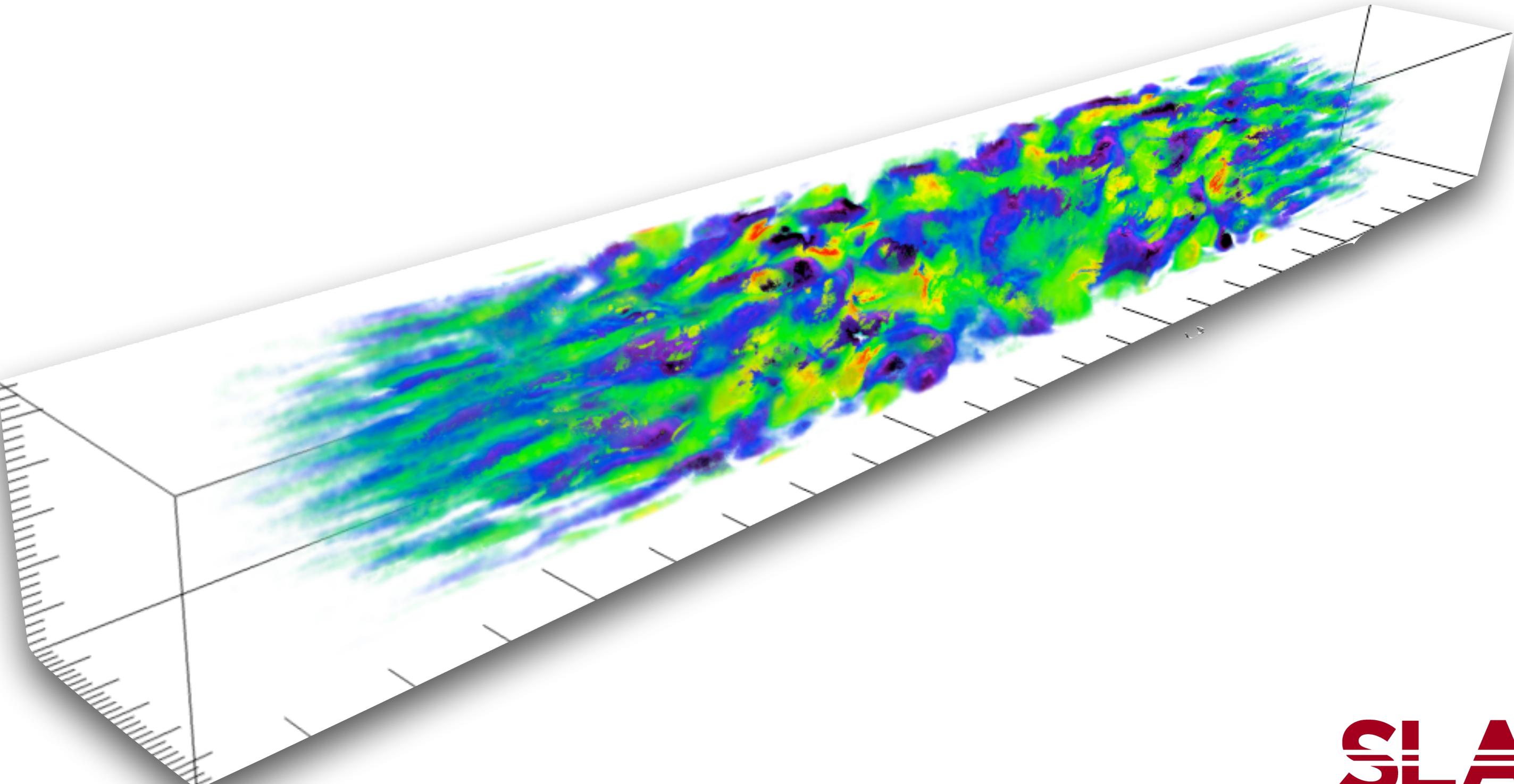


Particle acceleration in shocks: from simulations to observations via laboratory experiments

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Acknowledgements

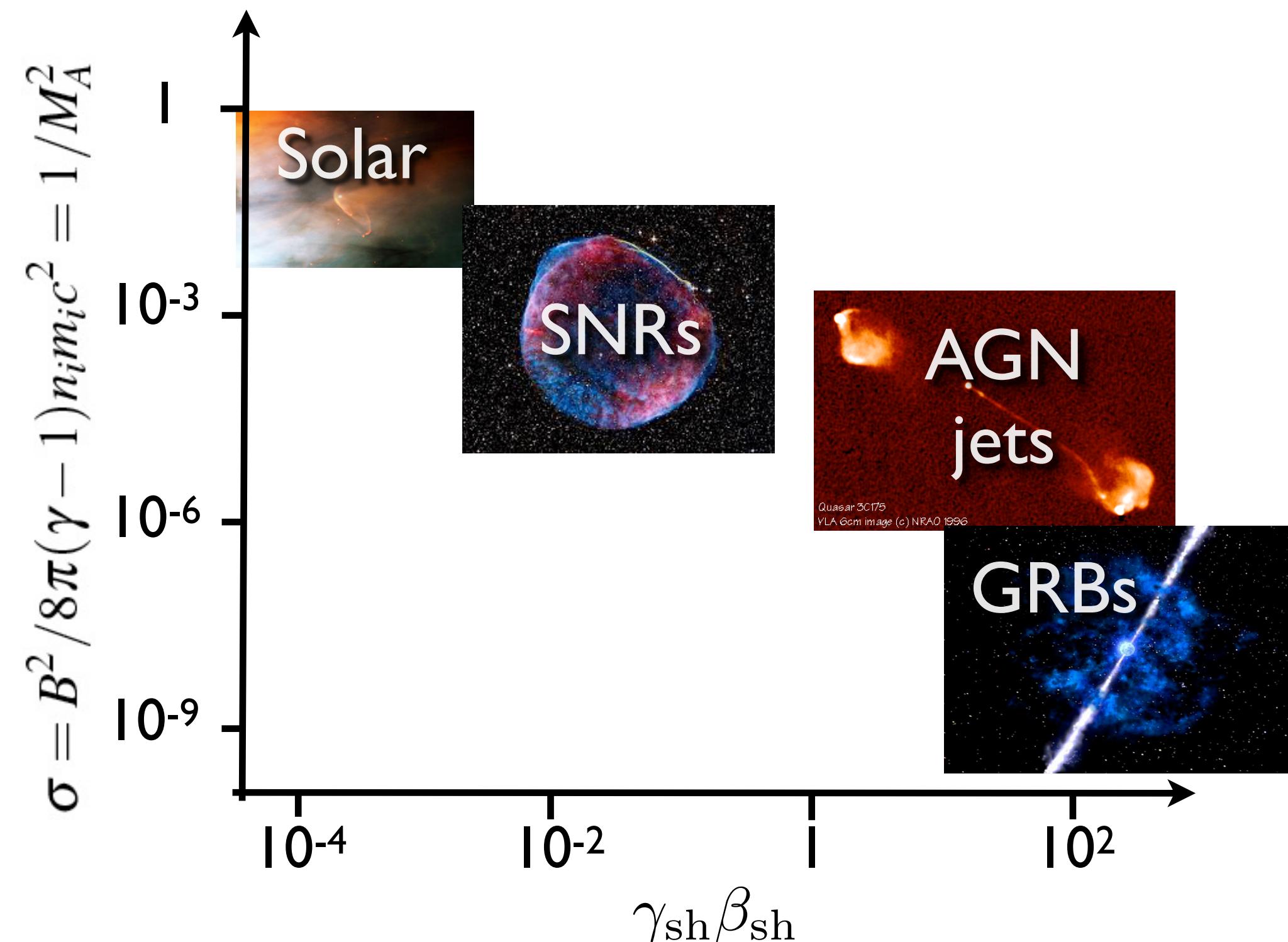


- Work in collaboration with
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 - A. Spitkovsky (Princeton)
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 - G. Gregori (Oxford)
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 - S. Funk (Erlangen)
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- Financial support from the DOE Early Career Research Program

