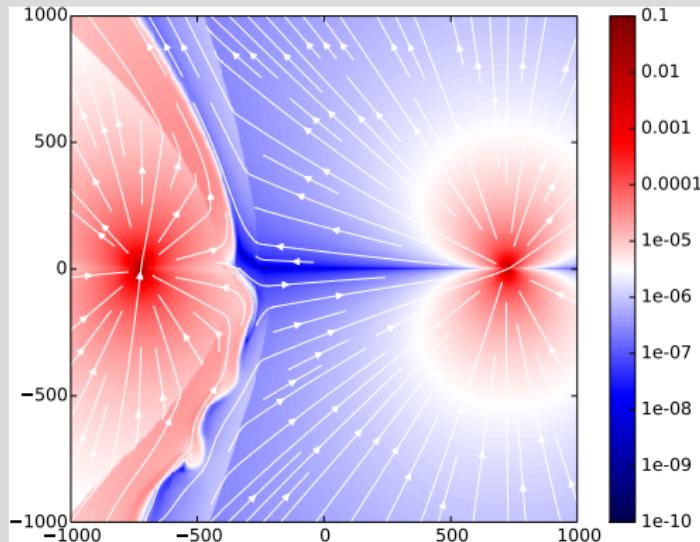


in γ^2 Velorum.



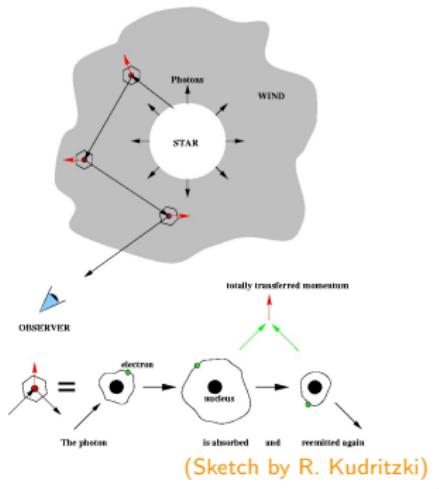
R. Kissmann

Binary System

- Two Massive Stars...

Line-driven Winds

The principle of radiatively driven winds

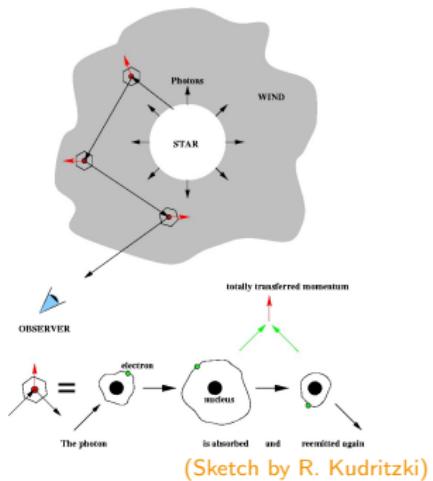


Binary System

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Binary System

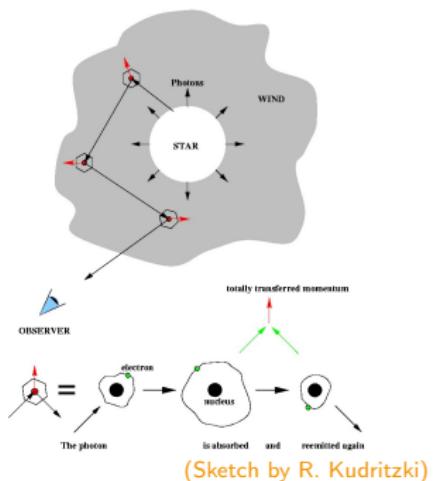
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Results

- Supersonic massive wind outflows
- Interaction → wind-collision region

Line-driven Winds

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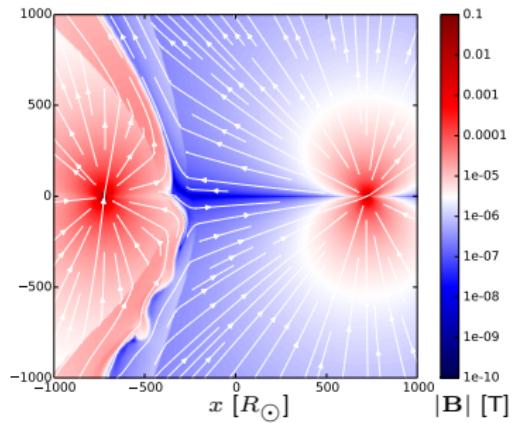
Particles

