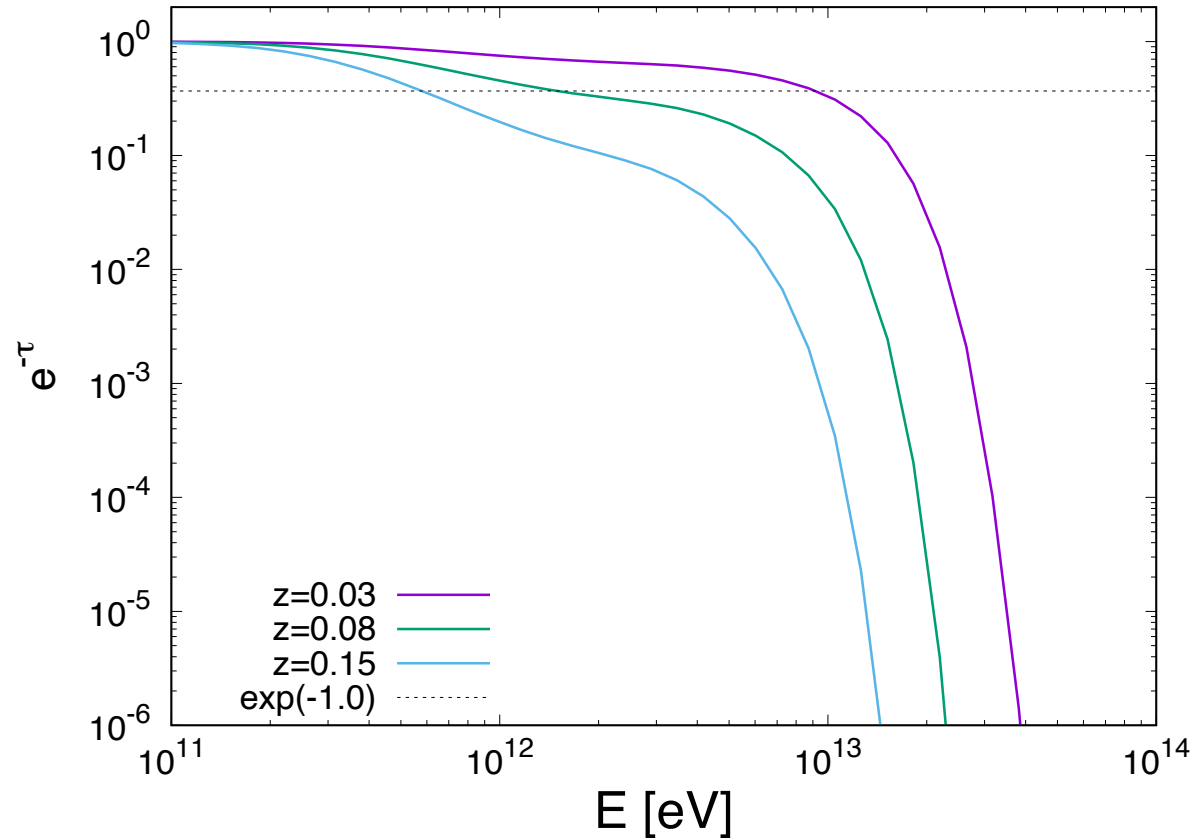
GRB 221009A



Key Phase Space for VHE GRB Detections?

Three key factors for GRB detection are apparent:

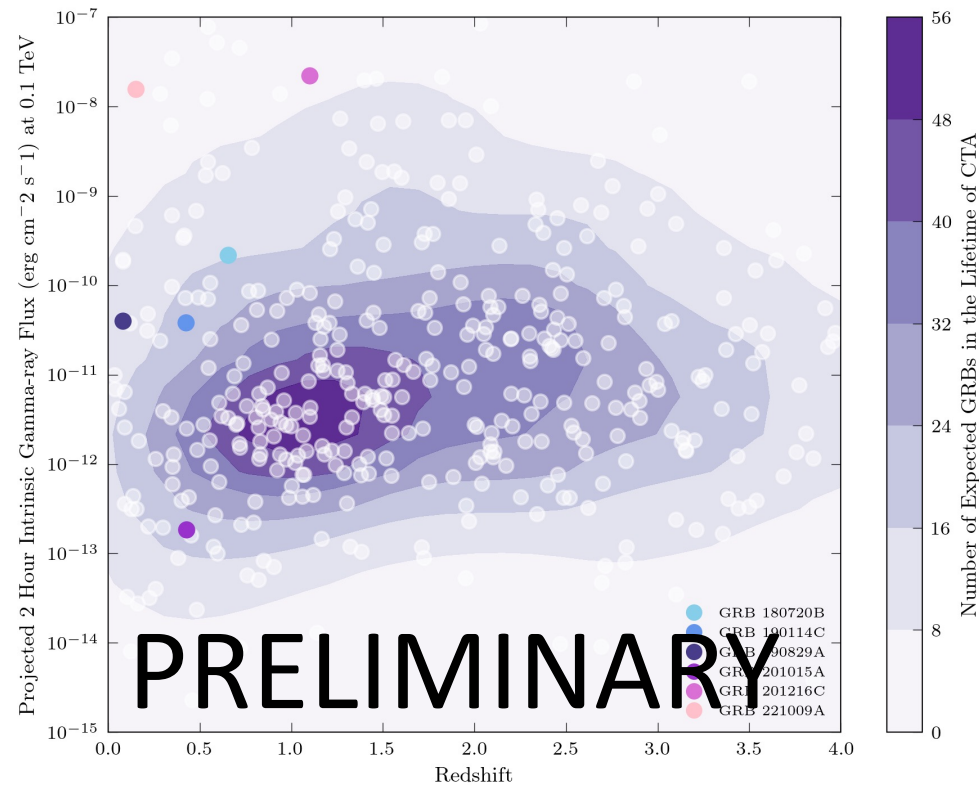
- **Locality** is crucial (EBL damage minimised)
- **Brightness** is crucial (allows detection at late times once Lorentz factor has decreased significantly)
- **Simultaneous MWL** coverage (in keV to multi-TeV energy range) is crucial



Within Swift's lifetime (~ 20 years so far), the most local GRB was $z=0.03$

DESY. Spectra up to 10 TeV, with small EBL effects, may potentially be probeable

Prospective Rates for Testing the GRB Emission Process with CTA



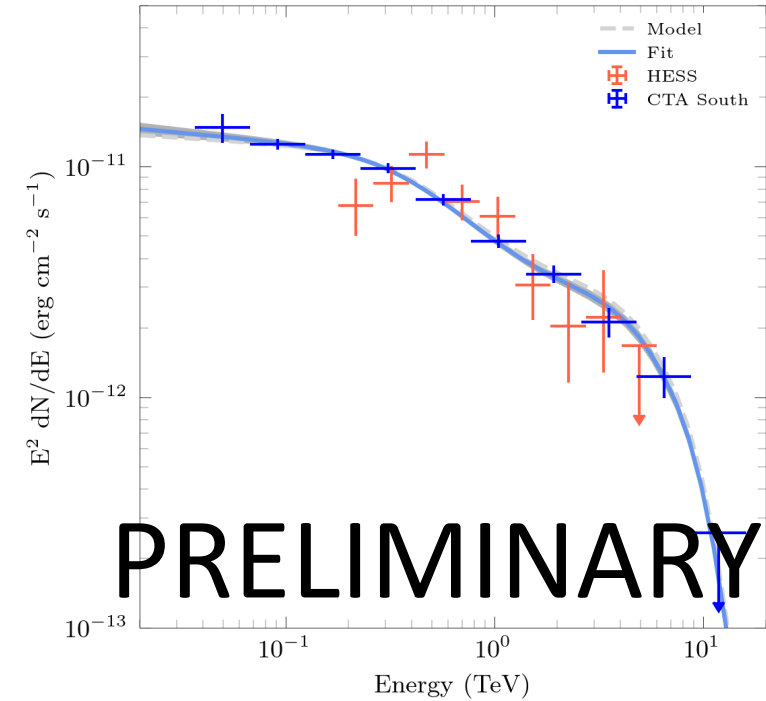
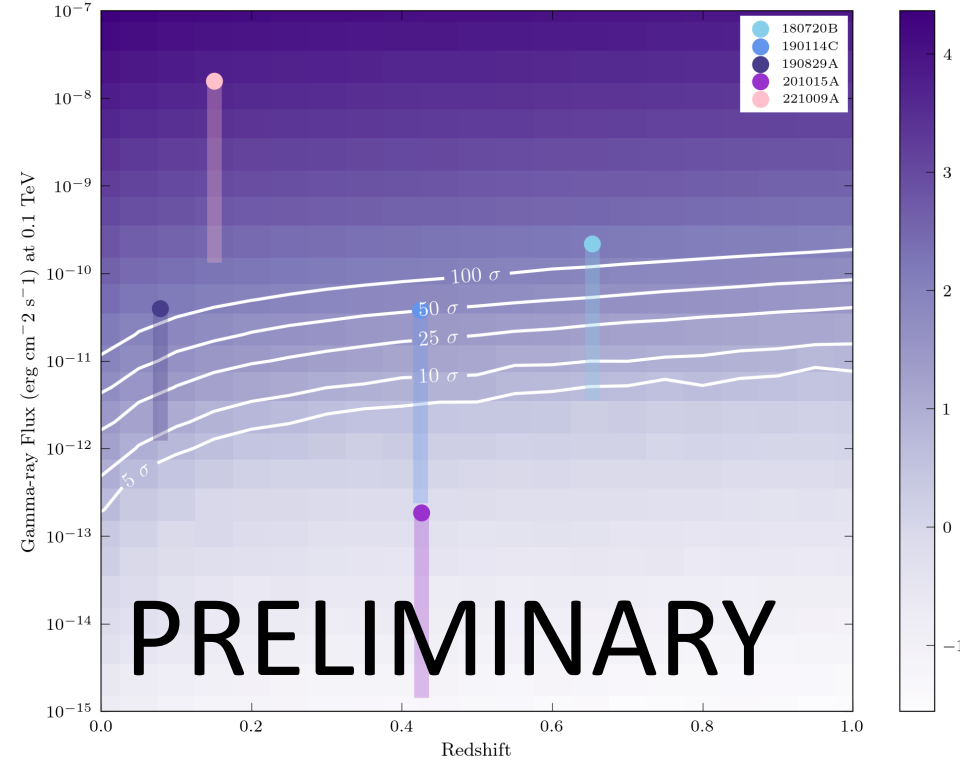
[Provided by J. Pfeil and D. Parsons]

- Future GRBs for providing a stronger probe of the spectral emission model must be **local** and have **bright** afterglows
- For **CTA**, a rate of up to 4 yr^{-1} is possible to expect, consistent with other estimates
[Ashkar et al., ApJ 964 57]
- However, of these events, the **local** subset of particular interest will be rare ($< 0.25 \text{ yr}^{-1}$)

A GRB 190829A Like Event for CTA

Obs. assumed to start at T0 + 2hrs for 5 hrs

Night 1/
3.6h obs. time
= HESS observation time



[Provided by J. Pfeil and D. Parsons]