Shock microphysics is important to understand particle acceleration

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- Astrophysical shocks are efficient accelerators of both electrons and protons (cosmic rays)
- Theory of diffusive shock acceleration (DSA) is well established*
- However, injection of particles at the shock and magnetic field amplification is not fully understood and impact overall efficiency and maximum energy
- Observations (in particular, multi-wavelength) provide critical constrains on models for acceleration but shock microphysics is still not resolved
- Spacecraft measurements provide important characterization of microphysics but mostly for low Mach # shocks ($M_{sh} < 10$)



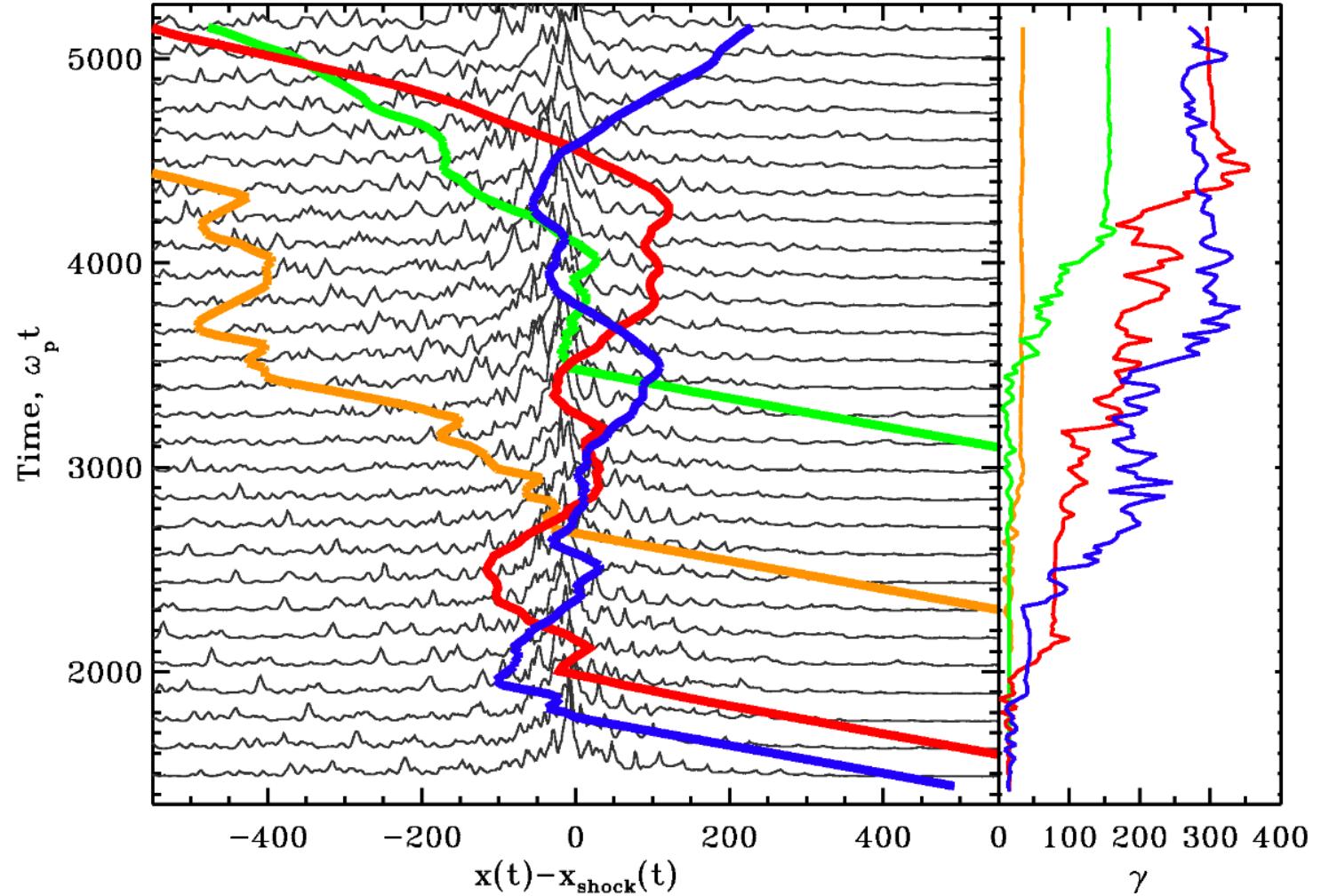
* Krymskii 1977, Axford, Leer, Skadron 1977, Bell 1978, Blandford & Ostriker 1978, Drury 1983

Kinetic simulations are important to study injection physics at the shock

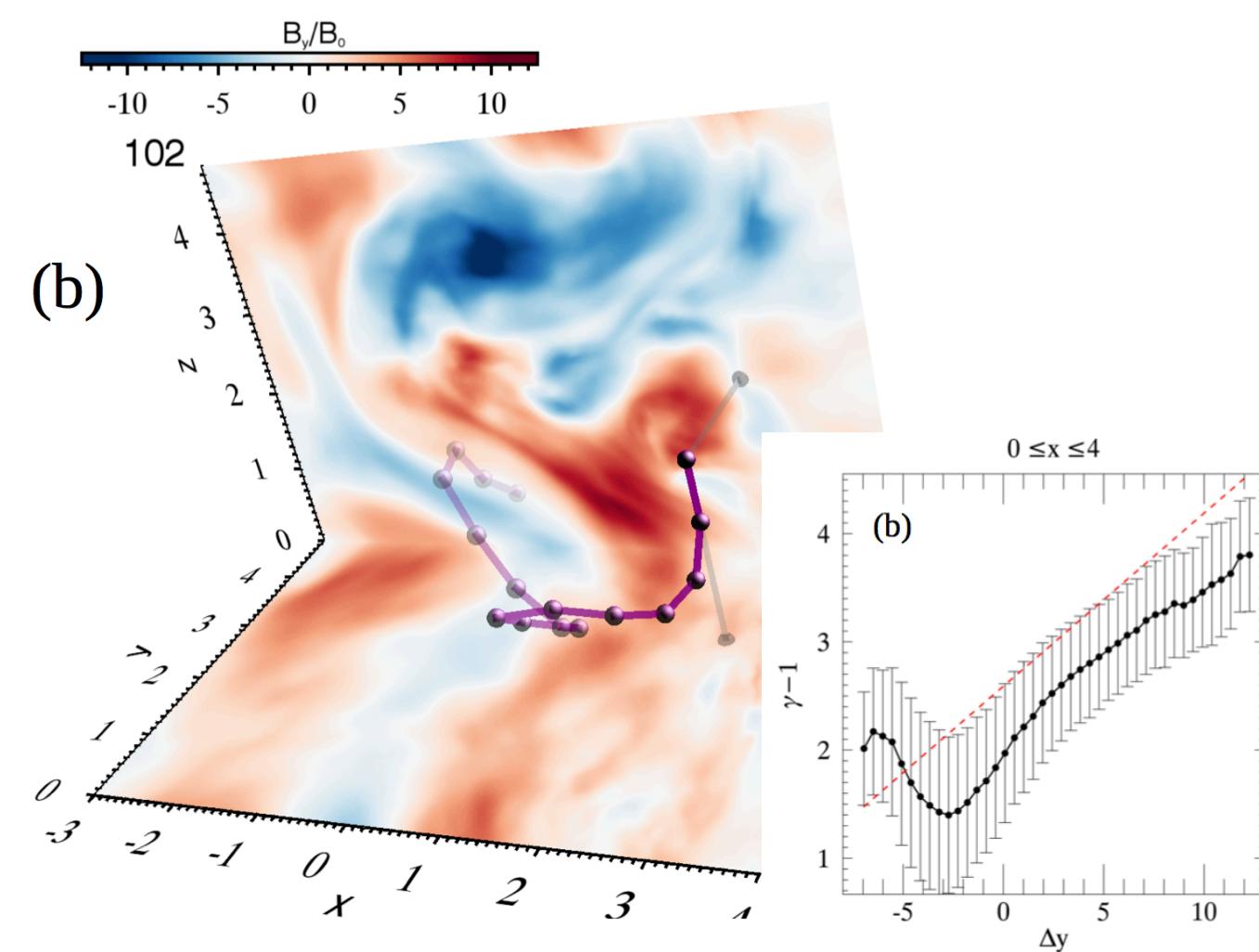
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- Particle-in-cell (PIC) simulations have been established over the last decades as critical tool to study acceleration in electromagnetic shocks
- For high- M_A shocks role of ambient field might be reduced and self-generated waves/magnetic turbulence (Weibel, Buneman, Bell...) control injection at shock structure