- Shock Acceleration
- Interaction with matter
 - gamma rays

1: MHD Solver

- Line-driven winds
- Stellar dipole fields
- Free evolution

Magnetic Field

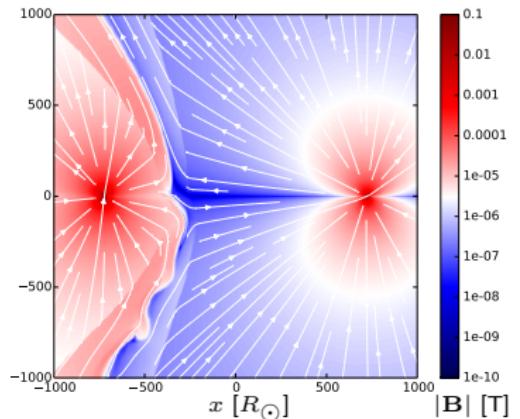


(RK et al. (2016) ApJ 831, 121)

1: MHD Solver

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Magnetic Field



2: Energetic Particles

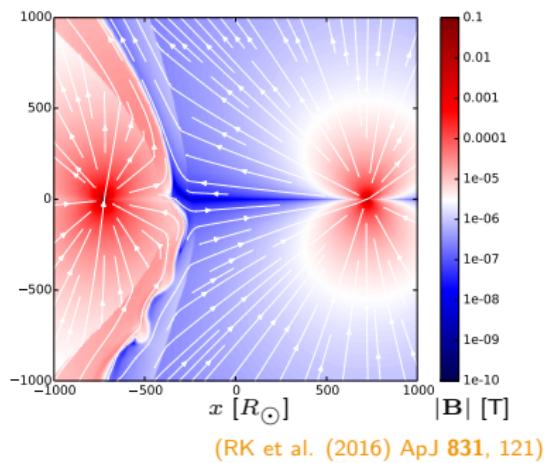
- Injection at Shocks
- Solution of Parker-transport equation

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2: Energetic Particles

- Injection at Shocks
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3: Non-Thermal Emission

- Computation From Particle Spectra
- Postprocessing

Stellar Winds

- Example: Hydrodynamics

System of Equations

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0$$

$$\frac{\partial \rho \mathbf{u}}{\partial t} + \nabla \cdot (\rho \mathbf{u} \mathbf{u} + p \mathbf{I}) = 0$$

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Stellar Winds

- Example: Hydrodynamics
- Radiative cooling
- Force density \mathbf{f} :
 - Gravity of stars
 - Radiative Driving

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Force density

$$\mathbf{f} = \rho \sum_{i=1}^n \left(-GM_{\star,i} \frac{\mathbf{r}_i}{r_i^3} + \mathbf{g}_{rad,i}^l + \mathbf{g}_{rad,i}^e \right)$$

Stellar Winds

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- Radiative Driving:
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Effect of Electrons

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Acceleration by Lines

$$\mathbf{g}_{rad,i}^l = \frac{\sigma_e}{c} \frac{L_{\star,i}}{4\pi r_i^2} k t^{-\alpha} I_{FD} \mathbf{e}_{r_i}$$

Line Driving

- Contribution of $> 10^4$ lines
 - Wind expansion → Doppler
- Expensive

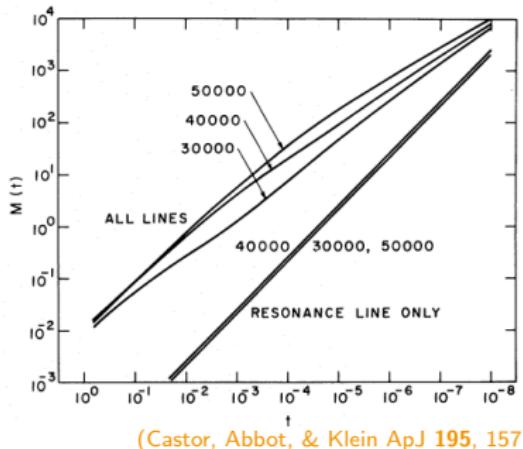
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Numerical Approximation

- Collective: power law

Dependence on Optical Depth



Resulting Acceleration

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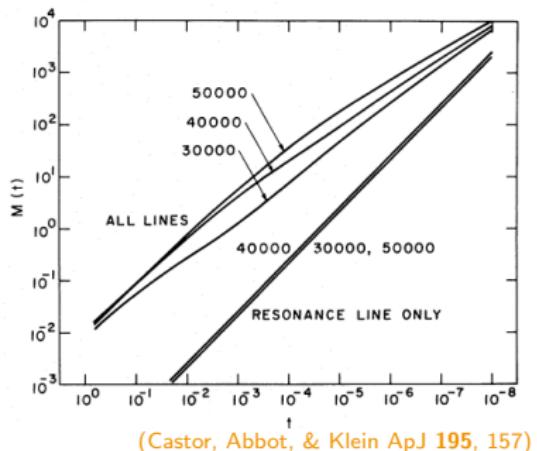
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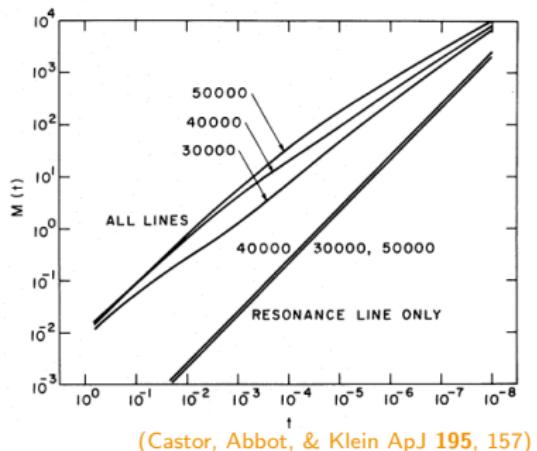
Numerical Approximation

