

Cosmic Probes of the Next Fundamental Scale of Nature

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Prologue

I do not have specific theoretical predictions for CTA in this talk. My aim is to draw community's attention to a range of new particle physics phenomena which, in the foreseeable future, can only be probed by means of high energy astrophysics.

A little bit of history

- Cosmic rays were instrumental in development of particle physics $\sim 30^{\text{th}}\text{-}50^{\text{th}}$ discoveries: positron (32'), muon (37')...
- Since $\sim 50^{\text{th}}$, theoretical developments + collider physics lead to several breakthrough discoveries.

Pattern of these discoveries:

Known theory \rightarrow extrapolate to high energies \rightarrow define the energy scale where the theory breaks down \rightarrow build the collider \rightarrow discover new theory \rightarrow ...

Fermi theory of weak interactions $\rightarrow E_* \sim 100 \text{ GeV} \rightarrow$ SppS (CERN) \rightarrow discovery of W,Z-bosons (electroweak unification) $\rightarrow E_* \sim 1 \text{ TeV} \rightarrow$ LHC (CERN) \rightarrow discovery of Higgs boson (Standard Model)

What is the next energy scale to be probed?

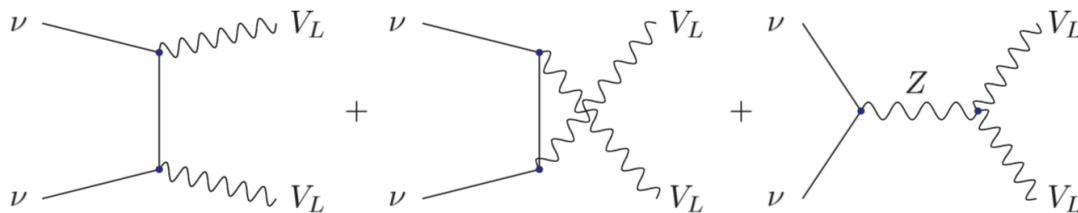
- **Neutrino masses** - robust evidence from particle physics (neutrino oscillation) experiments

Add neutrino mass to the SM Lagrangian (EW gauge invariance is still OK, but nonlinear):

$$\mathcal{L}_\nu = -\frac{1}{2}m_\nu \nu_L^T C \nu_L + h.c \equiv -\frac{1}{2}m_\nu [L^T \epsilon \Sigma] C [\Sigma^T \epsilon L]$$

$$L = (\nu, \ell), \quad \Sigma = \exp\{i\sigma^a \pi^a(x)\}(0, 1)$$

Consider in this theory neutrino scattering off longitudinal EW bosons:



Perturbative unitarity implies:

$$\Lambda \lesssim \frac{4}{\alpha_2} \cdot \frac{M_W^2}{m_\nu} \sim 10^{11} \text{ GeV}$$

Maltoni, Niczyporuk, and Willenbrock, 01'

What is the next energy scale to be probed?

- **Dark Matter** – robust, but only observed in gravitational interactions

Assuming non-relativistic DM is produced thermally via weak-strength scatterings with SM particles, we arrive at the ‘WIMP miracle’:

$$\Omega_X h^2 \sim \frac{3 \cdot 10^{-27} \text{ cm}^3/\text{sec}}{\langle \sigma v_{\text{rel}} \rangle}$$

Cross section is constrained from perturbative unitarity:

$$\sigma_J \leq \pi(2J+1)/p_i^2 \approx 16\pi(2J+1)/(m_X^2 v_{\text{rel}}) \implies m_X^2 \leq 16\pi/(\sigma_{J=0} v_{\text{rel}}), [v_{\text{rel}} \approx 1/4]$$

$$\Lambda \sim m_X \lesssim 100 \text{ TeV}$$

Griest and Kamionkowski, 90'

What is the next energy scale to be probed?