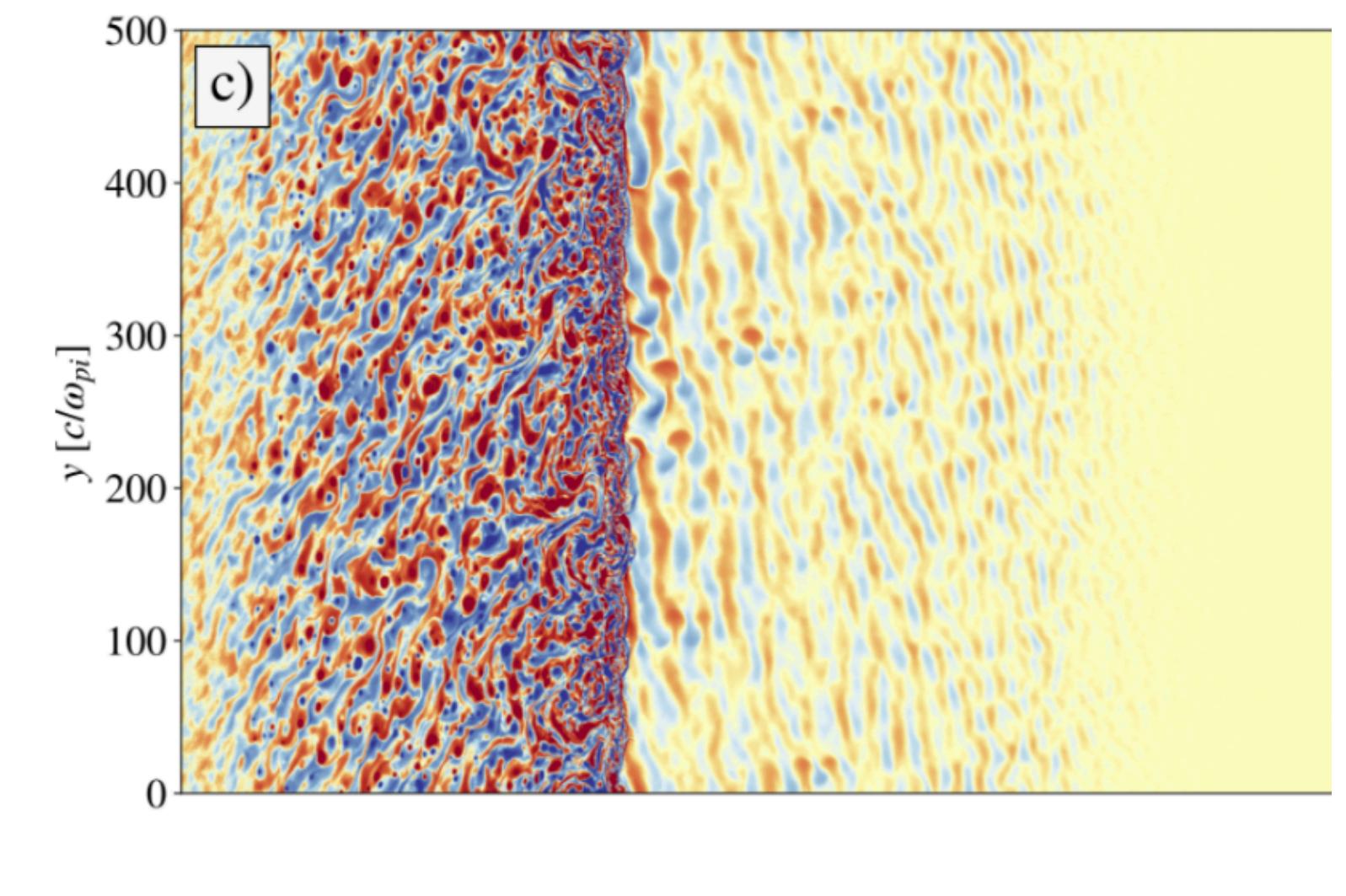
Acceleration in relativistic Weibel shocks [1]



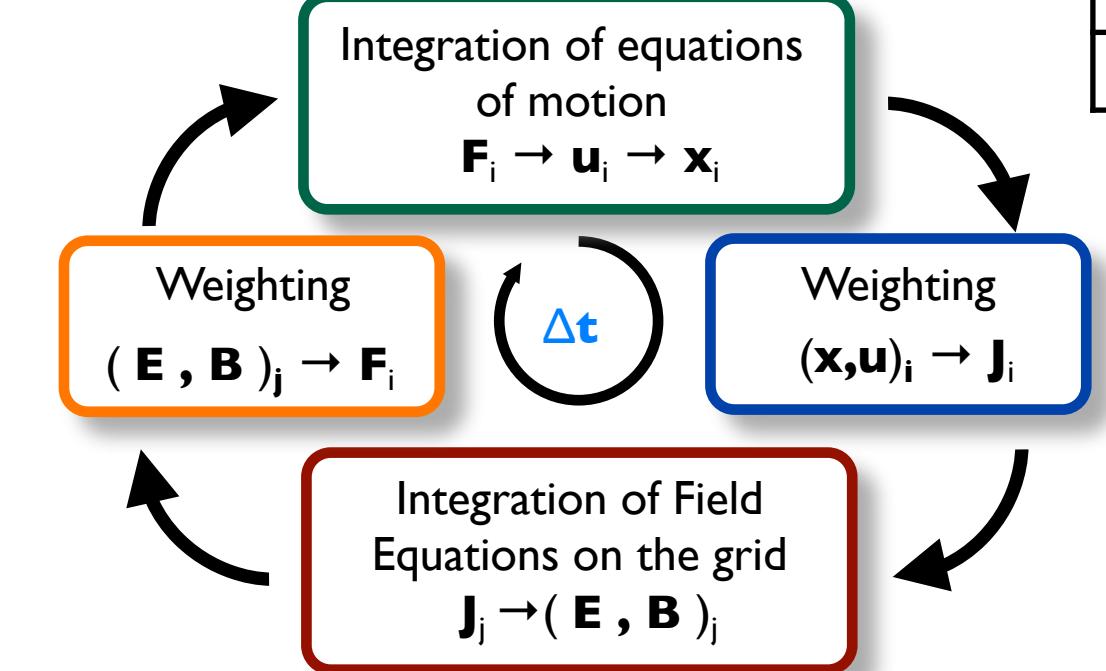
Stochastic SDA in Weibel turbulence
in perpendicular shocks [2]



Injection by Bell waves in parallel shocks [3]



$$\frac{d\mathbf{u}}{dt} = \frac{q}{m} \left(\mathbf{E} + \frac{1}{\gamma c} \mathbf{u} \times \mathbf{B} \right)$$

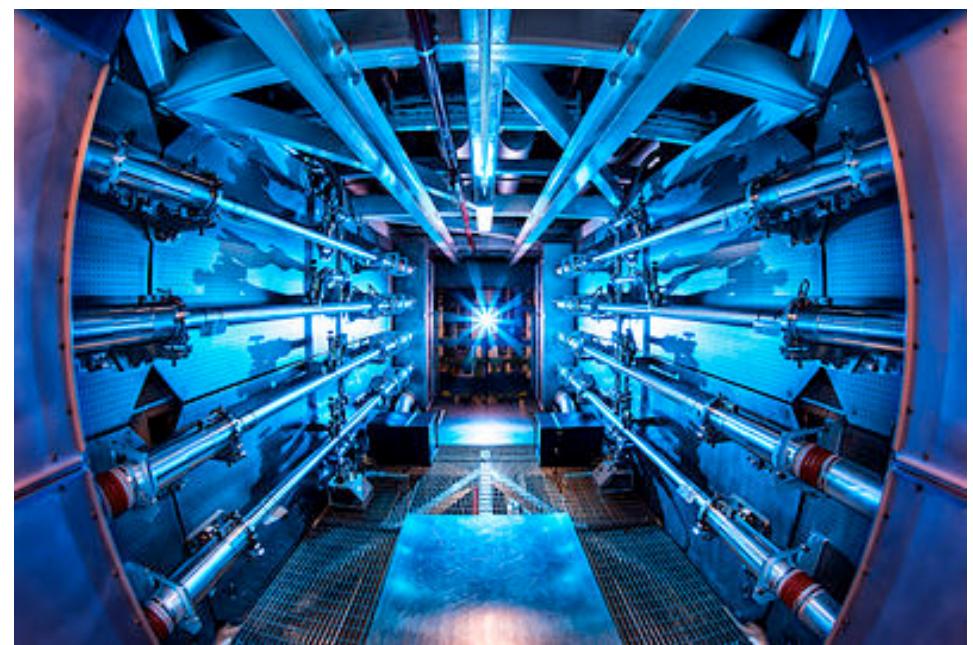


$$\frac{\partial \mathbf{E}}{\partial t} = c \vec{\nabla} \times \mathbf{B} - 4\pi \mathbf{j} \quad \frac{\partial \mathbf{B}}{\partial t} = -c \vec{\nabla} \times \mathbf{E}$$