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- \rightarrow Velocity gradient

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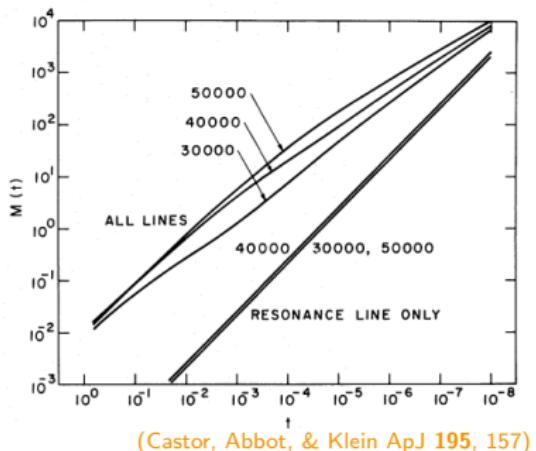
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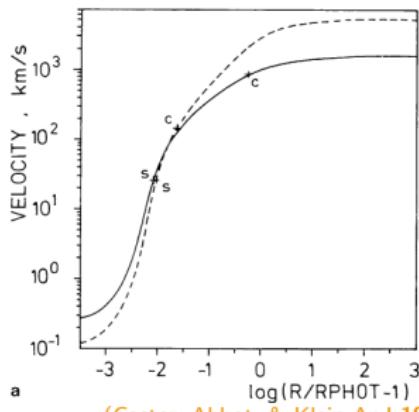
Line Driven Winds

- Very rapid acceleration
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Wind Velocity

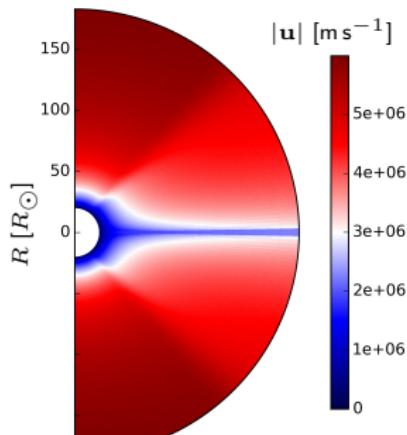


(Castor, Abbot, & Klein ApJ 195, 157)

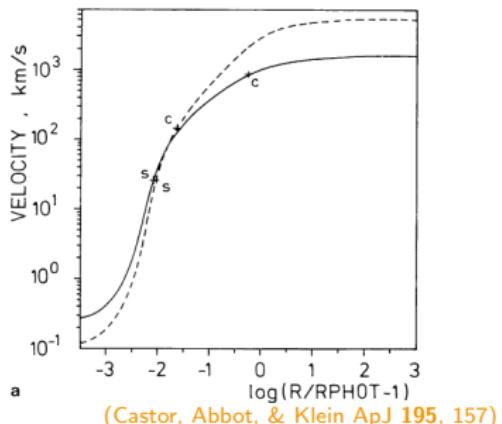
Line Driven Winds

- Very rapid acceleration
- Acceleration rate \leftrightarrow velocity gradient
- Magnetic field

Modified Velocity Field



Wind Velocity



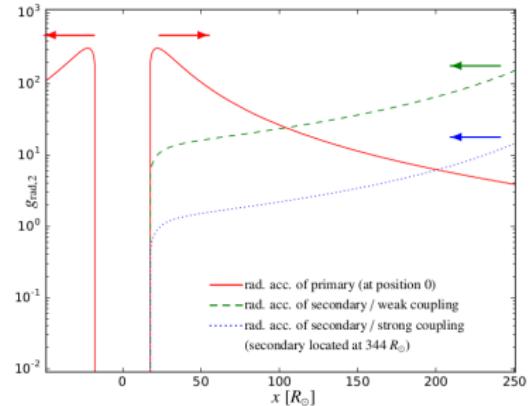
Situation in WR 11

- Collision before v_∞ is reached

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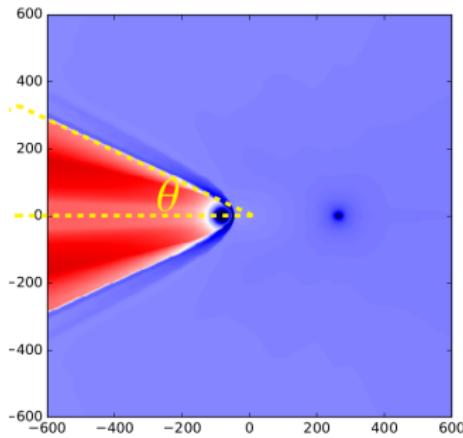
Apastron Configuration