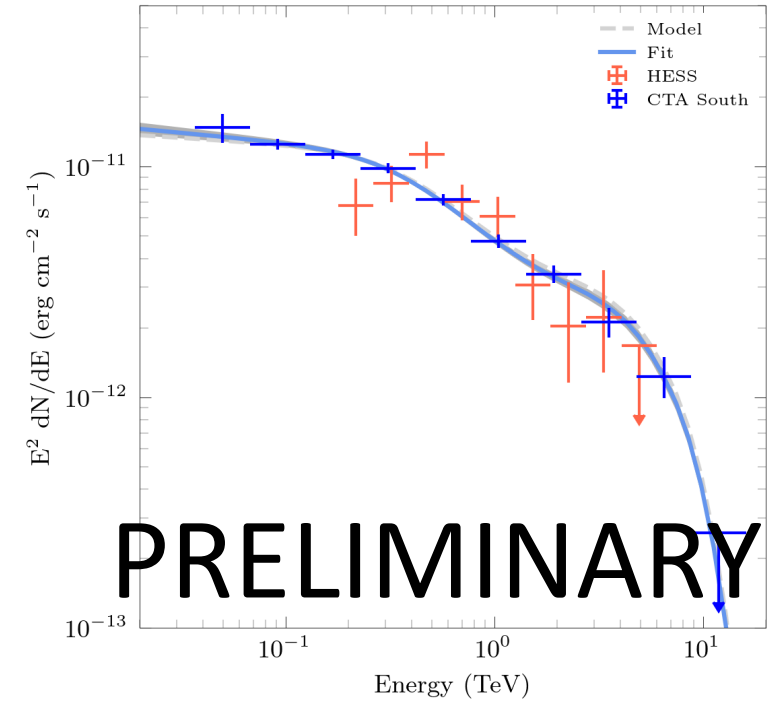
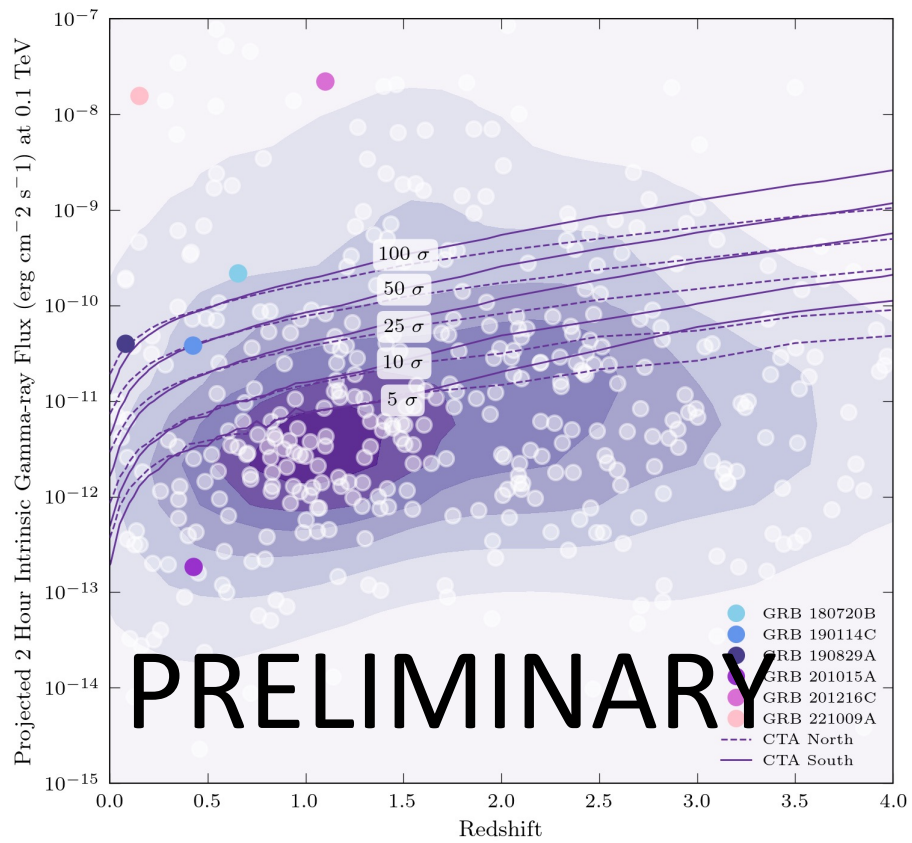
EBL Attenuated Power Law		
Fit Parameter	HESS	CTA South
γ^{int}	$2.06 \pm 0.10 \pm 0.26$	2.09 ± 0.02

Conclusions

- ◆ Fast (rel.) shocks in the ejecta of GRB jets appear to operate as particle acceleration machines
- ◆ Synchrotron emission from long GRB can tell us directly how efficient these sources operate as cosmic ray accelerators
- ◆ We are now (since 2018) starting to probe the very high energy (TeV) gamma-ray emission from GRB, providing new insights into the source environment
- ◆ Whether a new component in the GRB spectrum is present remains unclear—curiously, the VHE GRB detections appear compatible with a continuation of the synchrotron emission beyond the expected supposed theoretical limit
- ◆ For CTA to answer this emission process question, the catching of extremely local GRB events will play a crucial role

Prospects for Testing the GRB Emission Process with CTA

Night 1/
3.6h obs. time
= HESS observation time



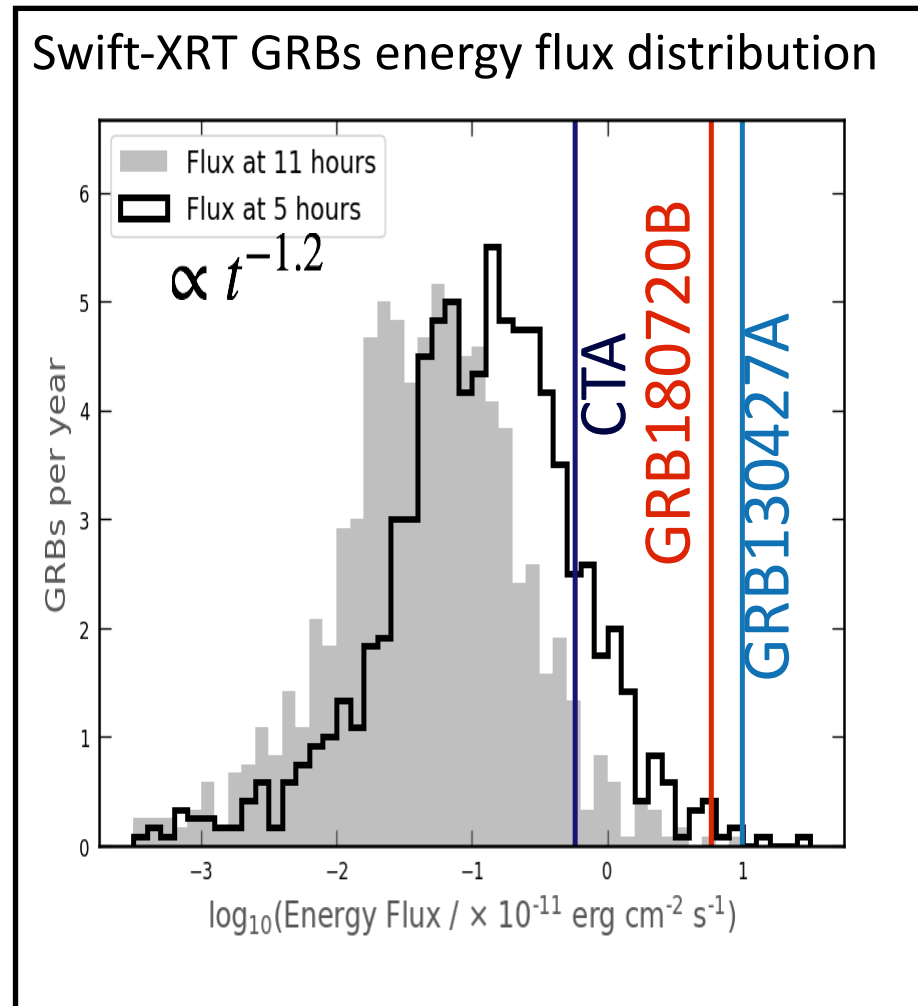
EBL Attenuated Power Law

Fit Parameter	HESS	CTA South
γ^{int}	$2.06 \pm 0.10 \pm 0.26$	2.09 ± 0.02

[Provided by J. Pfeil and D. Parsons]

Prospects for Future Observatories

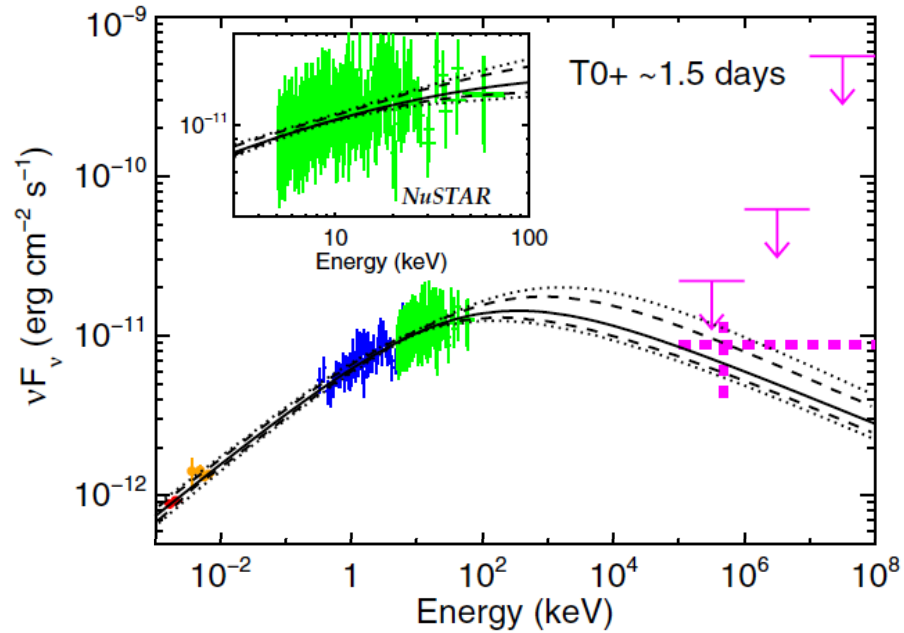
- CTA to have ~ 10 times better sensitivity than present ACTs
- Will be able to detect flux over many decades in time with detailed spectra information.
- Boost the detection of GRBs at VHE.
 - ~ 3 GRBs per year at 11 hours after burst.
 - ~ 11 GRBs per year at 5 hours after burst