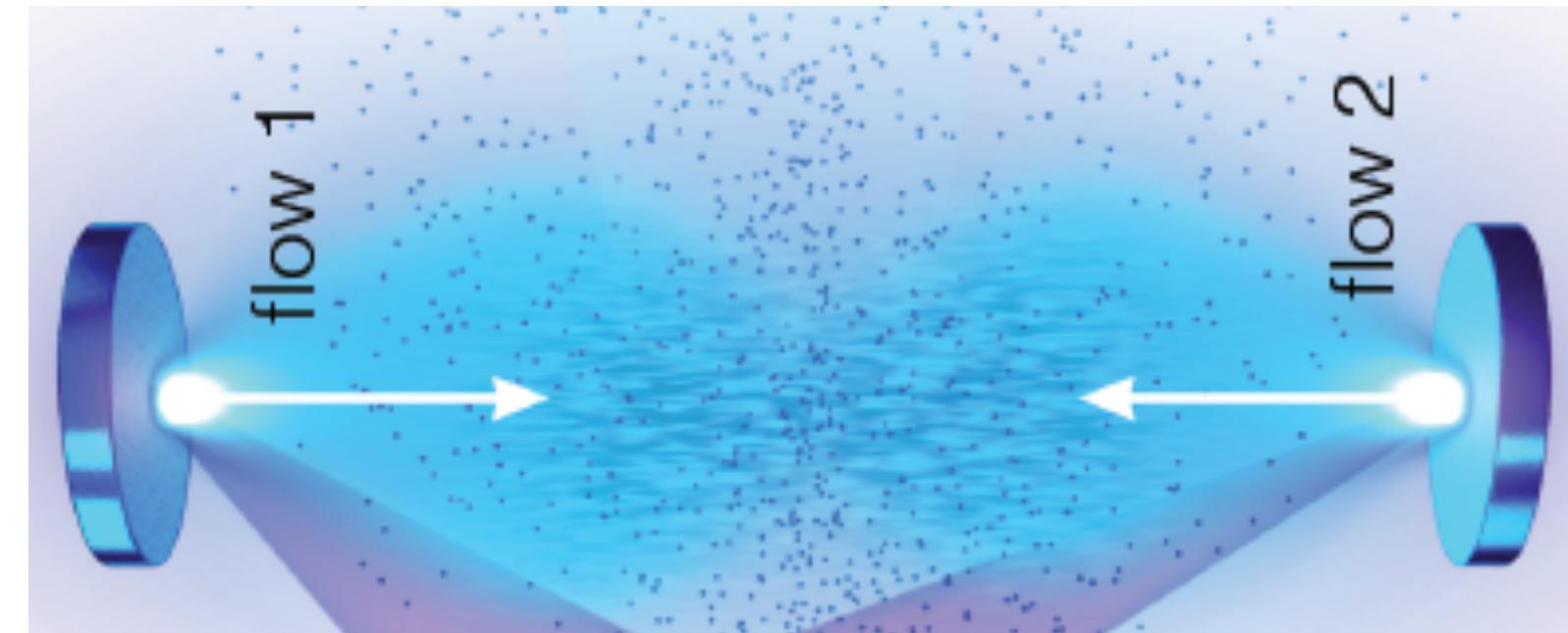
Laboratory experiments can complement studies of particle acceleration

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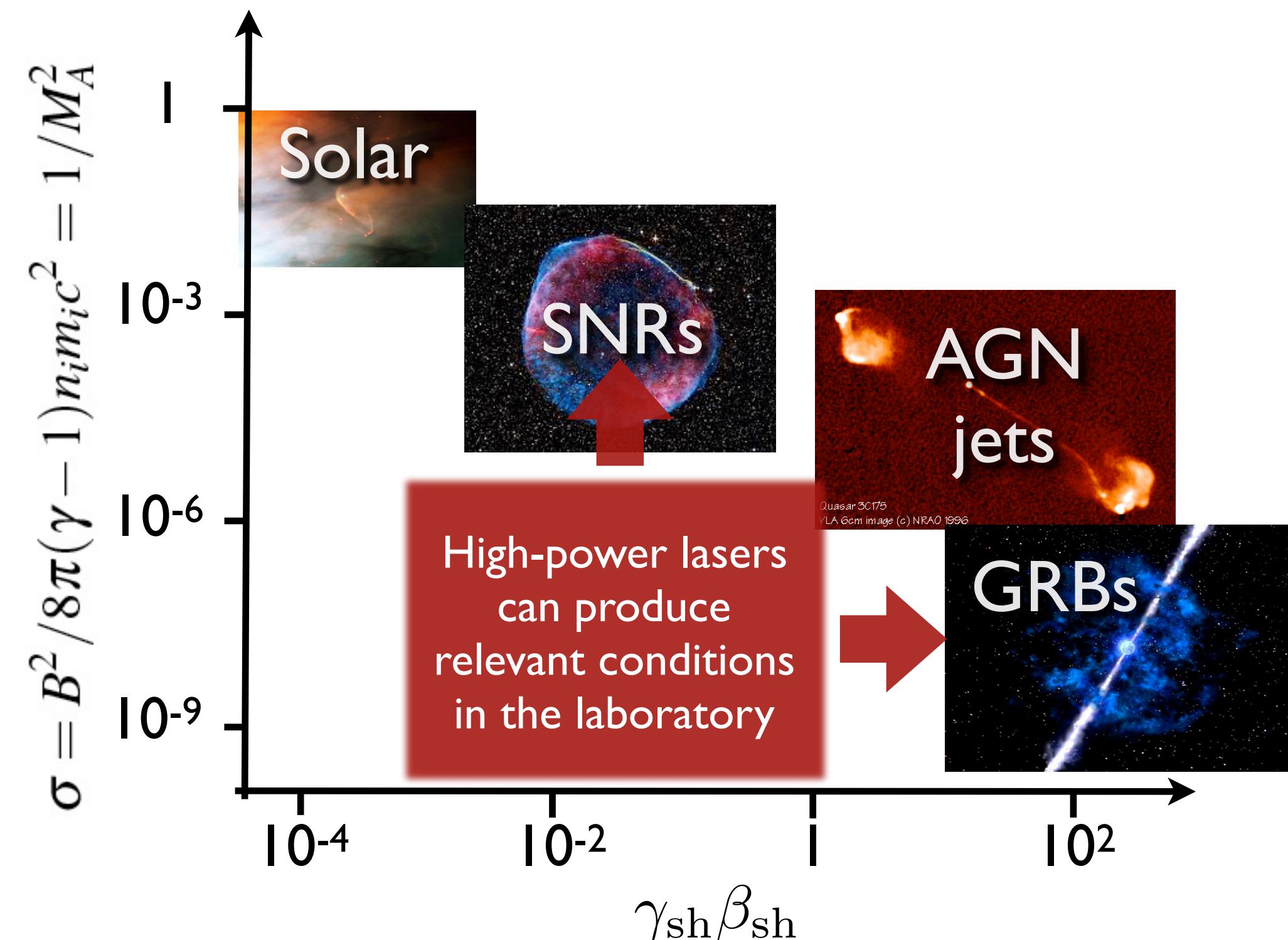
- Significant experimental studies of ion-acoustic shocks since 60s
- Only now it is becoming possible to drive energetic enough plasma flows with lasers to produce electromagnetic shocks
($L_{\text{system}} > 100 c/\omega_{\text{pi}}$ and $\lambda_{\text{mfp}} \gg L_{\text{system}}$)
- Controlled study of shock structure and particle acceleration for different plasma conditions (including high M_{sh})
- Benchmark numerical tools that are being used to develop injection models