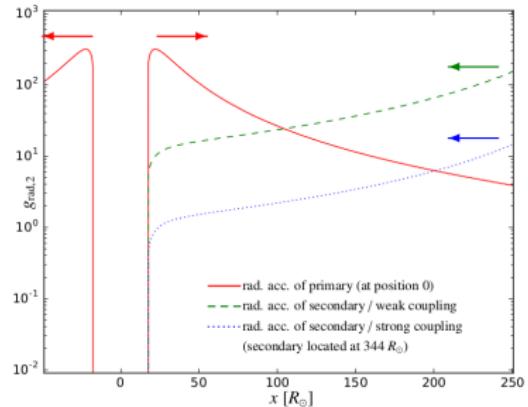
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Velocity (Weak Coupling)



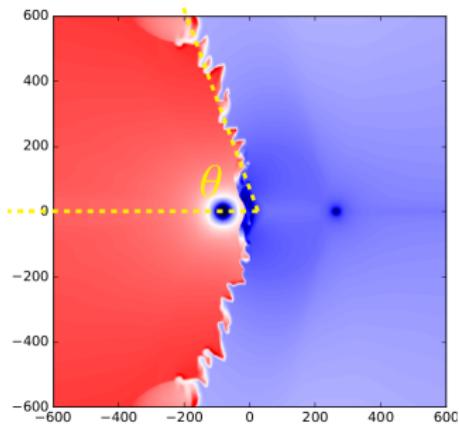
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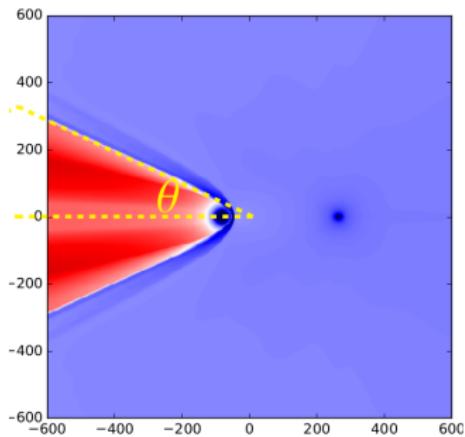
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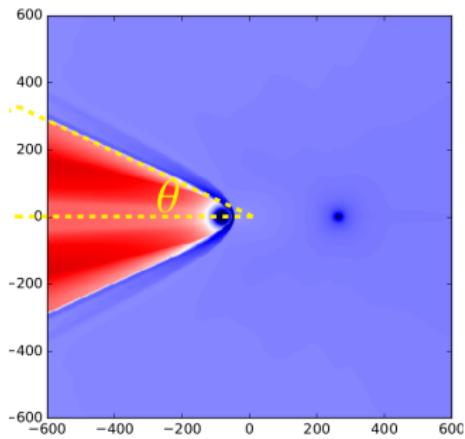
Velocity (Weak Coupling)



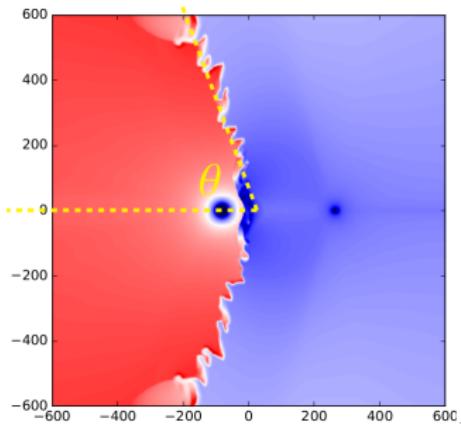
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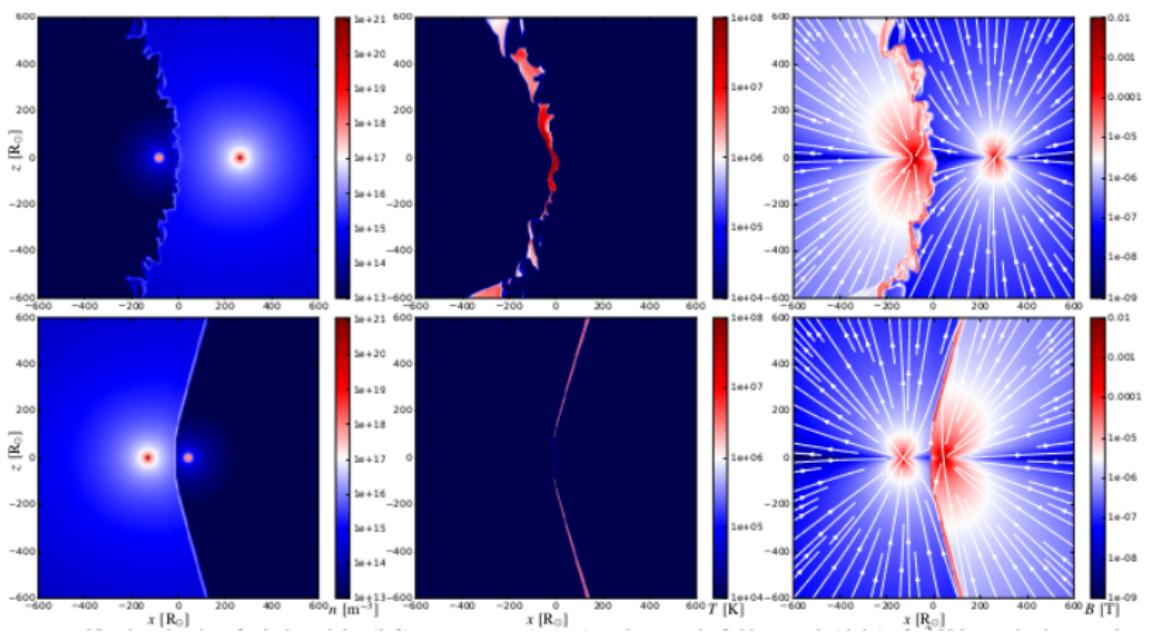
Velocity (Strong Coupling)