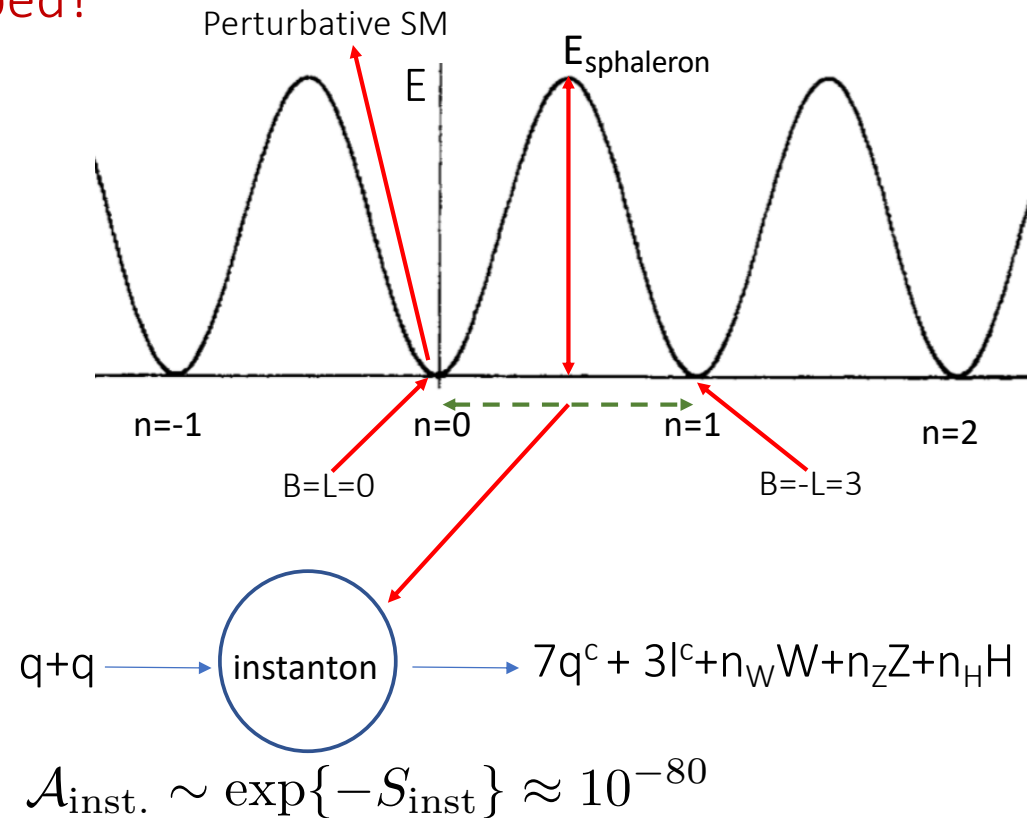
- EW vacuum has topologically non-trivial structure [SU(2) sector].
- Neighboring vacua differ by 3 units of B and L:
 $\Delta B = -\Delta L = 3\Delta n$ (quantum anomaly);
 $\Delta(B-L) = 0$.

- EW instantons are classical solution of Euclidean e.o.m., with action, e.g., for $\Delta n = 1$,

$$S_{\text{inst.}} = \frac{2\pi}{\alpha_2}$$

(multiple of W, Z, H particles in a coherent state)

- describe vacuum-to-vacuum transitions)