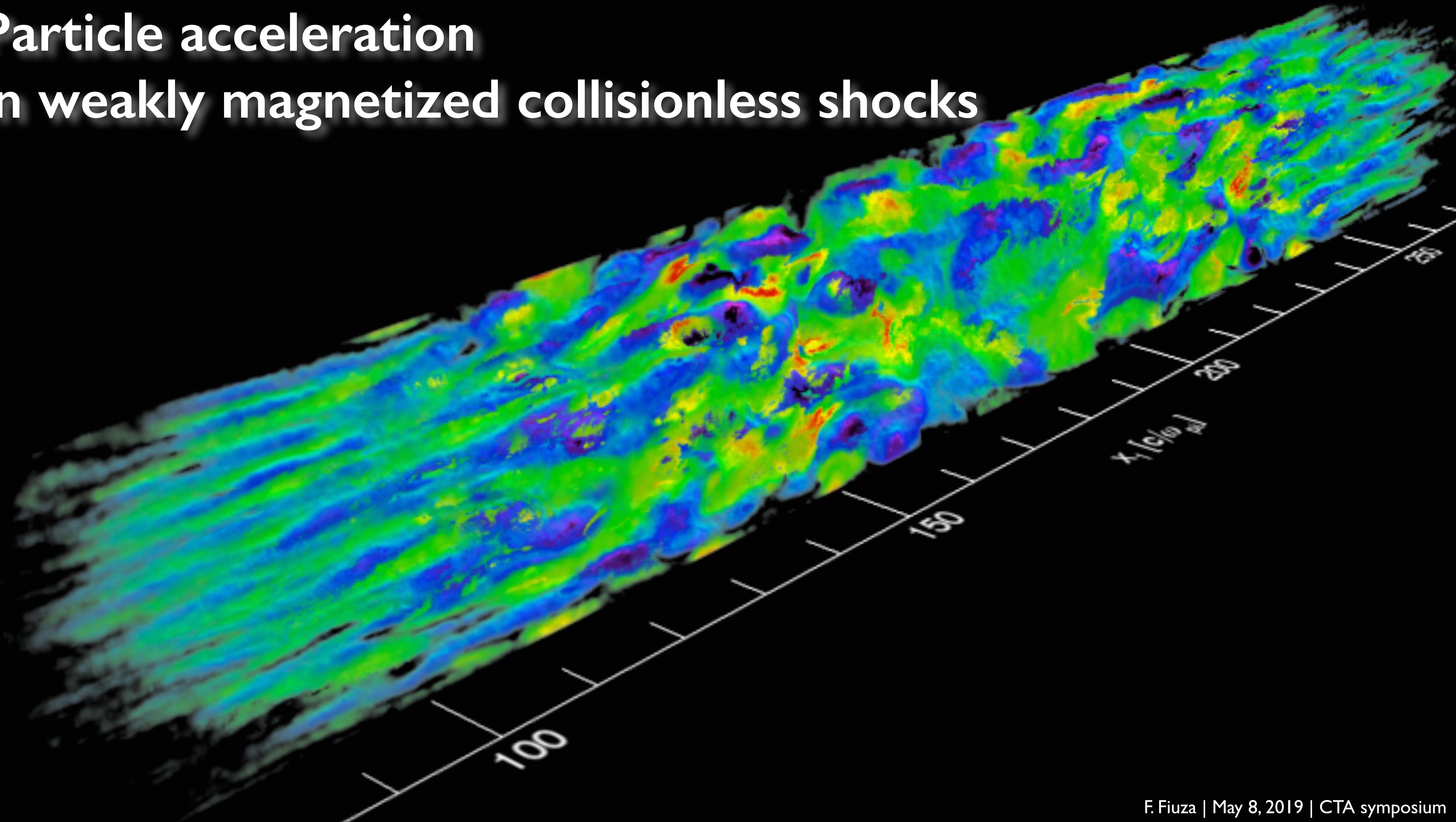
National Ignition Facility



Cartoon of laser-driven counter-streaming plasma experiments

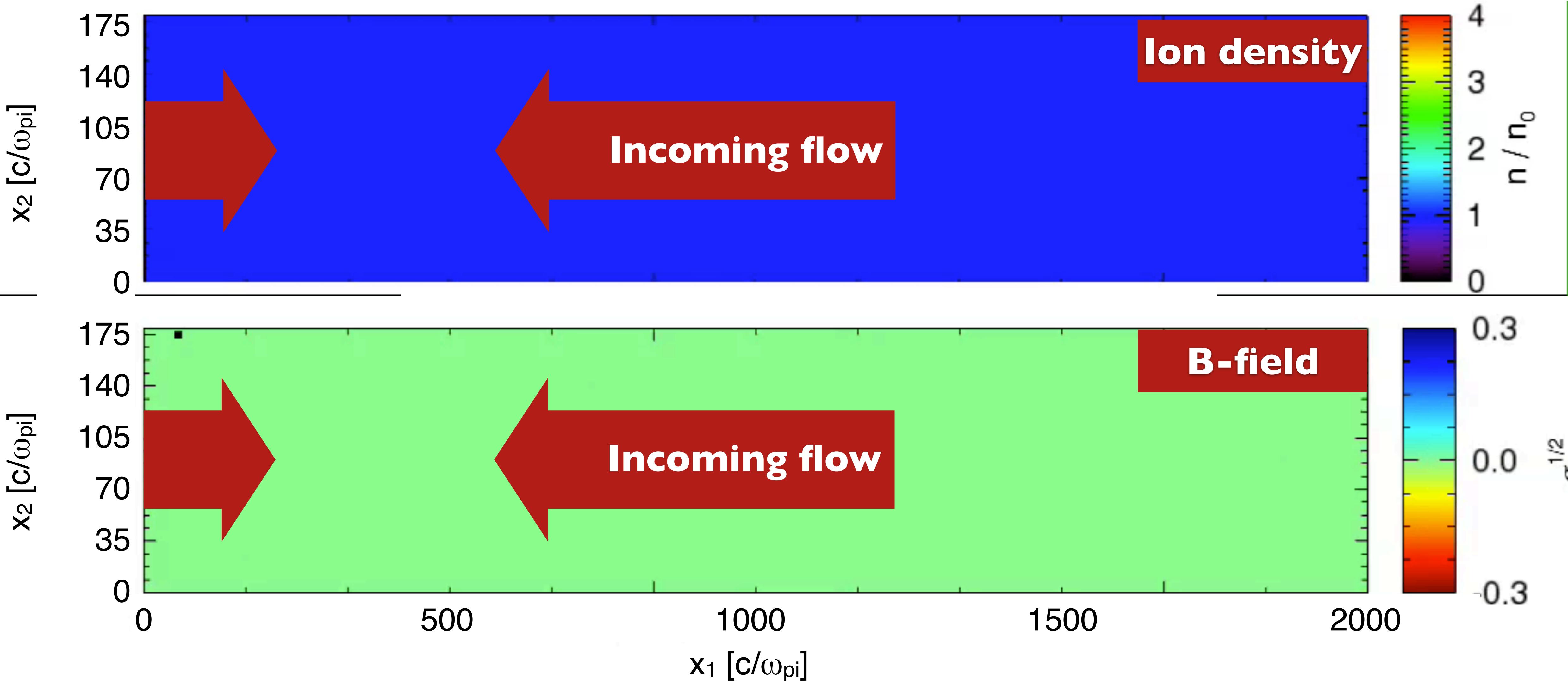