Effects

- Radiative breaking
- Shadowing

Wind Properties in WR 11



Transport Equation

$$\frac{\partial j}{\partial t} - D(E) \nabla^2 j + \nabla \cdot (\mathbf{u} j) - \frac{\partial}{\partial E} \left(\left(\frac{E}{3} \nabla \cdot \mathbf{u} + \dot{E}_{\text{loss}} \right) j \right) = Q_0 \delta(E - E_0)$$

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- **Injection at shock fronts**
- Advection with fluid flow
- Spatial diffusion
- Energy losses

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Energy loss processes

- Synchrotron (Electrons)
- Inverse Compton (Electrons)
- Thermal bremsstrahlung (Electrons)
- Coulomb losses
- Nucleon-nucleon interaction

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Implementation

- Electrons & Protons
- Advect scalar fields
- Semi-Lagrangian solver

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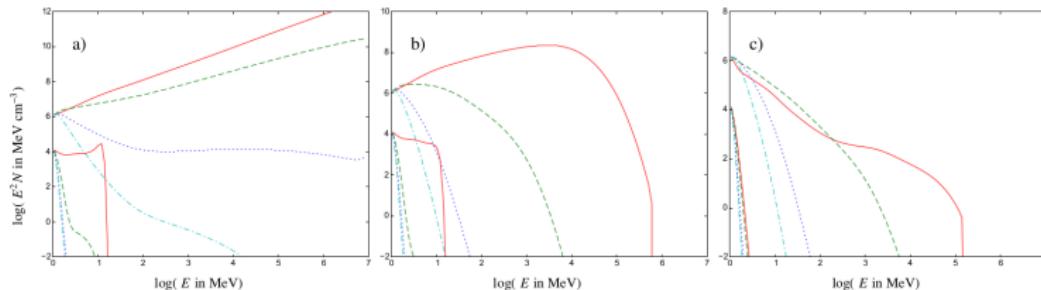
- Injection at shock fronts
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Results

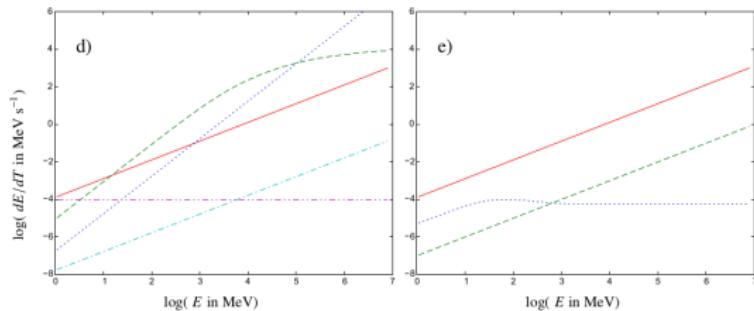
- Position-dependent particle flux
- Can compute non-thermal emission