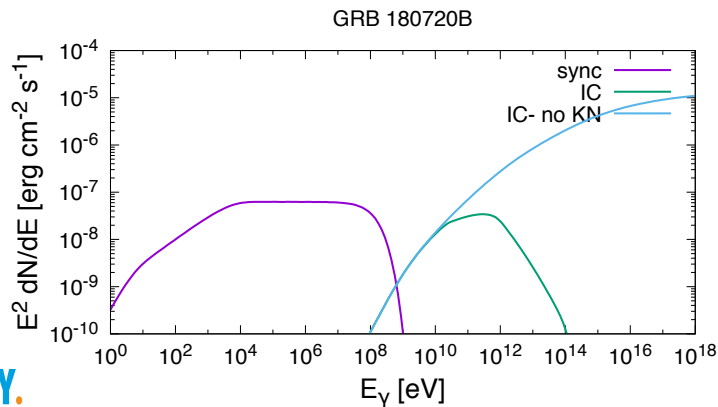
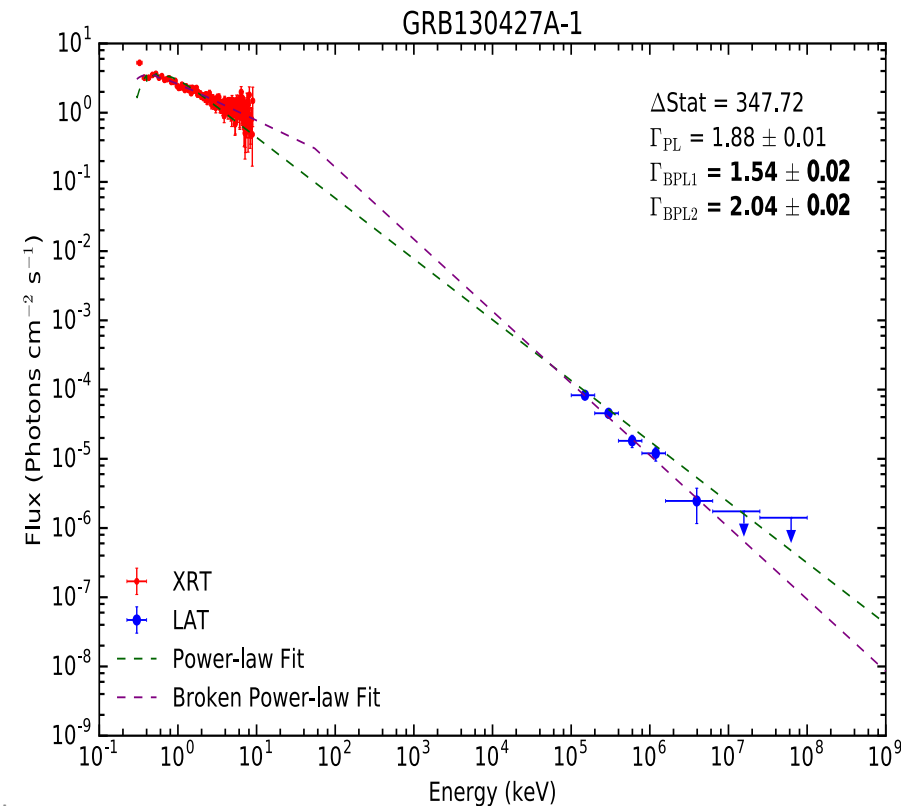
Ruiz-Velasco+ (1st CTA symposium)
HESS Collaboration *Nature* **575**, 464–467 (2019)

No Synchrotron Cutoff of GRB 130427A Seen in X-rays and Gamma-Rays

[Kouveliotou et al., ApJL 779 (2013)]

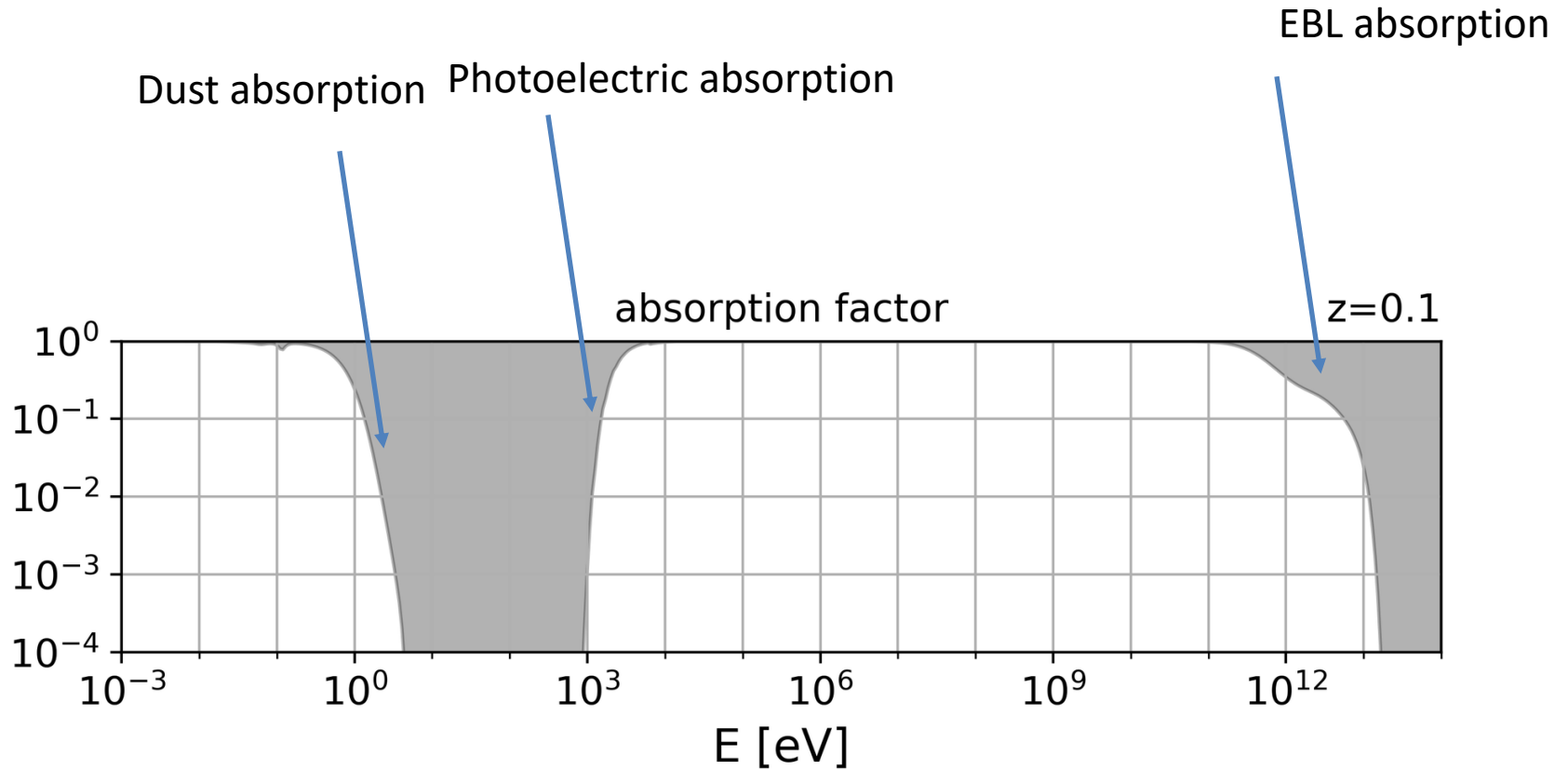


[Ajello et al., ApJ 863 138 (2018)]

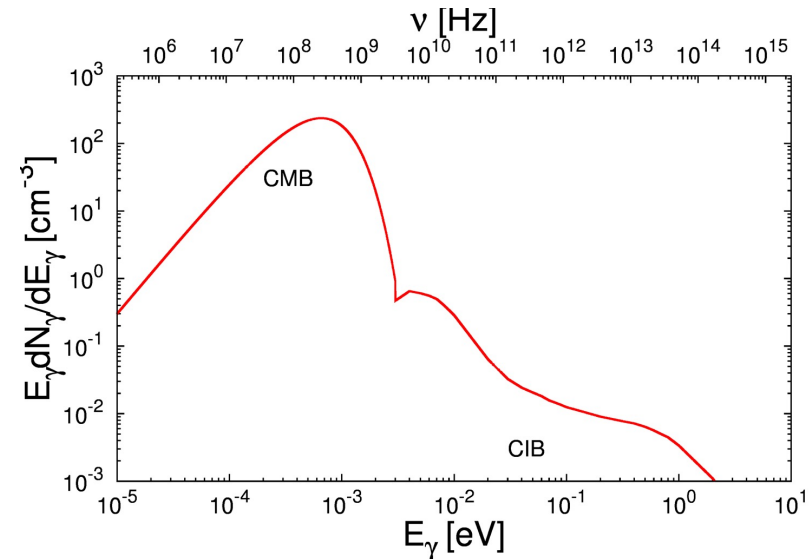
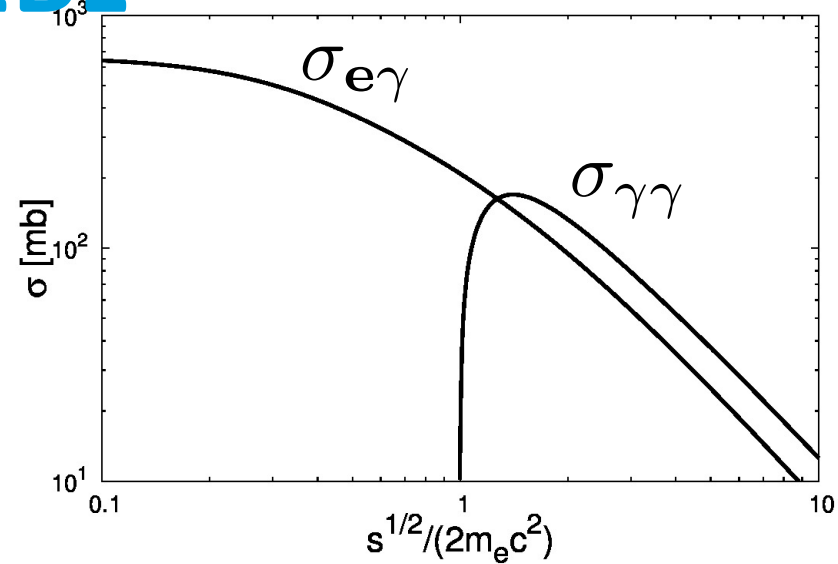
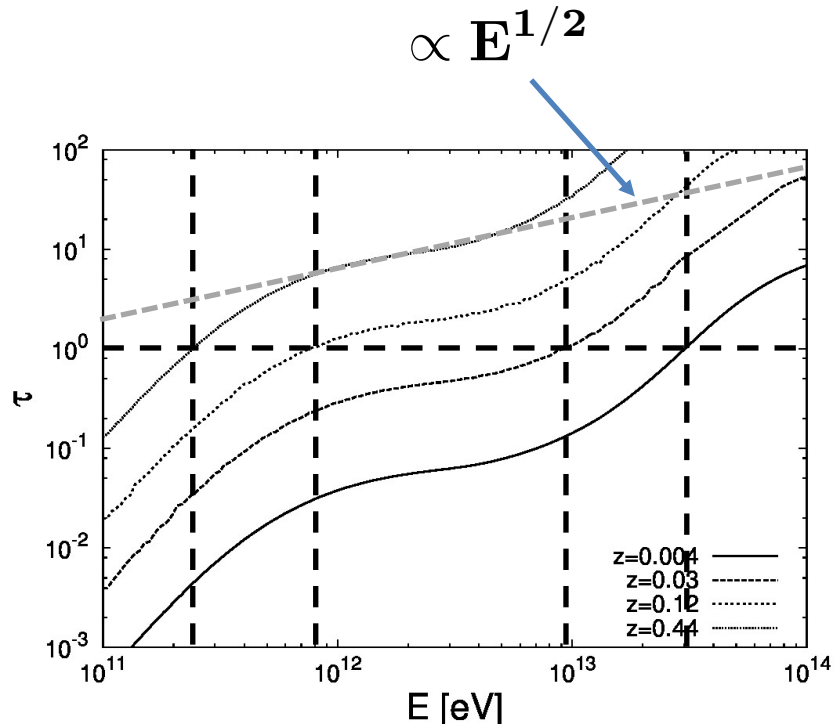