Particle acceleration in weakly magnetized collisionless shocks



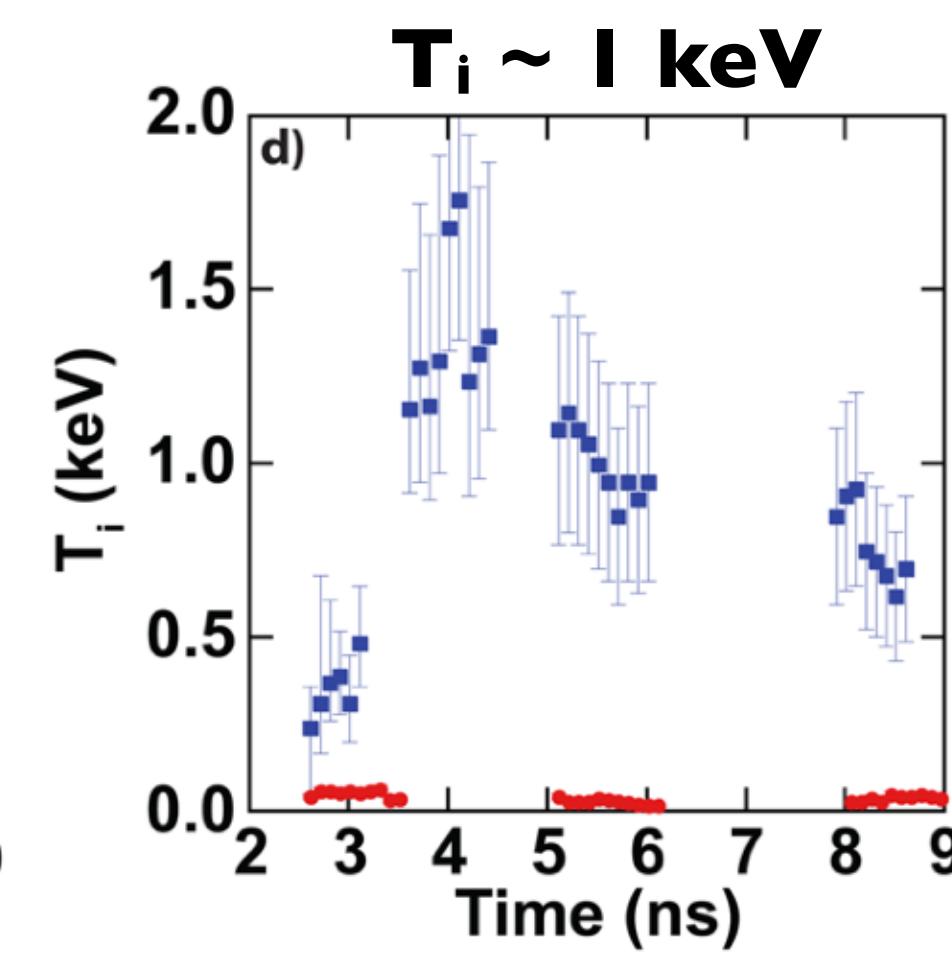
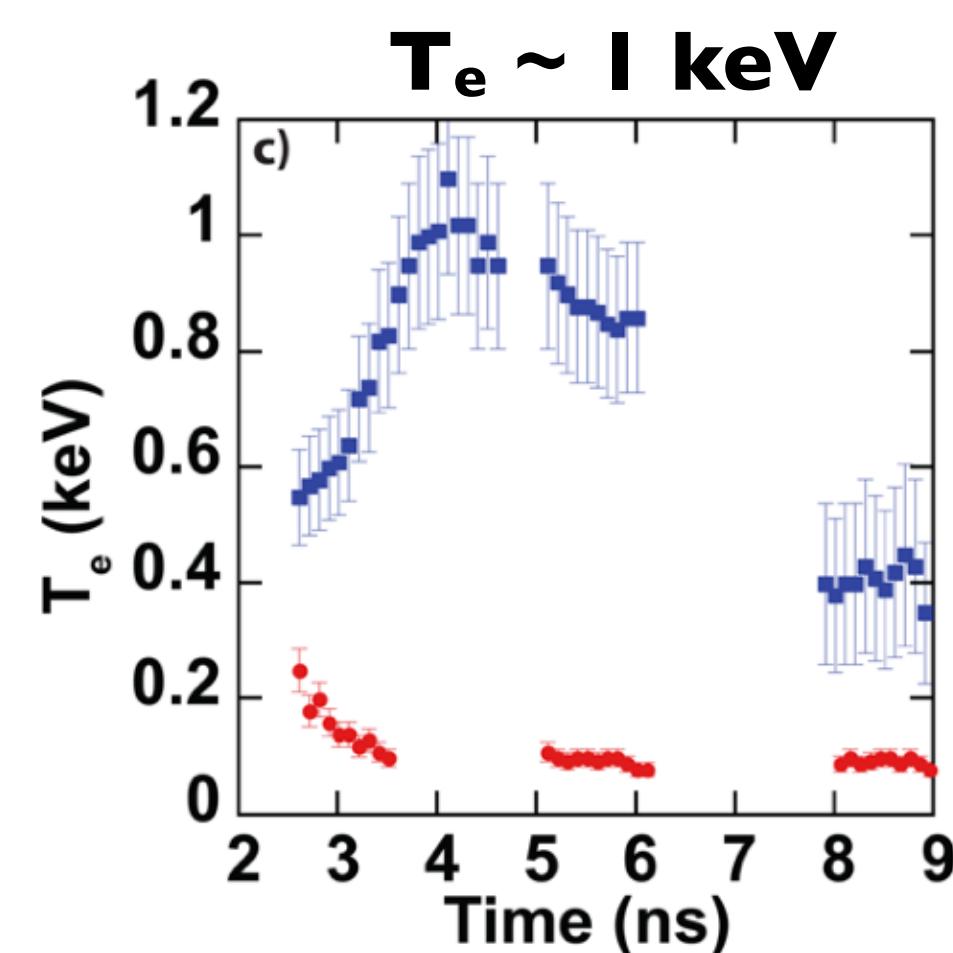