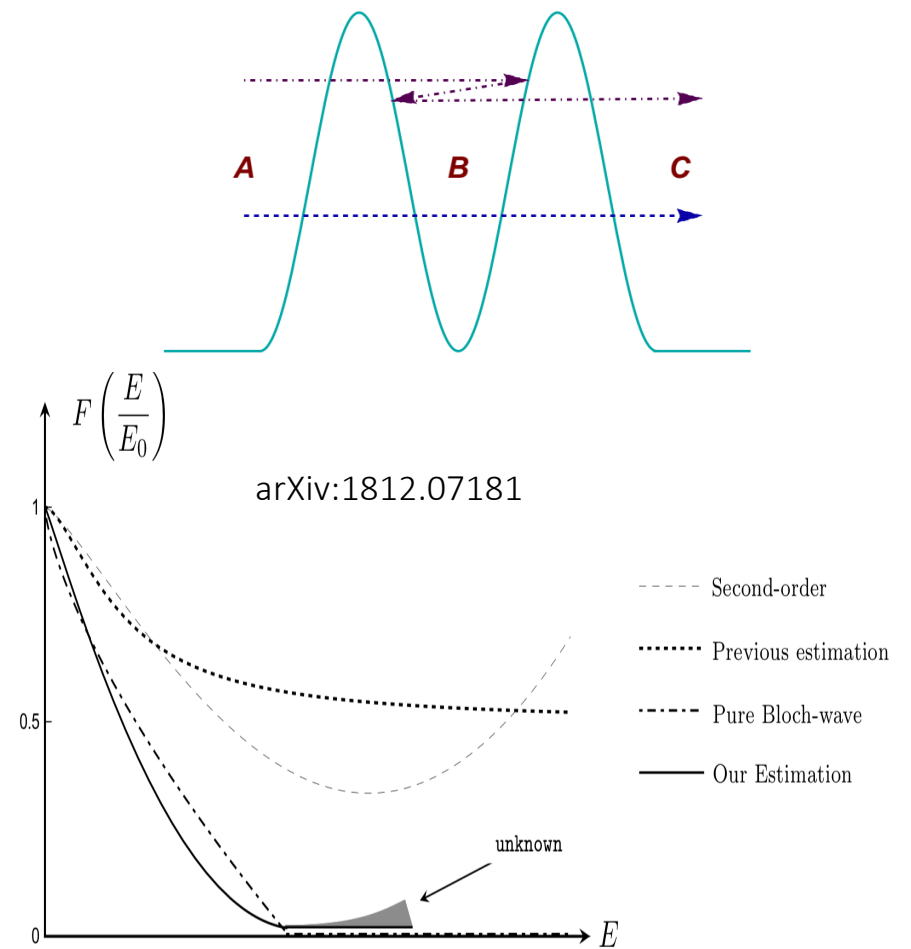


$$\Lambda \sim E_{\text{sphaleron}} \sim \frac{4M_W}{\alpha_2} \approx 10 \text{ TeV}$$

Sphalerons at high energies

- Jump over barrier is described by production and subsequent decay of a sphaleron.
- Sphaleron is an unstable particle-like classical solution with a typical size $\sim 1/M_W$ and mass ~ 10 TeV.
- Spectacular B+L – violating processes with multiple of W,Z and H (background-free!)
- Cross section:

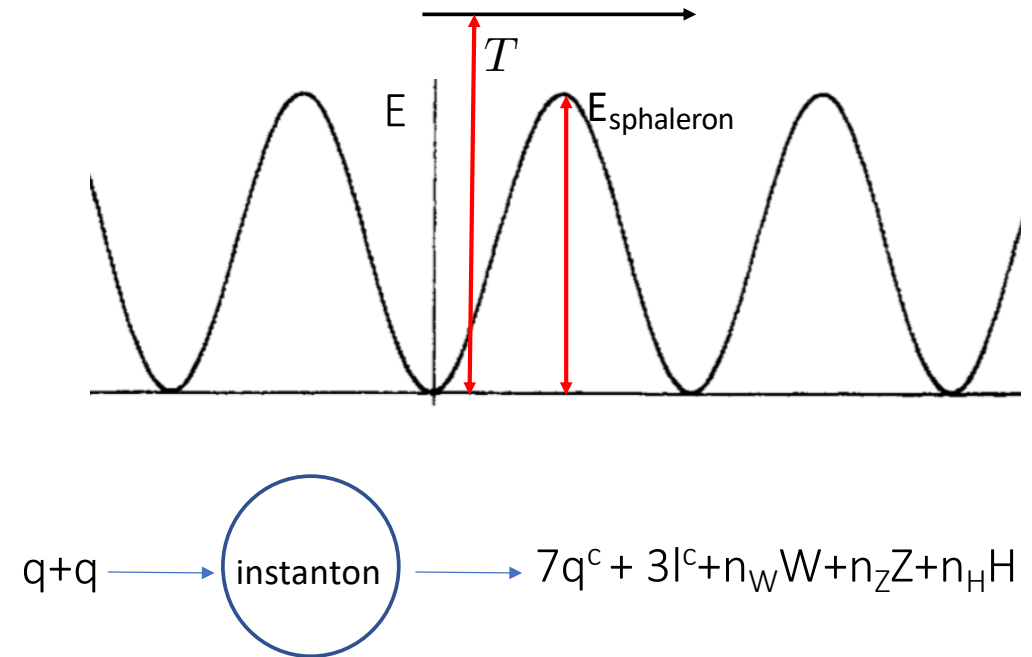
$$\sigma \propto \exp\{-2S_{\text{ints.}} F(E/E_0)\}, \quad [E_0 \equiv E_{\text{sphaleron}}]$$