The Role of Spatial Diffusion

Particle Spectra

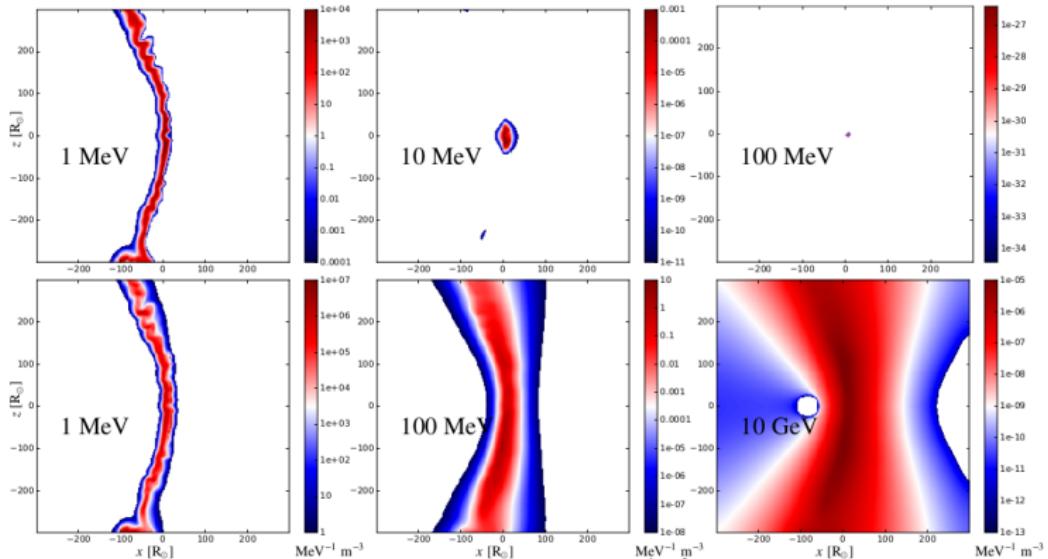


Energy-Loss and Acceleration Rates



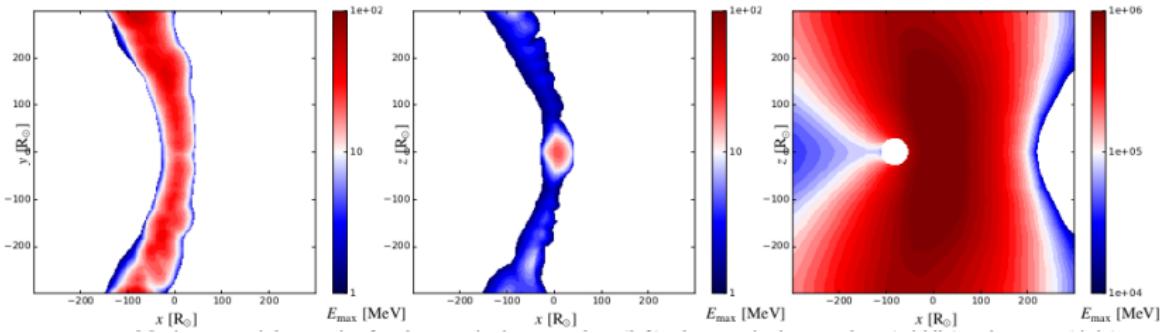
Resulting Particle Distribution

Spatial Distribution



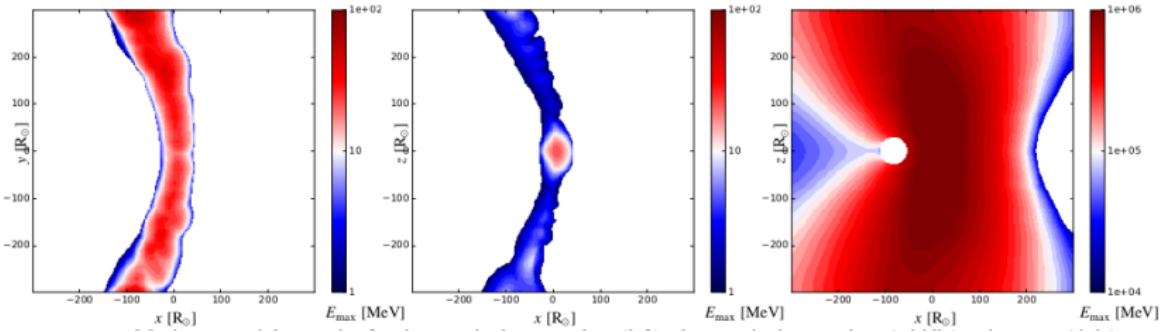
Resulting Particle Distribution

Maximum Particle Energies

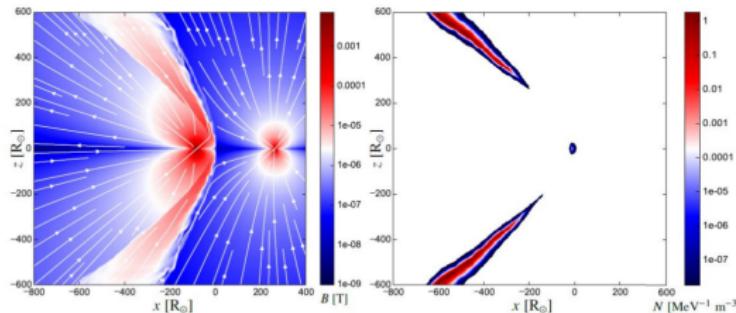


Resulting Particle Distribution

Maximum Particle Energies



Magnetic Field & Synchrotron Losses



Properties of WR 11

- Electrons Suppressed:
 - High radiation fields
 - Strong magnetic field