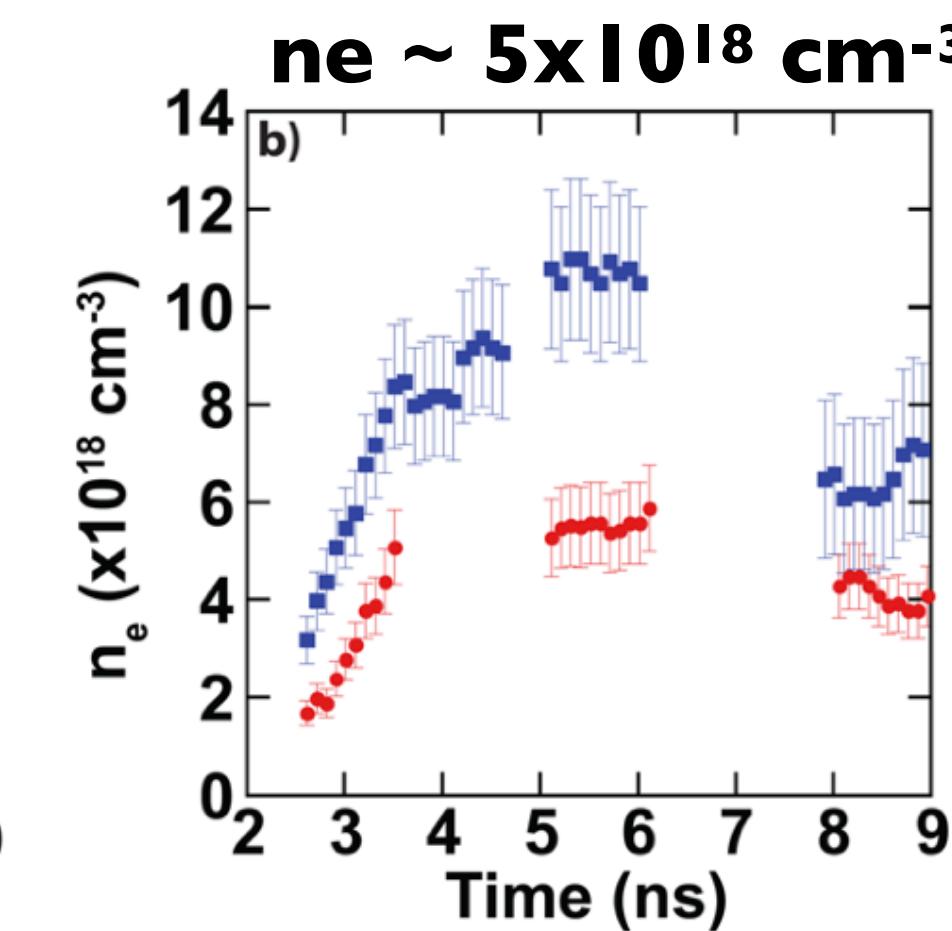
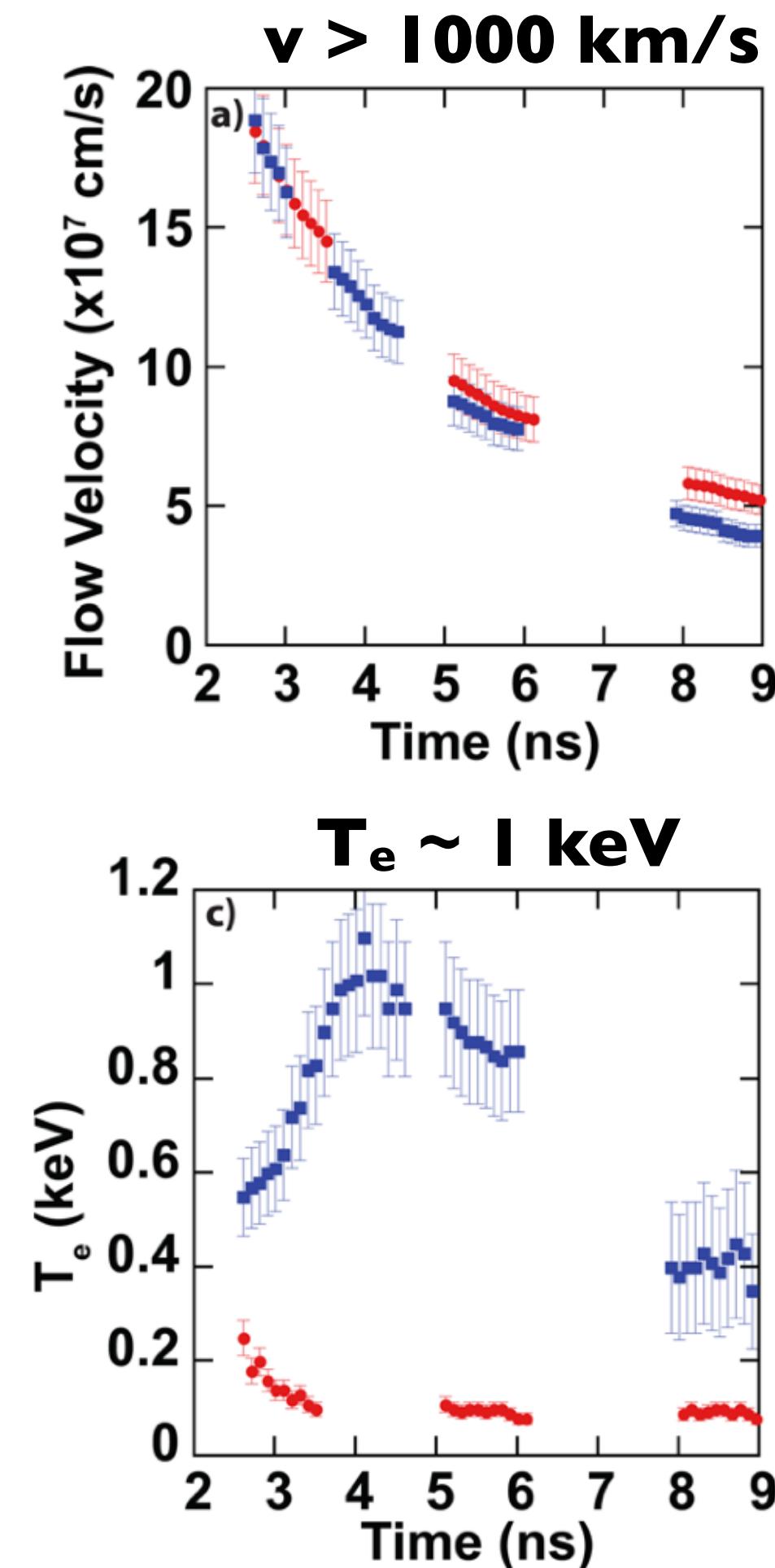
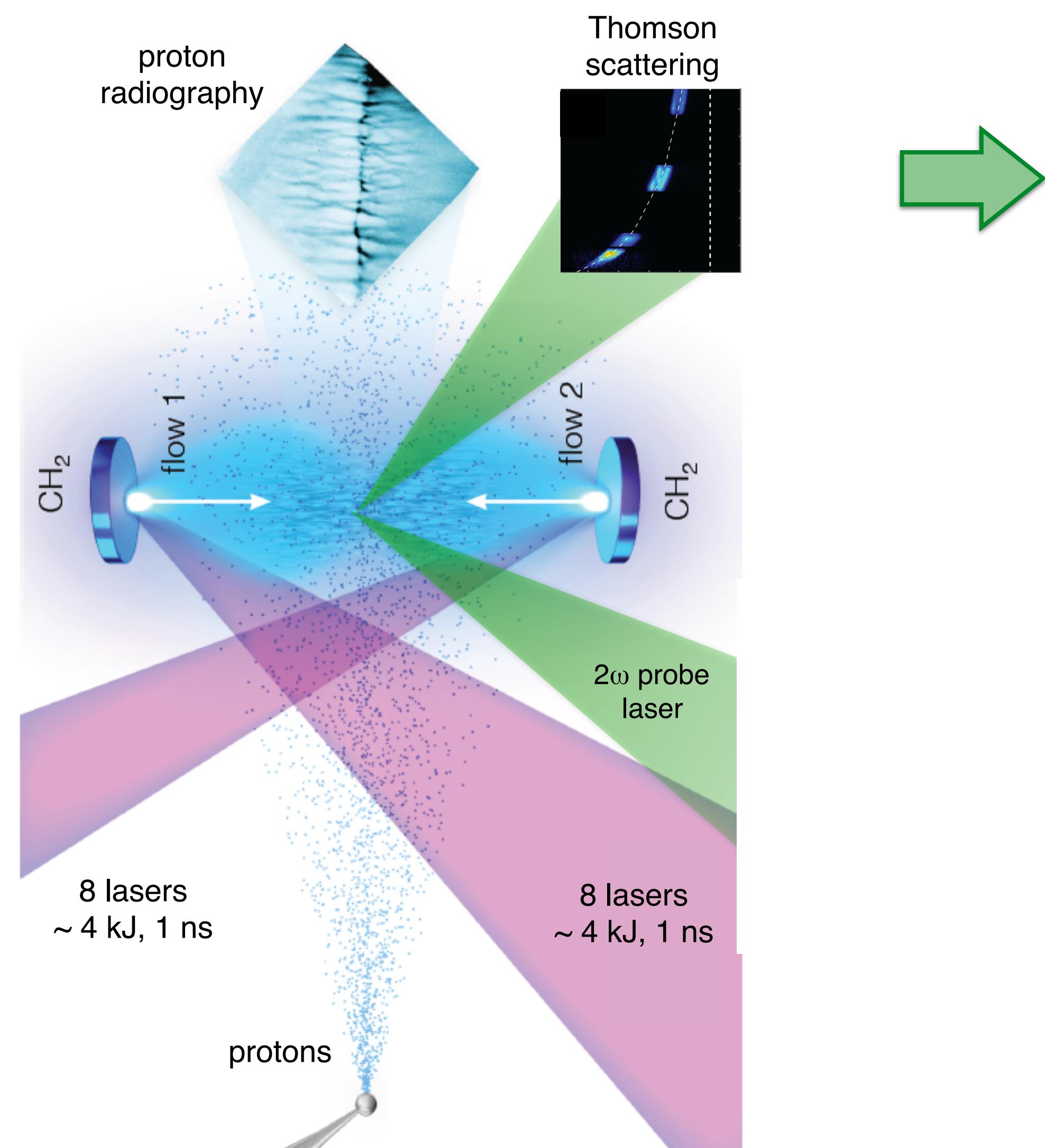
Formation of collisionless shocks in weakly magnetized plasmas