Ringwald; McLerran, Vainstein and Voloshin 90'
Bezrukov and Levkov, 03'
Tye and Wong, 15'

Going back in time

- Let's extrapolate our theory back in time, when the temperature of the universe was $T > E_{sphaleron}$
- Instanton mediated processes are rapid (thermally activated transitions) $\sim \alpha_2 T^4$
- Problem: any pre-existing matter-antimatter asymmetry gets washed-out and we end up in an inhabitable universe without matter.



- Alternatively: In non-equilibrium and with extra CP violation these processes could explain the origin of matter in the visible universe!

Electroweak monopoles

[Arunasalam, Collison, AK, 18']

- Standard (and incorrect) argument against electroweak monopoles:

$$H^\dagger H \equiv \phi_1^2 + \phi_2^2 + \phi_3^2 + \phi_4^2 \stackrel{r \rightarrow \infty}{=} \rho_0^2$$

Map of S^2 (boundary at spatial infinity) onto the vacuum manifold S^3 . The map is trivial, hence topological ('t Hooft-Polyakov) monopoles do not exist.

- However, ϕ_i can be singular (gauge d.o.f.). In that case the vacuum manifold may not be S^3 .

- Consider an ansatz:

Cho and Maison, 96'

$$H = \frac{1}{\sqrt{2}}\rho(r)\zeta, \quad \zeta = i \begin{pmatrix} \sin(\theta/2)e^{-i\phi} \\ -\cos(\theta/2) \end{pmatrix},$$

$$\mathbf{A}_\mu = -\frac{1}{g_2}A(r)\partial_\mu t \hat{r} + \frac{1}{g_2}(f(r) - 1)\hat{r} \times \partial_\mu \hat{r},$$

$$B_\mu = -\frac{1}{g_1}B(r)\partial_\mu t - \frac{1}{g_1}(1 - \cos\theta)\partial_\mu \phi.$$

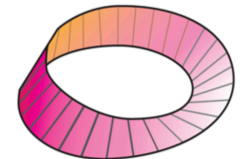
Singular at $\theta = \pi/2$

Electroweak monopoles

- Denote the components of doublet Higgs as: $z_1 \equiv \phi_1 + i\phi_2, z_2 \equiv \phi_3 + i\phi_4$
- Are defined up to hypercharge gauge transformations: $(z_1, z_2)^T \equiv (\lambda z_1, \lambda z_2)^T, \lambda \in U(1)_Y$.
Hence could be viewed as coordinates on a complex plane \mathbb{C}^2 (modulo singularities).
- Remove singularities by using the gauge freedom and defining two monopole solutions on two different patches of space:

$$H_N = i \frac{\rho(r)}{\sqrt{2}} \begin{pmatrix} \sin(\theta/2) e^{-i\phi} \\ -\cos(\theta/2) \end{pmatrix}, \quad B_\phi^N = -\frac{1}{g'} \frac{1 - \cos \theta}{r \sin \theta} \quad \text{for } 0 \leq \theta \leq \pi/2, \text{ and}$$

$$H_S = i \frac{\rho(r)}{\sqrt{2}} \begin{pmatrix} \sin(\theta/2) \\ -\cos(\theta/2) e^{i\phi} \end{pmatrix}, \quad B_\phi^S = \frac{1}{g'} \frac{1 + \cos \theta}{r \sin \theta} \quad \text{for } \pi/2 \leq \theta \leq \pi.$$



- At the equator ($\theta = \pi/2$) the transition function $e^{i\phi}$ is a holomorphic function $\Rightarrow (z_1, z_2)$ actually span a projective complex plane \mathbb{CP}^1 .
- Hence, monopole solution is topologically nontrivial: $\pi_2(\mathbb{CP}^1) = \pi_2(S^2) = \mathbb{Z}$

Electroweak monopoles

- Considering, two monopole solutions on the whole space (with opposite magnetic charges), one gets monopole-antimonopole bound state, which actually is a sphaleron!
- Monopole – particle scattering is known unsuppressed (Rubakov 81'; Callan 82'). By crossing symmetry the process of production of monopole-antimonopole pair in two-particle collision must not be suppressed either. Monopole-antimonopole pair then can form sphaleron:

$$q + q \rightarrow M + M^c \rightarrow 7q^c + 3l^c + n_W W + n_Z Z + n_H H$$

- EW monopoles inevitably introduce new CP violating phase (Witten effect):

$$\mathcal{L}_\theta = \theta_2 F_{\mu\nu}^a \tilde{F}^{a\mu\nu} + \theta_1 B_{\mu\nu} \tilde{B}^{\mu\nu} \Rightarrow \mathcal{L}_\theta = \theta_{ew} F_{\mu\nu}^a \tilde{F}^{a\mu\nu}, \quad \theta_{ew} = \theta_2 - \theta_1$$

- Contribute to EDM of known particles
- Successful electroweak baryogenesis scenario [Arunasalam and AK, 17']

The electroweak monopole

- The mass of EW monopoles is divergent. Within the string theory inspired Born-Infeld-type extension of the Standard Model [Arunasalam, AK, 17']:

$$E_{\text{monopole}} \simeq 77.1 \sqrt{\beta} + 2.8 \text{ TeV}, \quad \sqrt{\beta} \text{ is the Born-Infeld mass parameter}$$

- PVLAS measurements of nonlinearity in light propagation:

$$\sqrt{\beta} \gtrsim 5.0 \cdot 10^{-4} \text{ GeV} \implies E_{\text{monopole}} \gtrsim 2.8 \text{ TeV}$$

- Constraints from the light-by-light scattering data extracted from heavy ion collisions at LHC:

$$\sqrt{\beta} \gtrsim 88 \text{ GeV} \implies E_{\text{monopole}} \gtrsim 9.6 \text{ TeV} \quad \text{Ellis, Mavromatos, You, 17'}$$

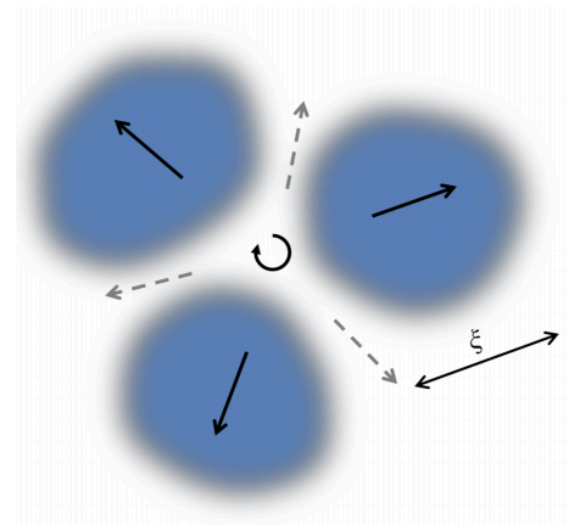
- LHC is not capable to produce EW monopoles. Higher energy collider or search in cosmic rays!
- 'Sweet spot' value for EW monopole mass $\sim 10^7 \text{ GeV}$ (baryogenesis)