The Observational Challenges for GRBs

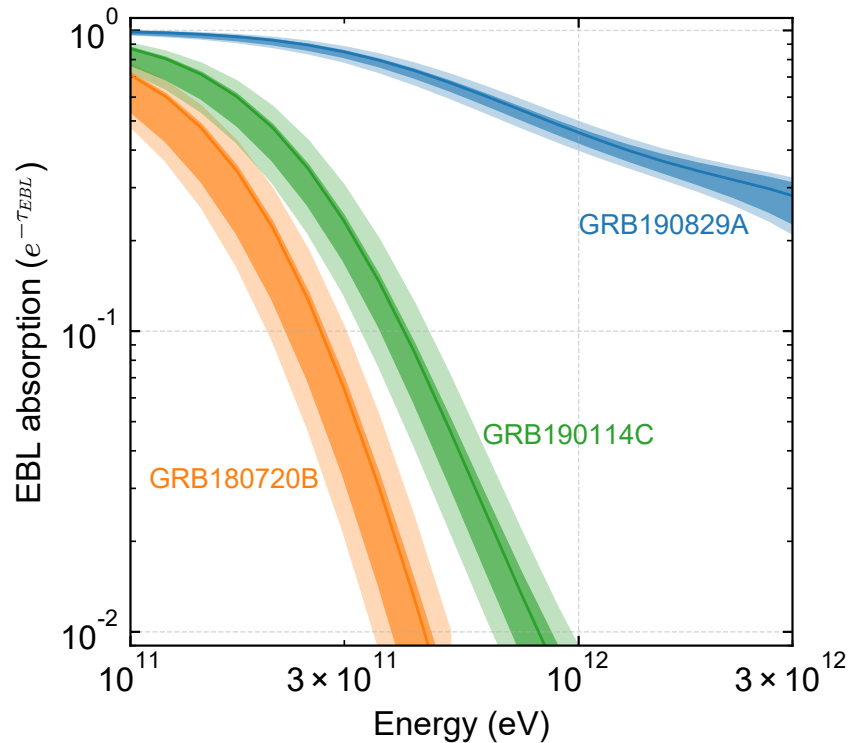
Absorption!



Attenuation through Pair Production on the EBL



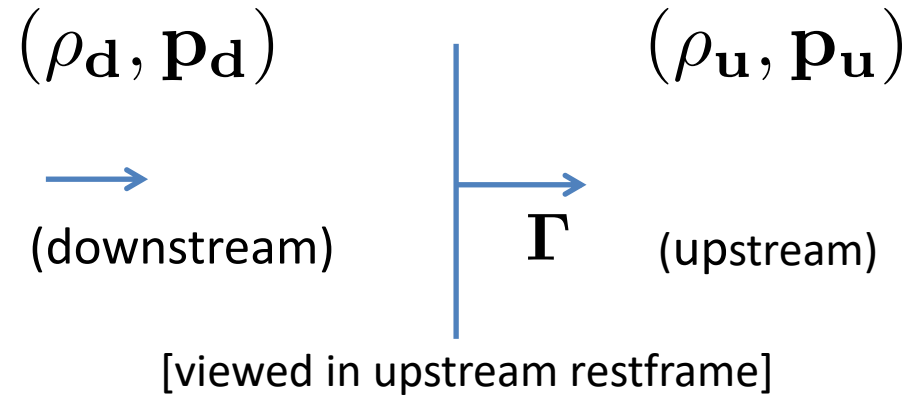
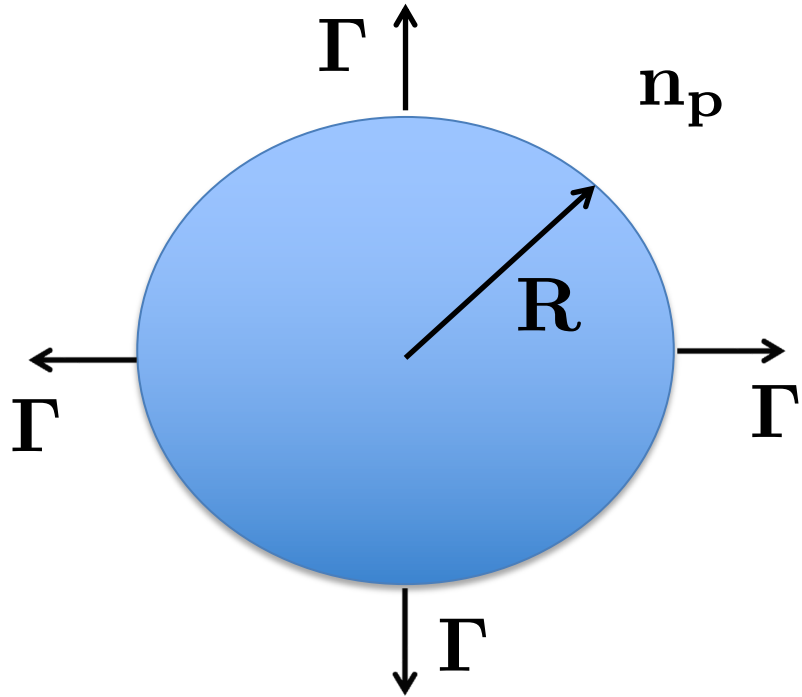
Energy Spectrum Information



The effect of the EBL on the (optically thin) attenuation for a nearby ($z=0.08$) source for $E_\gamma < 6$ TeV is a softening of the spectrum by around $\Delta\Gamma \approx 0.5$, starting around 250 GeV.

[HESS- A. Taylor, et al., Science 2021]

Origin of Temporal Decay Structure



Assuming η_γ is constant in time.....

$$\frac{L_{\text{sync}}^{\text{iso}}}{4\pi\Gamma^2 R^2 c} = \epsilon_{\text{rad}} \Gamma^2 n_p m_p c^2$$

$$\Gamma \propto t^{-3/8} \quad R \propto t^{1/4}$$

$$L_{\text{sync}}^{\text{iso}} \propto t^{-1}$$

Hadronic Particle Acceleration in Sources

$$\frac{\partial n_{\mathbf{p}}}{\partial t} = -\nabla_{\mathbf{p}} \cdot \left[\frac{\mathbf{p}}{\tau_{\text{acc}}(\mathbf{p})} n_{\mathbf{p}} - \frac{\mathbf{p}}{\tau_{\text{loss}}(\mathbf{p})} n_{\mathbf{p}} \right] - \frac{n_{\mathbf{p}}}{\tau_{\text{esc}}(\mathbf{p})} + Q$$

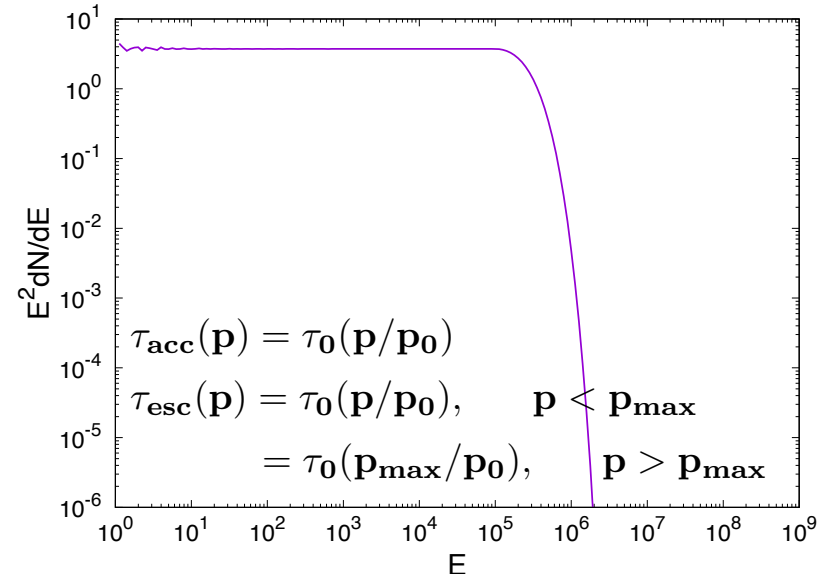
Steady state

No losses

Delta injection

$$n_{\mathbf{p}} = Q \left(\frac{\mathbf{p}}{\mathbf{p}_0} \right)^{-\left(1 + \frac{\tau_{\text{acc}}}{\tau_{\text{esc}}}\right)}$$

Note- shock acceleration is not the only acceleration process on the block

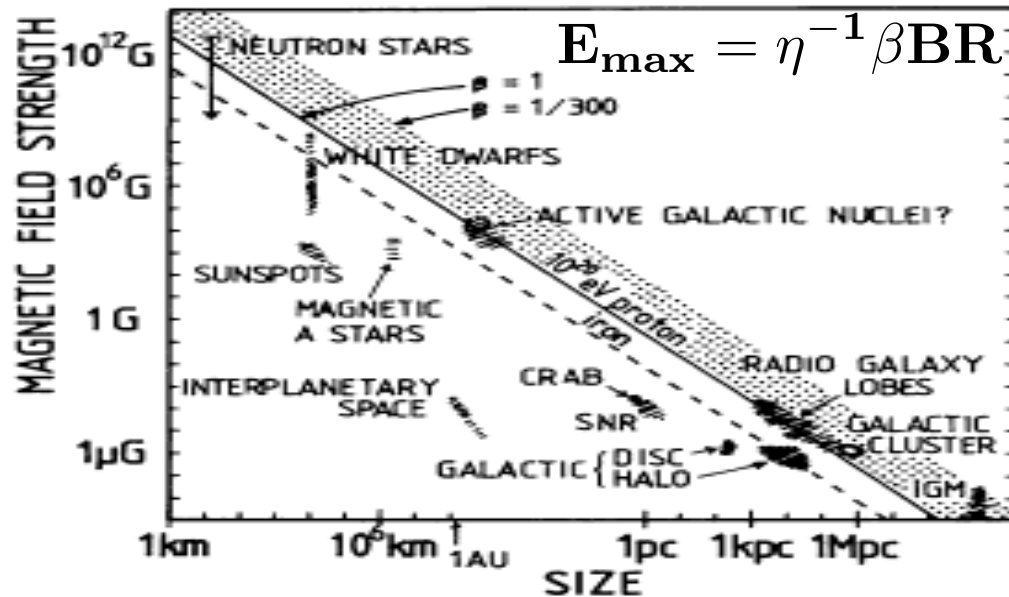


Cosmic Ray Source Requirements

$$t_{\text{acc}} = \eta \frac{R_{\text{lar}}}{c\beta^2}$$

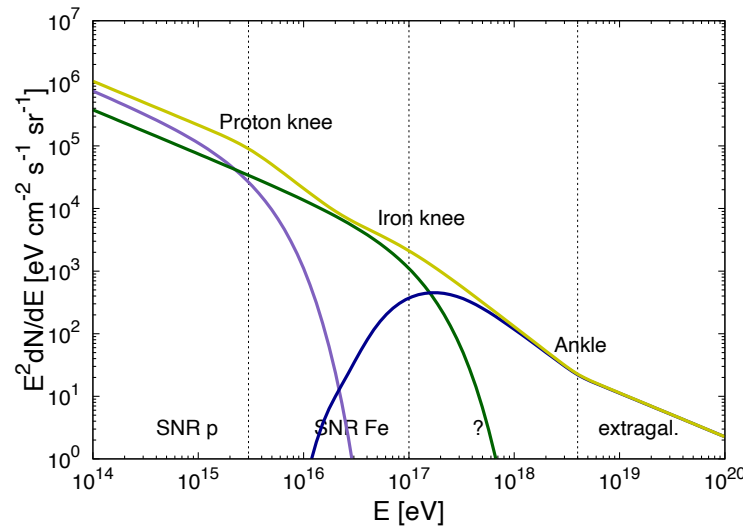
$$t_{\text{esc.}} = \frac{R}{c\beta}$$

[AM Hillas (1984)]