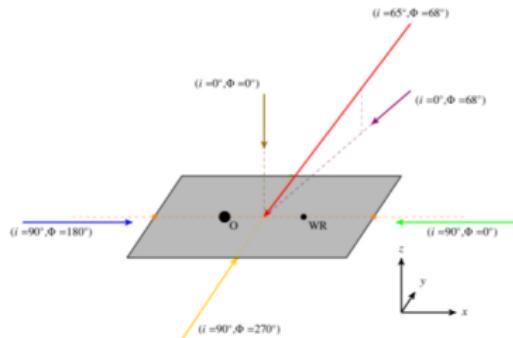
Properties of WR 11

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- Dominant Process:
$$\rightarrow p + p \rightarrow p + p + \pi^0$$
$$\rightarrow \pi^0 \rightarrow \gamma + \gamma$$

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Projection of Radiation



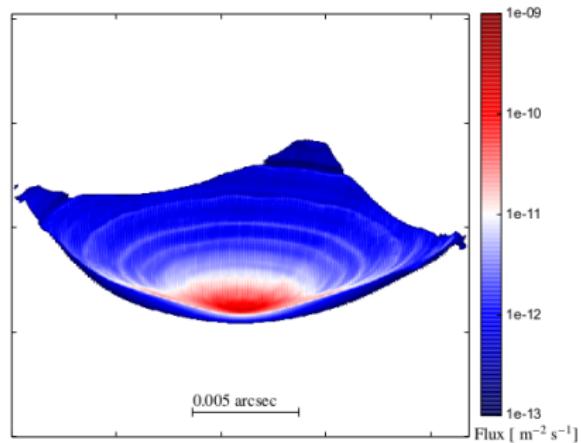
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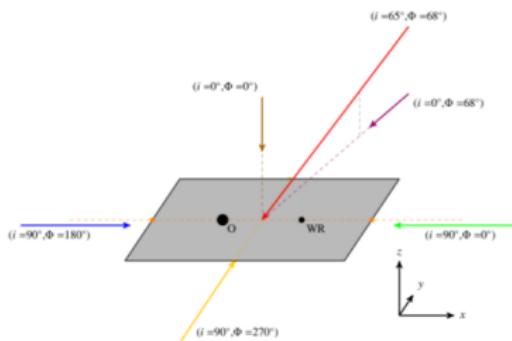
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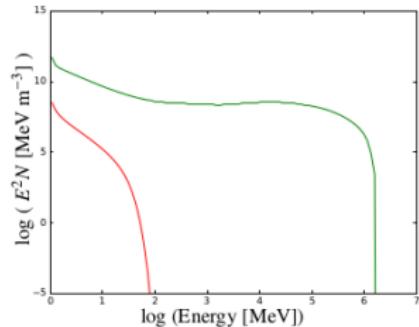
Pion-Decay Emission