Cosmological production of EW monopoles

- The EW monopoles are produced during the electroweak phase transition when the temperature of the universe was $T_{\text{EW}} \sim 100 \text{ GeV}$ ($\sim 10^{-32} \text{ s}$ after Big Bang) via the Kibble mechanism.
- The estimated monopole number density today:

$$n_M \sim \frac{1}{\alpha_g^3} \left(\frac{M}{M_{\text{Pl}}} \right) T_{\text{CMB}}^3 \sim 10^{-26} \left(\frac{M}{10^7 \text{ GeV}} \right) \text{ cm}^{-3}.$$

$\alpha_g = 1/2\alpha \simeq 68.5$ - the magnetic 'fine structure' constant



Astrophysics of EW monopoles

- While produced non-relativistic, (not very heavy) EW monopoles are easily accelerated in a galactic magnetic field $B \sim 3\mu\text{G}$:

$$v_{\text{mag}} \sim \begin{cases} c, & M \lesssim 10^{11} \text{GeV} , \\ 10^{-3} c \left(\frac{10^{17} \text{GeV}}{M} \right)^{1/2}, & M \gtrsim 10^{11} \text{GeV} . \end{cases}$$

- The flux of relativistic monopoles:

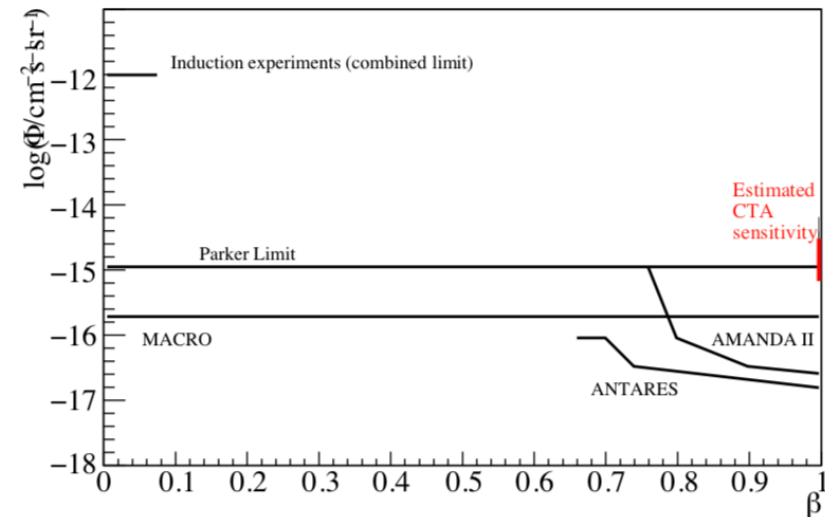
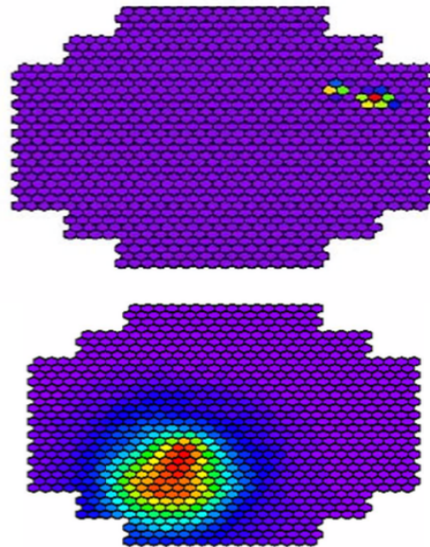
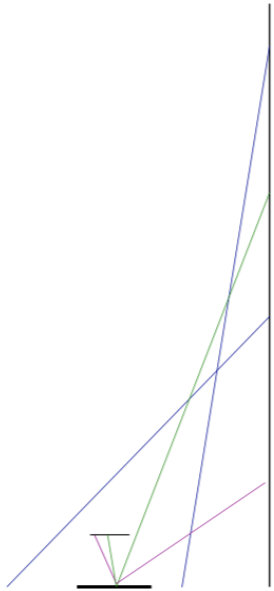
$$F = \frac{cn_M}{4\pi} \approx 2.3 \cdot 10^{-19} \left(\frac{M}{10^7 \text{GeV}} \right) \text{cm}^{-2} \text{sr}^{-1} \text{s}^{-1}$$