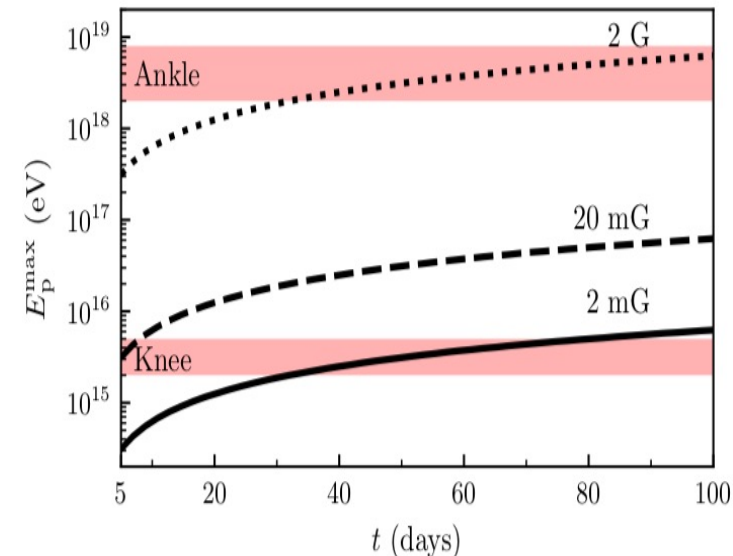


Not many objects appear capable of accelerating cosmic rays up to EeV energies. Blackhole related phenomena seem most promising- **AGN** and **GRB**

GRB Outflows as a Cosmic Ray Sources

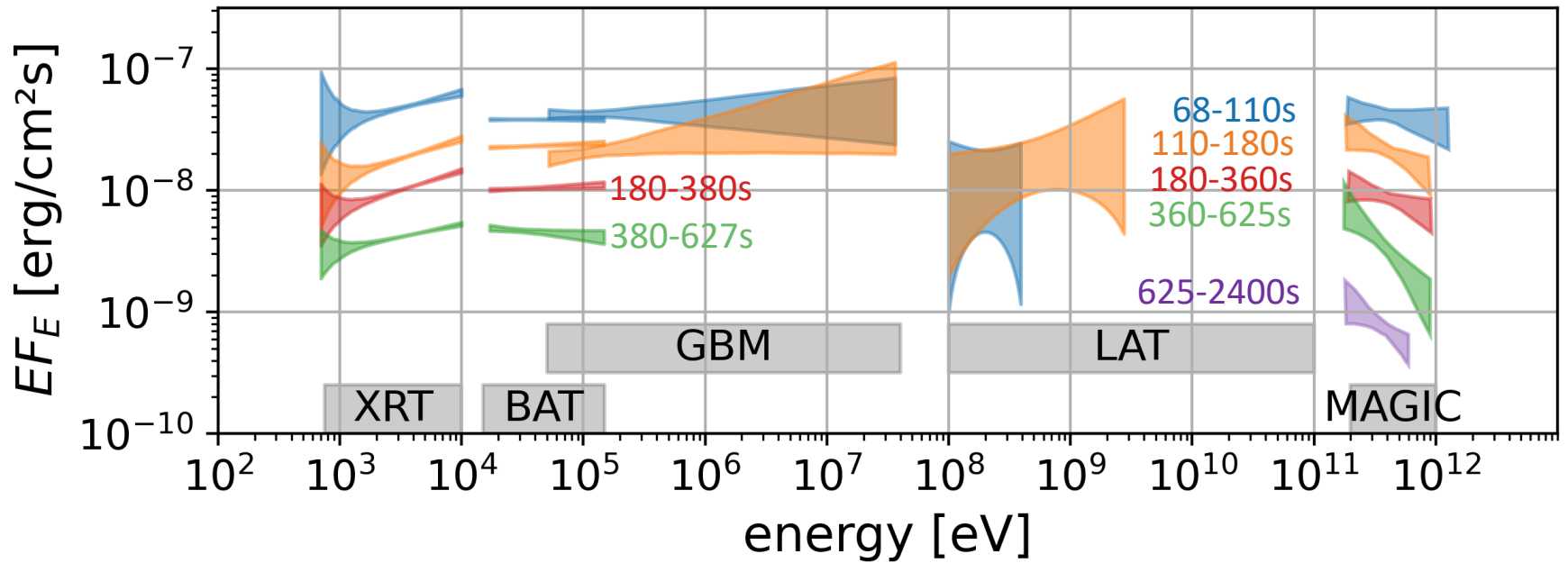


- As the source expands, **CRs** can be accelerated to energies between the **knee and the ankle**
- If the B -field is as large as $\sim G$ \rightarrow possibility of **UHECRs**



[X. Rodrigues, A. Taylor, et al., ApJ 2019]

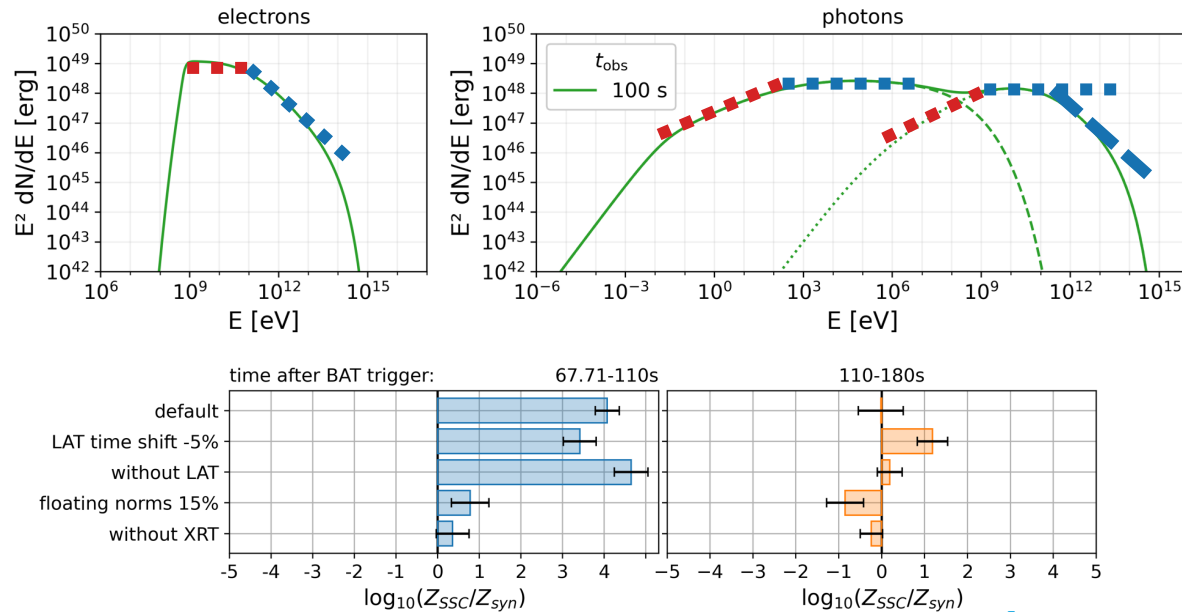
GRB 190114C (Detected by MAGIC)



[Nature 575, 459-463 (2019)]

- remarkably flat over 9 orders of magnitude in energy!

Evidence for a New Component?

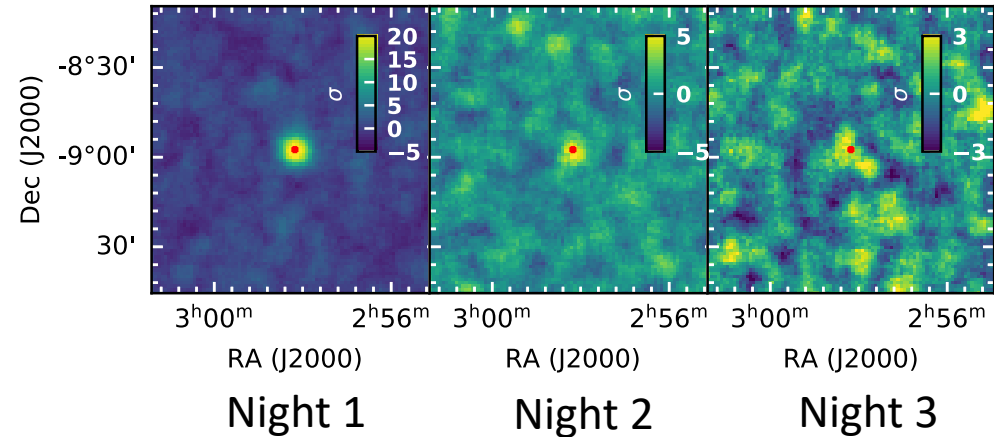
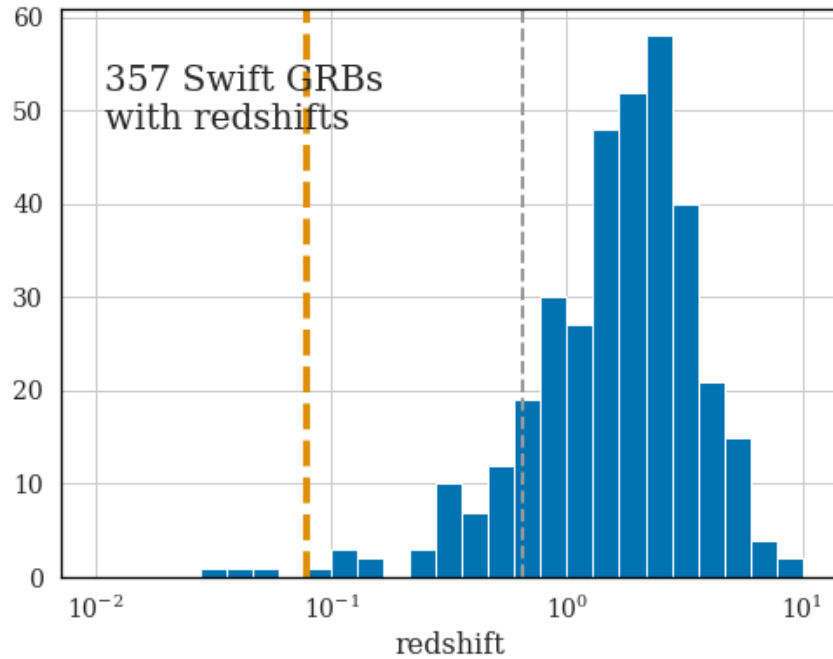


[M. Kinger et al., MNRAS 501 2023]

- SSC spectra are mirroring a smoothly BPL electron distribution
- We need more **bright, nearby** GRBs (without moonlight!)
- GRB 190114C shows no clear evidence for the onset of a new component