Projection of Radiation

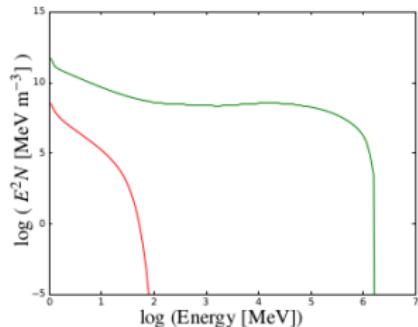


Integrated Particle Spectra

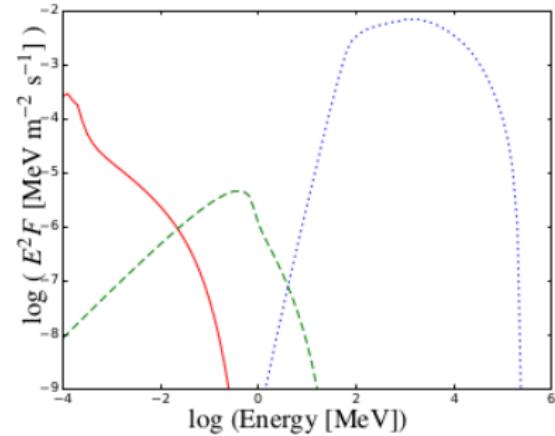


Gamma-Ray Emission II

Integrated Particle Spectra

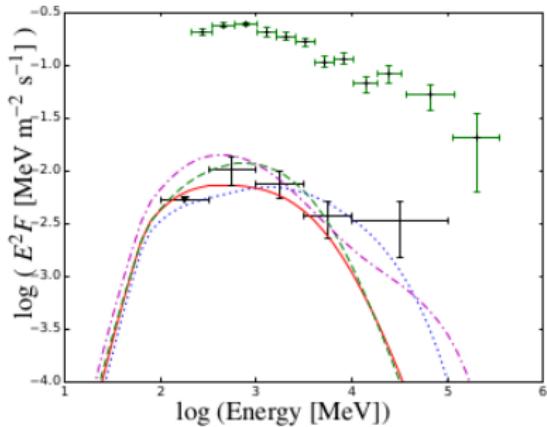


Non-Thermal Radiation

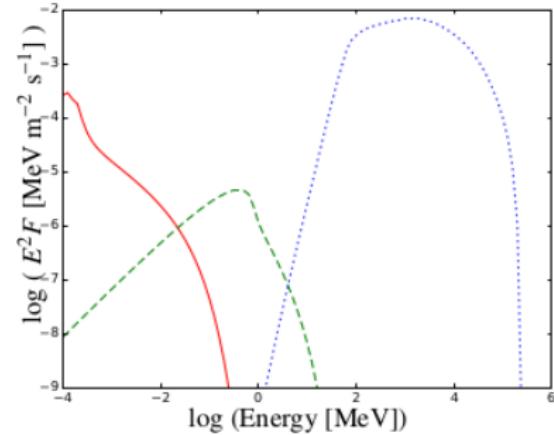


Gamma-Ray Emission II

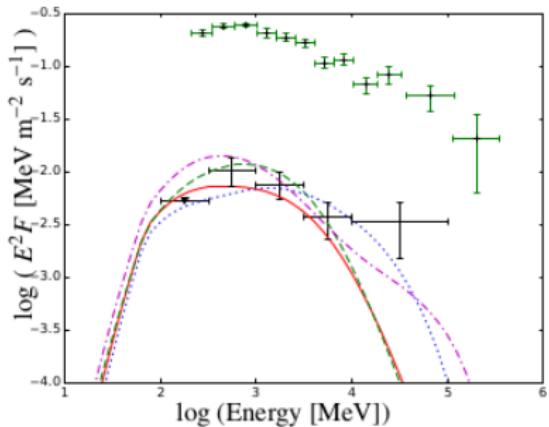
Comparison To Data



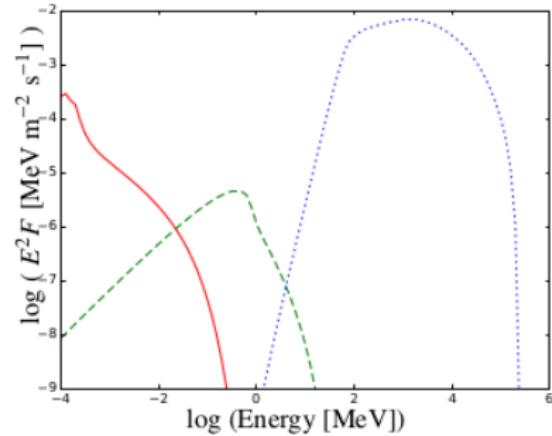
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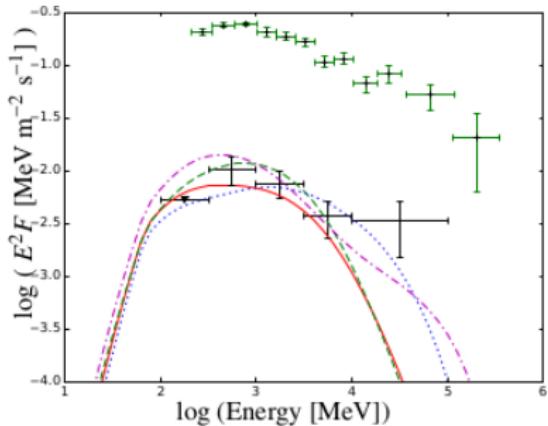
Non-Thermal Radiation



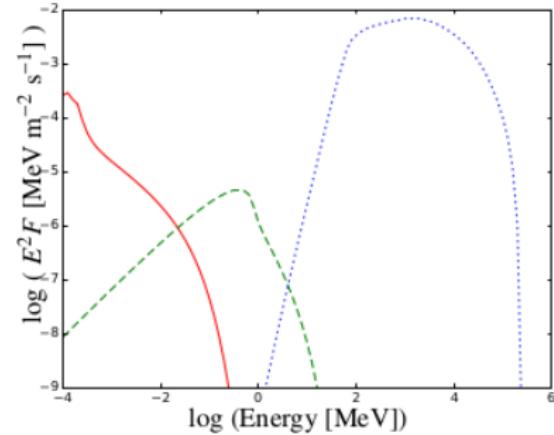
Conclusion

- WR 11: hadron accelerator
- Fit to data possible
- Max flux at apastron
- Min flux at periastron

Comparison To Data



Non-Thermal Radiation



Ongoing / Outlook

- Orbital Motion
- Other Systems
- New application:
gamma-ray binaries