Cherenkov light from relativistic monopoles

- Because much stronger electromagnetic interactions a relativistic monopole produces

$$\sim n^2 \left(\frac{g}{e} \right)^2 = 2n^2 \alpha_g^2 \approx 9400 \text{ more photons than e.g., a relativistic muon.}$$

- If no other interactions, very distinct image [Spengler, Schwanke, 11']:



M. Doro et al, 2012

More exotic signatures from EW monopoles and sphalerons

- B+L-violating electroweak scatterings:

$$M + N \rightarrow M + 6q^c + 3l^c + [\text{Higgses}, W\text{'s}, Z\text{'s}]$$

Much more brighter showers than usual hadronic ones.

- More theoretical work required
- Are we throwing them out as a 'background'?
- A dedicated image cleaning? A dedicated analysis?

Cosmic ray air showers from sphalerons

- Available energy transfer $E = \sqrt{E_{CR} m_N} \approx 500 \text{ TeV!}$

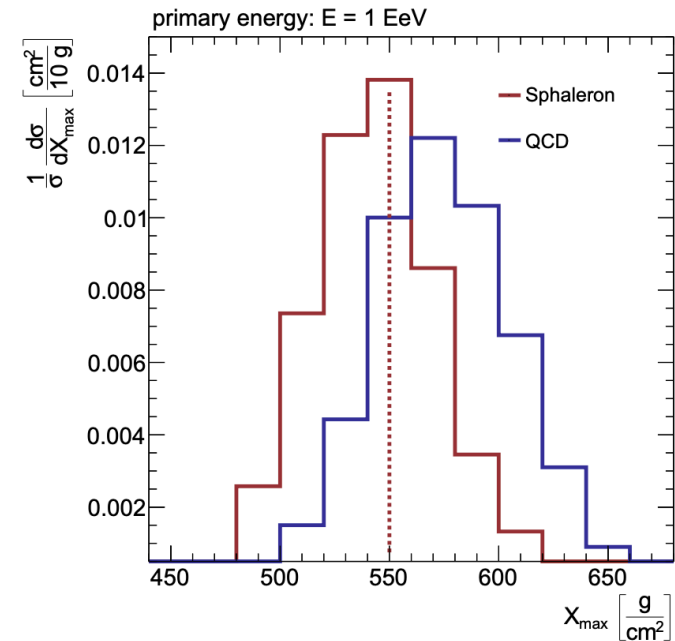
$$q + q \rightarrow 7q^c + 3l^c + n_W W + n_Z Z + n_H H$$

- At least one hard muon
- Different radial size of the air shower

Can be probed/constrained at Pierre Auger.

- Enhanced neutrino-nucleon scattering (IceCube)

$$\nu + q \rightarrow 8q^c + 2l^c + n_W W + n_Z Z + n_H H$$



arXiv:1602.00647

Conclusion

- The robust prediction for a new physics scale within SM is ~ 10 TeV.
- This scale is associated with a non-perturbative aspects of electroweak theory and potentially provides (less explored) portal to the BSM physics.
- Ultimate relation to one of the most fundamental puzzles of modern cosmology – the origin of matter in the universe
- High energy astrophysics is the only feasible option to probe these phenomena in the visible future
- Several theoretical/computational issues must be solved. Dedicated analyses and modelling.