HESS Detection of GRB 190829A

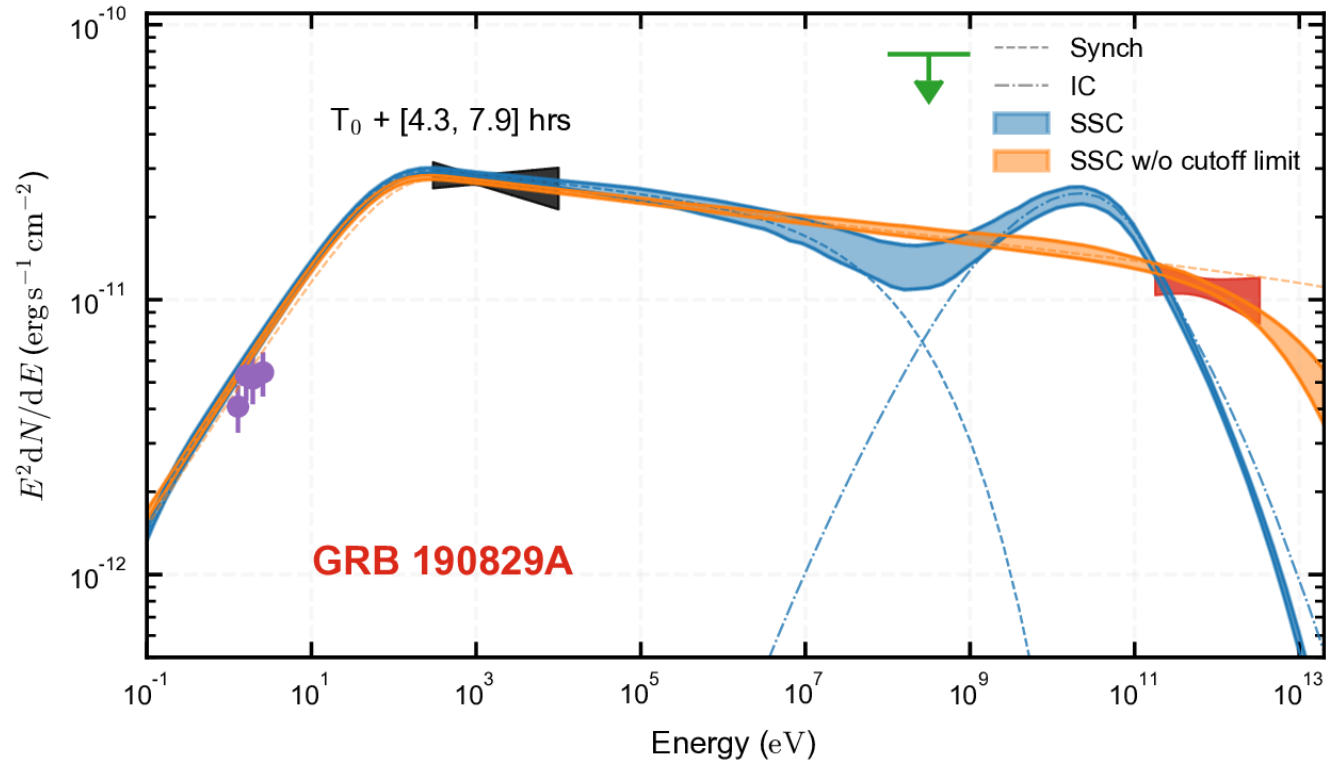
First detection of a GRB in VHE band for multiple nights



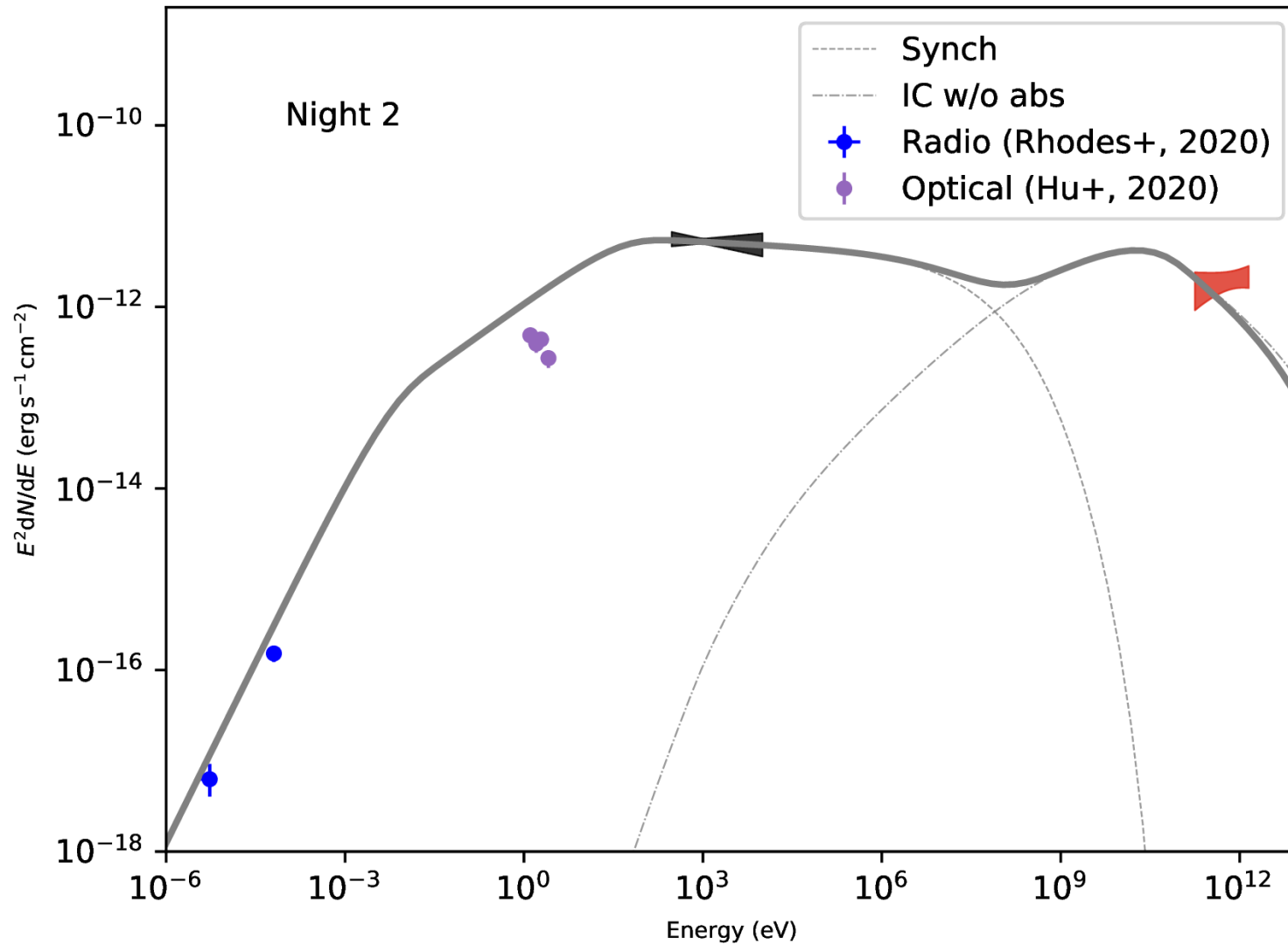
[HESS- A. Taylor, et al., Science 2021]

$$t_{90}^{\text{GBM}} \sim 60 \text{ s}, \quad t_{90}^{\text{BAT}} \sim 60 \text{ s}$$
$$z = 0.078$$

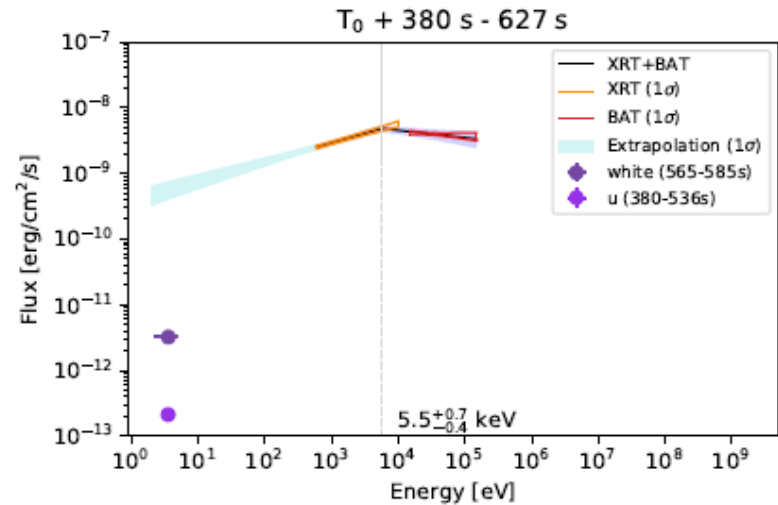
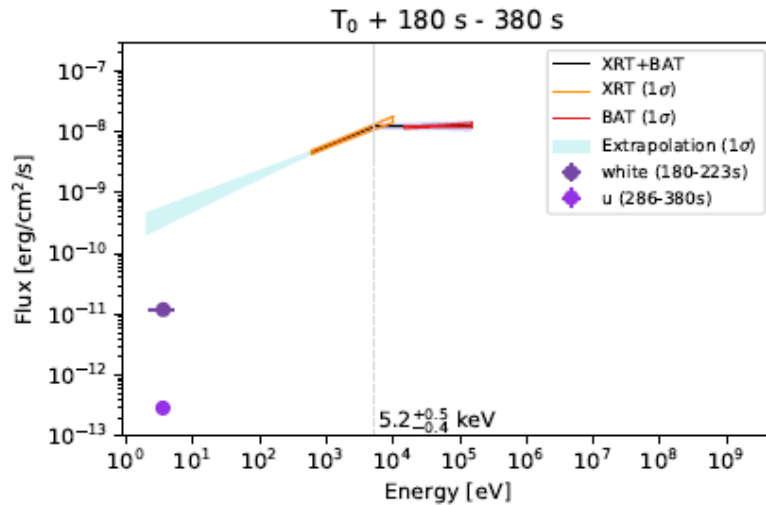
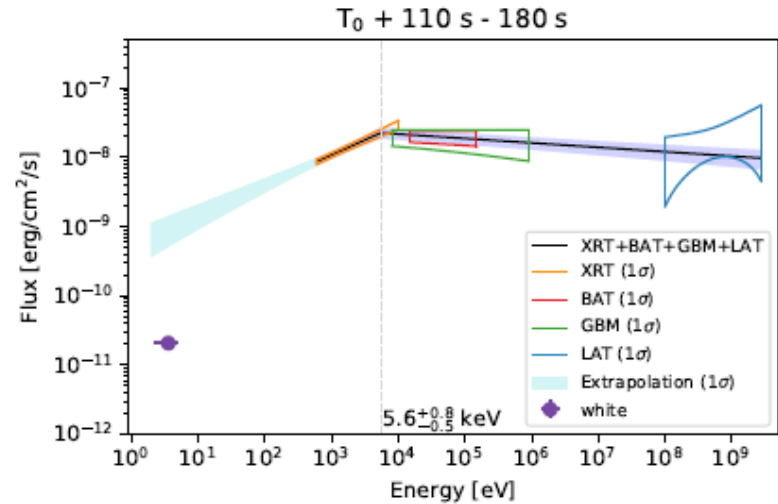
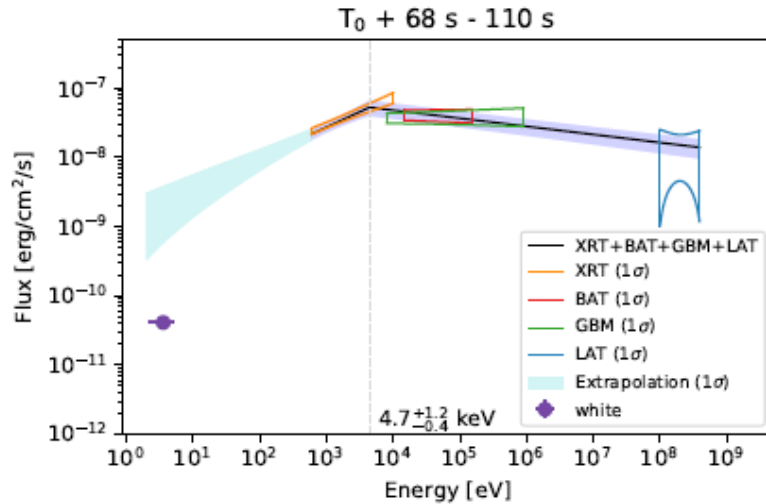
GRB 190829A- Optical Data



