Particle acceleration by kinetic instabilities in accretion disks: A particle-in-cell (PIC) simulation study

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Motivation:

Low-luminosity accretion disks around black holes: Examples: Sgr A* and M87.

What do they have in common: $\tau_{coll} >> \tau_{accr}$ τ_{coll} : Coulomb collision time and τ_{accr} : Accretion time of the gas

In this **weakly collisional plasmas**, there is **no obvious thermalization mechanism**. Therefore the evolution of the energy distribution could involve **non-thermal acceleration**.

Relevant for interpreting: High resolution imaging



Sgr A* multi-wavelength observations.



Power-law tail with spectral index $\alpha_s \sim 3.5$ in quiescent state

Sgr A* a Pevatron?



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Can this scattering accelerate stochastically the particles?

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2D particle-in-cell (PIC) simulations (TRISTAN-MP) in a shearing box

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 μ conservation

 $p_{j\perp} > p_{j\parallel}$

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Example: Simulation with mi/me=128. Ion-cyclotron and mirror instabilities on ion Larmor radius scales. Whistler instability on electron Larmor radius scales.



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As long as $\beta_e \leq 10$ ($\beta_j \equiv 8\pi p_j/B^2$ is the ratio between the pressure of particles *j* and the magnetic pressure), the **electron anisotropy is dominated by the whistler instability alone**, with no influence of the ion-cyclotron and mirror instabilities.

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=> if $\beta_e \lesssim 10$ we can neglect the ion physics and study the physics of the whistler instability assuming immobile ions (as if they had infinite mass)



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- Initially there is growth of the background field that gives rise to the growth of electron pressure anisotropy.
- The anisotropy produces exponential growth and saturation of the whistler modes.
- After that, the anisotropy evolves in a quasi- stationary way.
- The anisotropy also gives rise to **anisotropic viscosity** ("AV"), that heats the plasma. It is possible to show that: $\frac{dU_i}{dt} = \Delta p_i q$



10-1

d)

d<U_>/dt [sP_]

(Kulsrud et al 1983)

where U_j is the internal energy of species *j*, and "*q*" is the growth rate of the magnetic field.

Electron acceleration:



• By the end of the simulation ($t \cdot s = 3$, equivalent to a magnetic amplification factor of ~3) the energy spectrum of the electrons contains a non-thermal tail that can be approximated as a power-law of spectral index $\alpha_s \sim 3.7$,

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But how is the acceleration produced?

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- The thermal electrons <u>give energy</u> to the whistler waves.
- The non-thermal electrons <u>receive energy</u> from the waves.





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• However, for a fixed value of $\beta_{e,init}$ the electrons can have different temperatures kT_e/m_ec^2 . We are currently studying this dependence Can **ions** also be accelerated stochastically?

2) Ion Acceleration: spectra in different β_i regimes

Thus, this change to a IC-dominated regime should produce a change in the resulting spectra of the ions:



 $(kT_i/m_ic^2=0.05)$

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Thus, this change to a IC-dominated regime should produce a change in the resulting spectra of the ions:



- In the IC-dominated, β_i =0.5 case there is a high energy tail that can be modeled as a **power-law plus** two bumps.
- The origin of the tail can be investigated by analyzing the way the particles in different parts of the tail gain their energy (similarly to what we did with electrons).





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- The electric field of the IC modes transfers energy from the thermal to the non-thermal ions.
- However, these results correspond to m_i/m_e=10 with ω_{c,i}/s=800. We need to push both parameters towards more realistic values. (At ~ 10 Schwarzschild radii in Sgr A*, ω_{c,i}/s~ 10⁸ [e.g., Ponti et al 2017]).





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- Also little difference when increasing magnetization
- Although some trend to make the spectra slightly harder for larger ω_{ci}/s .
- Another interesting and final test:

What happens if the IC modes are driven by **plasma compression instead of shearing**?

2) Ion Acceleration: Testing the process using compressing box

Setup of Sironi et al 2015

Case with

- β_i=0.5, •
- •
- $kT_i/m_ic^2=0.05$, $m_i/m_e=8$ and 16 •
- $\omega_{c,i}/s=1600$ and 3200 •





- Essentially no difference between mi/me=8 and 16.
- Little difference between $w_{c,i}/s=1600$ and 3200 (a bit harder when $w_{c,i}/s=3200$).
- The amplification mechanism (shear or compression) does not matter!

Conclusions

- Pressure anisotropy-driven, kinetic instabilities can accelerate ions and electrons stochastically in low-luminosity (weakly collisional) accretion disks.
- For two specific cases with initial β_j ~ 1 (j =i and e), and after the magnetic field is amplified by a factor of ~3, these spectra can be approximately modeled by
 - i) Case of electrons: a power-law of index ~3.7, which is close to what radio observations suggest for Sgr A* (e.g., Yuan et al. 2003). [Riquelme et al 2017]
 - ii) Case of ions: a power-law of index ~3.4 + two bumps. Largest Lorentz factor ~10.
 [Ley et al 2019]
- Open Questions:
 - i) How does this process depend on the **plasma parameters**: kT_j/m_jc^2 and ω_{cj}/ω_{pj} (j=i and e)?

ii) Long(er) term evolution: what happens if these processes occur many times due to turbulence?

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Thanks!