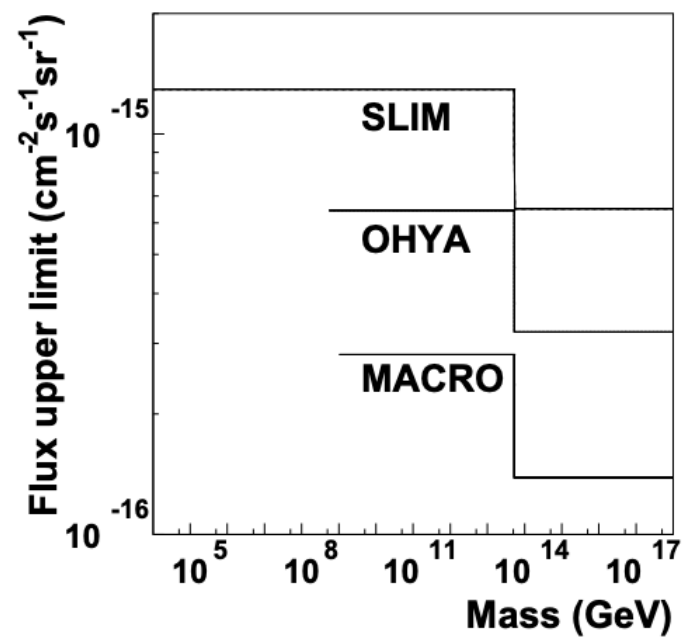
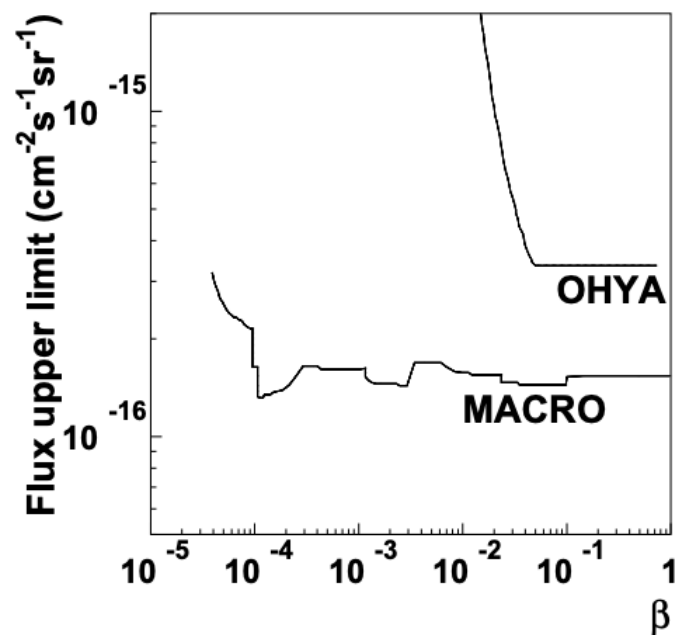
Astrophysics of EW monopoles

- Constraints from the survival of galactic magnetic field (the Parker bound):

$$F < \begin{cases} 10^{-15} \text{ cm}^{-2} \text{ sr}^{-1} \text{ sec}^{-1}, & M \lesssim 10^{17} \text{ GeV} , \\ 10^{-15} \left(\frac{M}{10^{17} \text{ GeV}} \right) \text{ cm}^{-2} \text{ sr}^{-1} \text{ sec}^{-1}, & M \gtrsim 10^{17} \text{ GeV} . \end{cases}$$

- EW monopoles do not catalyze proton decay (like GUT monopoles). Therefore, bounds from the heating of compact objects do not directly apply. However, they mediate different B+L violating processes, requires careful study.

Summary of constraints



D. Mealsted & E.J. Weinberg, PDG 2017