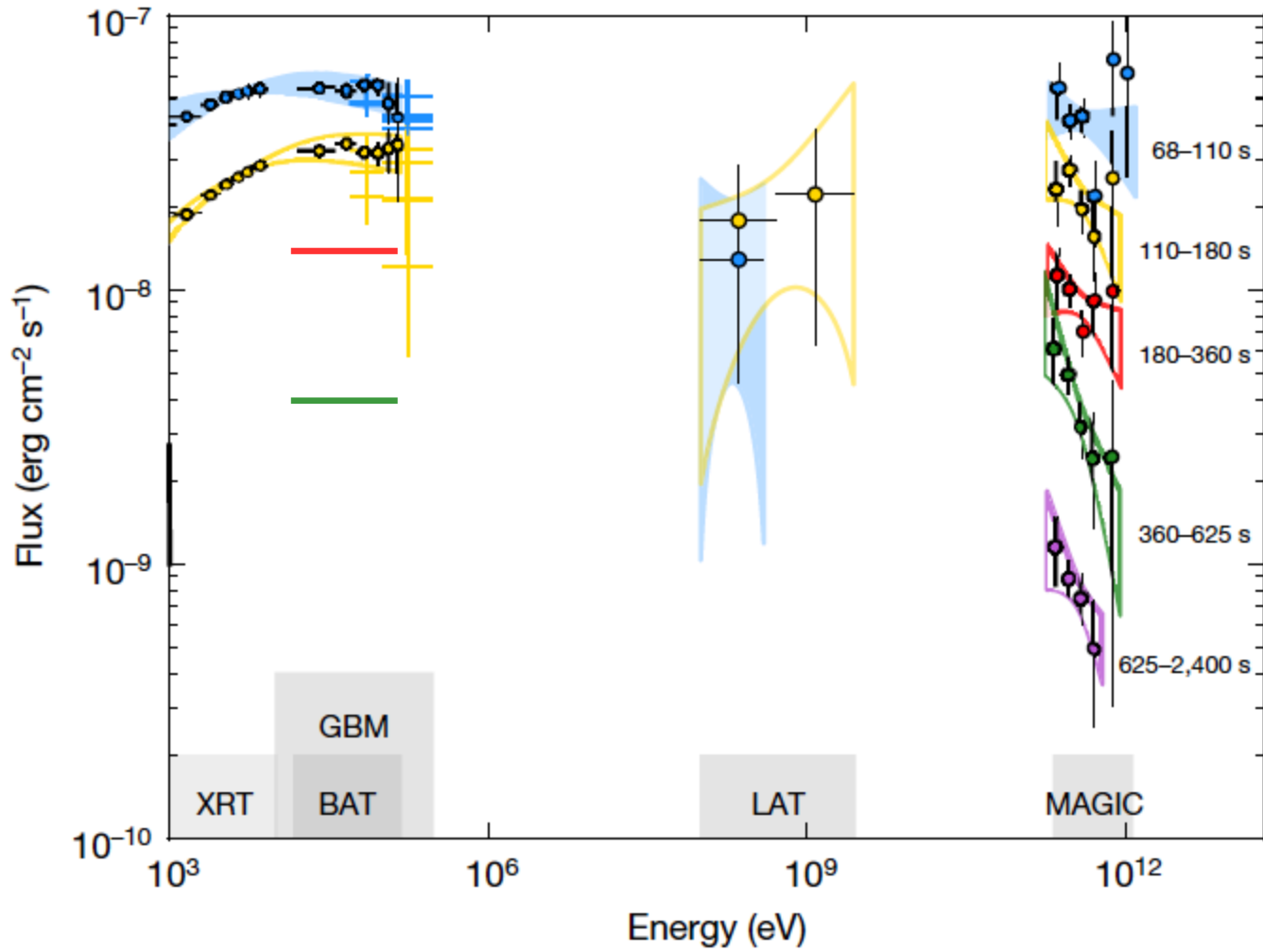
GRB 190829A- Radio Data



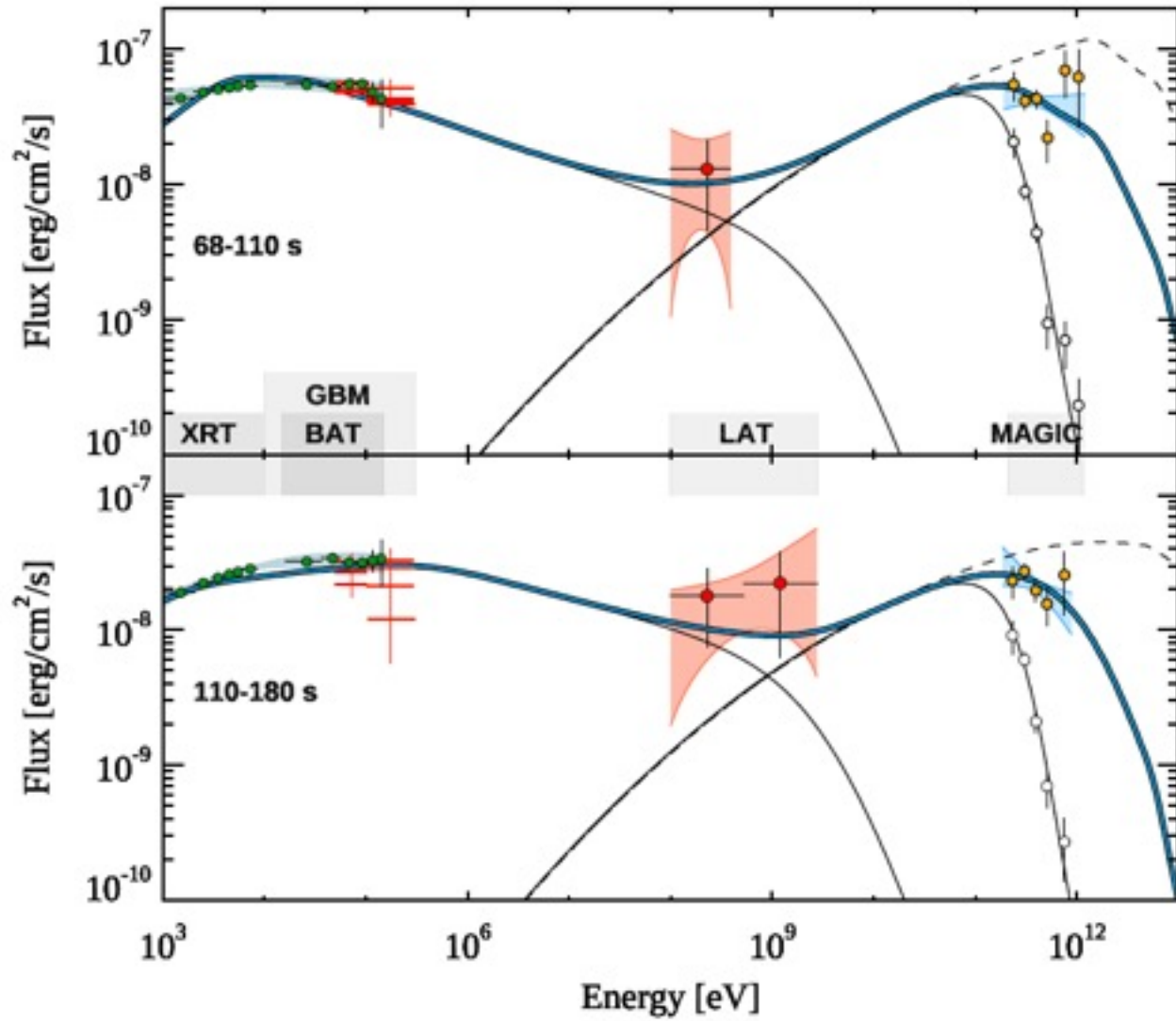
GRB 190114C



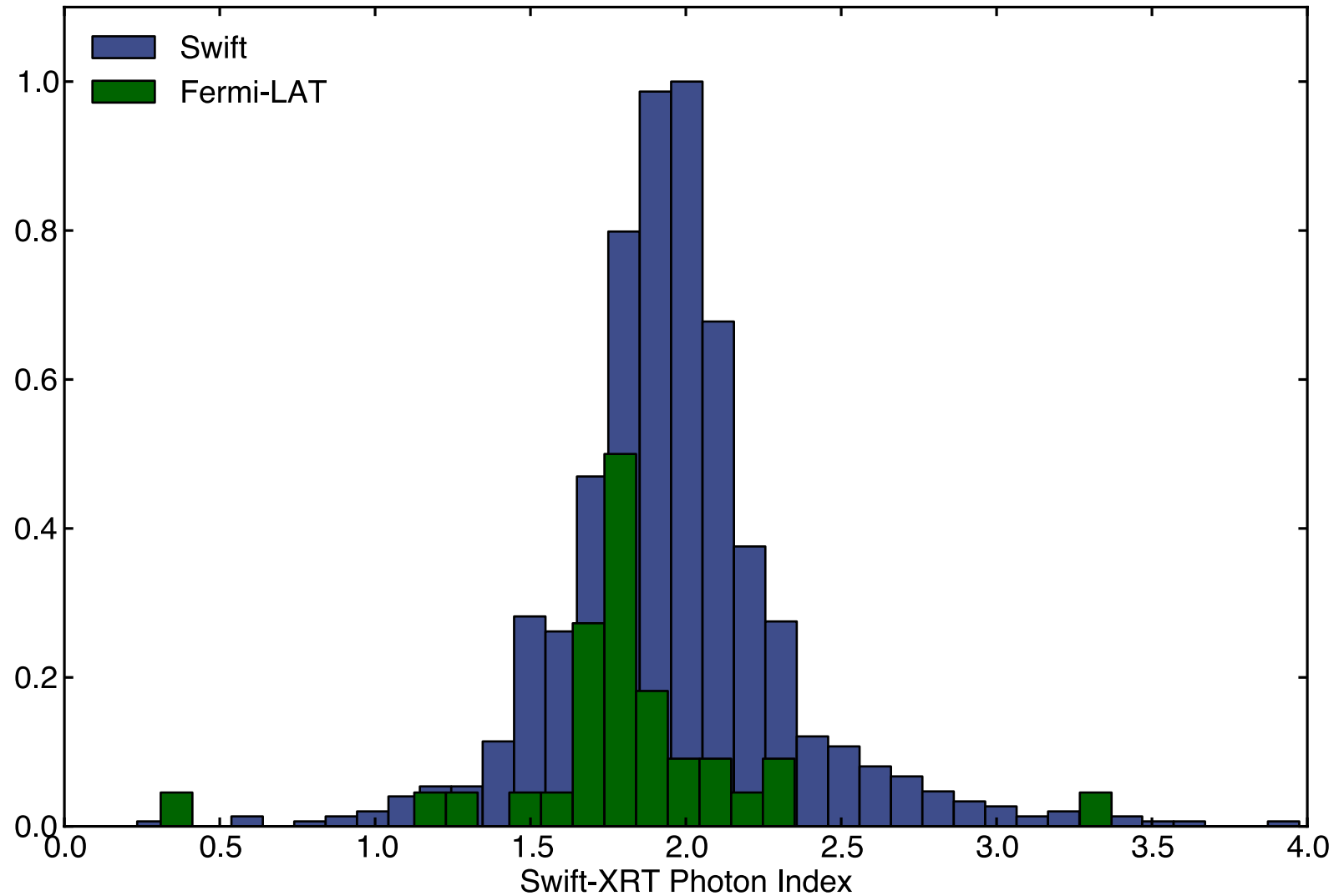
GRB 190114C



GRB 190114C



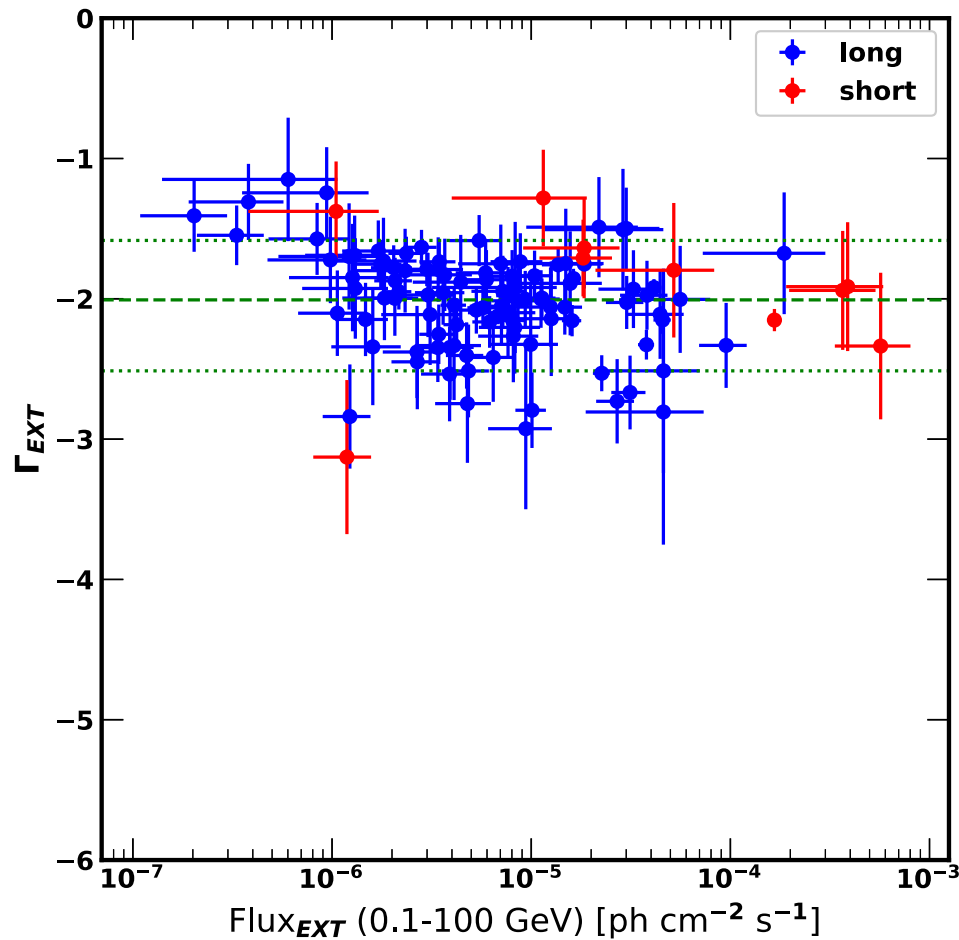
Swift XRT Photon Index Distribution



[Ajello et al., Ap. J., 863 138, 2018]

Andrew Taylor

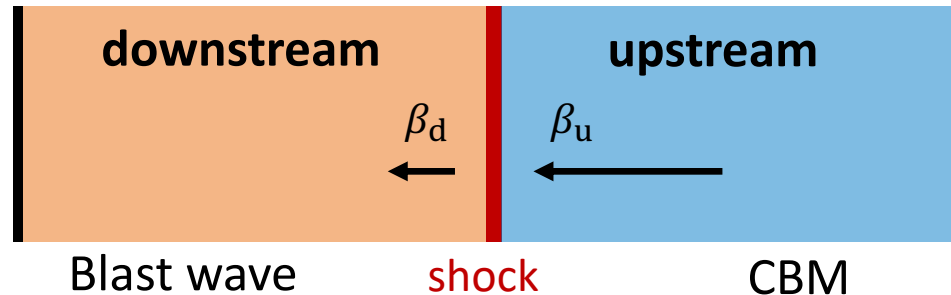
Fermi-LAT Photon Index Distribution



[Ajello et al., Ap. J., 878:52, 2019]

Relativistic Hydro Shocks

What's the compression ratio for relativistic shocks?



Mass Flux:

$$\rho_u \beta_u \Gamma_u = \rho_d \beta_d \Gamma_d$$

Momentum Flux:

$$\mathbf{p}_u + \mathbf{w}_u \beta_u^2 \Gamma_u^2 = \mathbf{p}_d + \mathbf{w}_d \beta_d^2 \Gamma_d^2$$

Energy Flux:

$$\mathbf{w}_u \beta_u \Gamma_u^2 = \mathbf{w}_d \beta_d \Gamma_d^2$$

$$\mathbf{w}_{\text{rel.}} = \frac{\gamma}{\gamma - 1} \mathbf{p} + \rho$$

Relativistic Shocks

Momentum Flux:

$$\mathbf{p}_1 + \left(\frac{\gamma}{\gamma - 1} \mathbf{p}_1 + \rho_1 \right) \beta_1^2 \Gamma_1^2 = \mathbf{p}_2 + \left(\frac{\gamma}{\gamma - 1} \mathbf{p}_2 + \rho_2 \right) \beta_2^2 \Gamma_2^2$$

Energy Flux:

$$\left(\frac{\gamma}{\gamma - 1} \mathbf{p}_1 + \rho_1 \right) \beta_1 \Gamma_1^2 = \left(\frac{\gamma}{\gamma - 1} \mathbf{p}_2 + \rho_2 \right) \beta_2 \Gamma_2^2$$

Cold Relativistic Shocks

Momentum Flux:

$$\rho_1 \beta_1^2 \Gamma_1^2 = \mathbf{p}_2 + \left(\frac{\gamma}{\gamma - 1} \mathbf{p}_2 + \rho_2 \right) \beta_2^2 \Gamma_2^2$$

$$\rho_1 \beta_1^2 \Gamma_1^2 - \rho_2 \beta_2^2 \Gamma_2^2 = \mathbf{p}_2 \left[\mathbf{1} + \left(\frac{\gamma}{\gamma - 1} \right) \beta_2^2 \Gamma_2^2 \right]$$

Energy Flux:

$$\rho_1 \beta_1 \Gamma_1^2 = \left(\frac{\gamma}{\gamma - 1} \mathbf{p}_2 + \rho_2 \right) \beta_2 \Gamma_2^2$$

$$\rho_1 \beta_1 \Gamma_1 (\Gamma_1 - 1) = \frac{\gamma}{\gamma - 1} \mathbf{p}_2 \beta_2 \Gamma_2^2 + \rho_2 \beta_2 \Gamma_2 (\Gamma_2 - 1)$$



Relativistic Shocks

Momentum Flux:

$$\frac{\mathbf{p}_2}{\Gamma_1^2 \beta_1^2 \rho_1} \left[\mathbf{1} + \Gamma_2^2 \beta_2^2 \left(\frac{\gamma}{\gamma - 1} \right) \right] = \left(\mathbf{1} - \frac{\Gamma_2 \beta_2}{\Gamma_1 \beta_1} \right)$$

Energy Flux:

$$\left(\frac{\gamma}{\gamma - 1} \right) \frac{\Gamma_2^2 \mathbf{p}_2 \beta_2}{\Gamma_1^2 \rho_1 \beta_1} = \left(\mathbf{1} - \frac{(\Gamma_2 - 1)}{(\Gamma_1 - 1)} \right)$$

Relativistic Shocks

$$\frac{1 - \frac{\Gamma_2 \beta_2}{\Gamma_1 \beta_1}}{1 + \Gamma_2^2 \beta_2^2 \frac{\gamma}{\gamma - 1}} = \frac{1 - \frac{\Gamma_2 - 1}{\Gamma_1 - 1}}{\Gamma_2^2 \beta_2^2 \frac{\gamma}{\gamma - 1}}$$

$$1 + \Gamma_2^2 \beta_2^2 \left(\frac{\gamma}{\gamma - 1} \right) = \Gamma_2^2 \beta_2^2 \left(\frac{\gamma}{\gamma - 1} \right)$$

$$(\beta_2 - 1)(\beta_2 - (\gamma - 1)) = 0$$

Eg: $\gamma = \frac{4}{3} \quad \rightarrow \quad \frac{\beta_2}{\beta_1} = \frac{1}{3}$

Evolutionary Phases of Blastwave

Assuming shock is radiative (ie. incoming KE flux radiated away)

[R. Blandford + McKee 1976]

$$\frac{dE_k}{dt} = -\varepsilon_{\text{rad}} 4\pi R^2 \beta (\Gamma^2 \rho - \Gamma \rho)$$

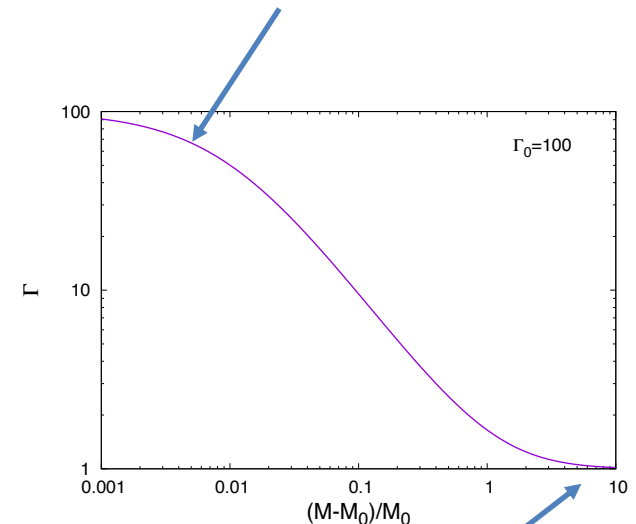
$$E_k = \frac{\rho 4\pi R^3}{3} (\Gamma - 1)$$

$$\frac{d\Gamma}{dM} = -\frac{(\Gamma^2 - 1)}{M}$$

This has the solution

$$\Gamma - 1 = 2 \left(\frac{M^2 (\Gamma_0 + 1)}{M_0^2 (\Gamma_0 - 1)} - 1 \right)^{-1}$$

Critical mass where free expansion changes to deceleration phase



Blast wave becomes non-relativistic

Evolution of Key Energies with Time