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High Mach # plasma flows can be created in the lab by laser irradiation

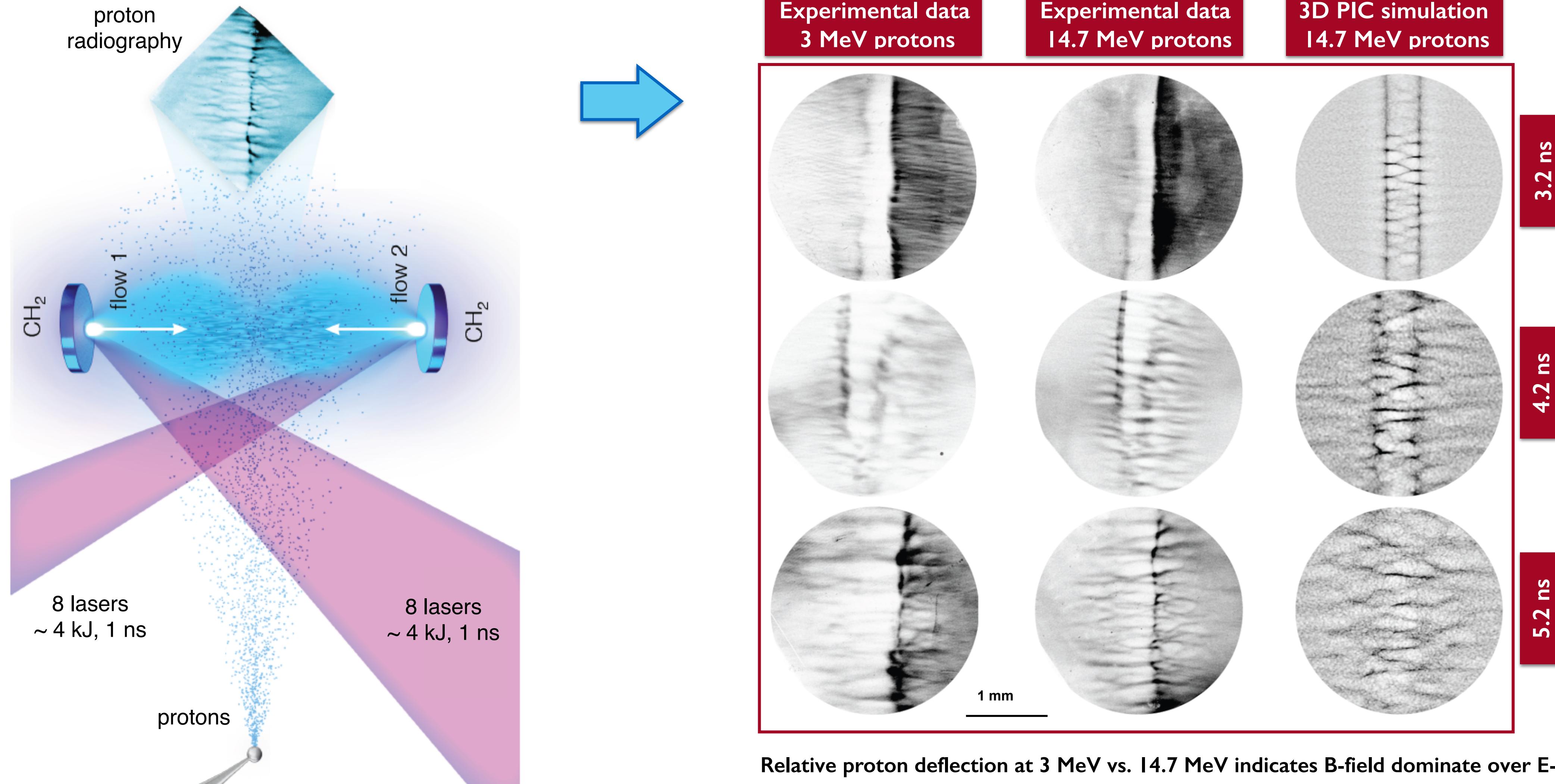
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Collisionless interaction with $\lambda_{\text{mfp}} > 10 L_{\text{system}}$

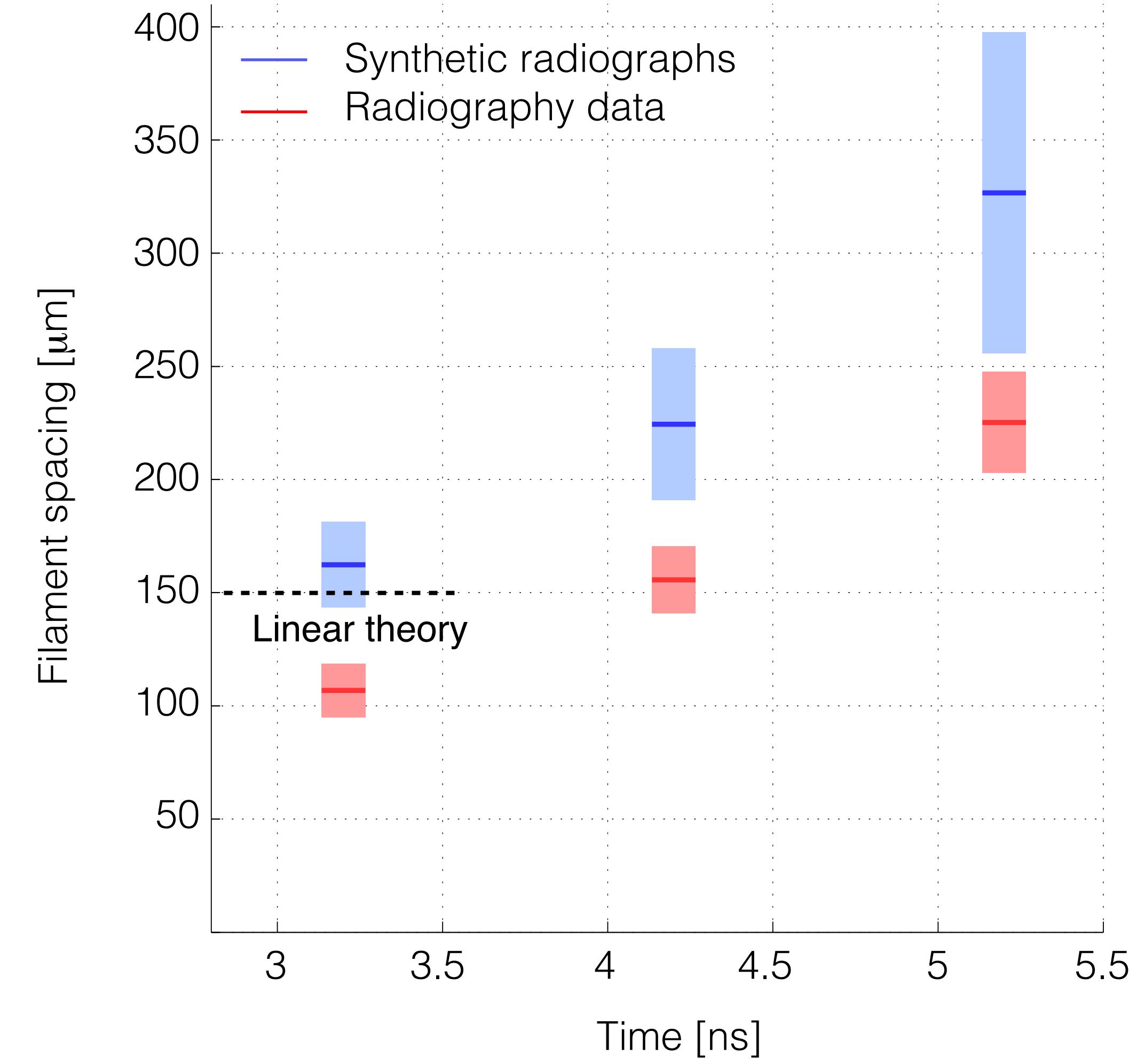
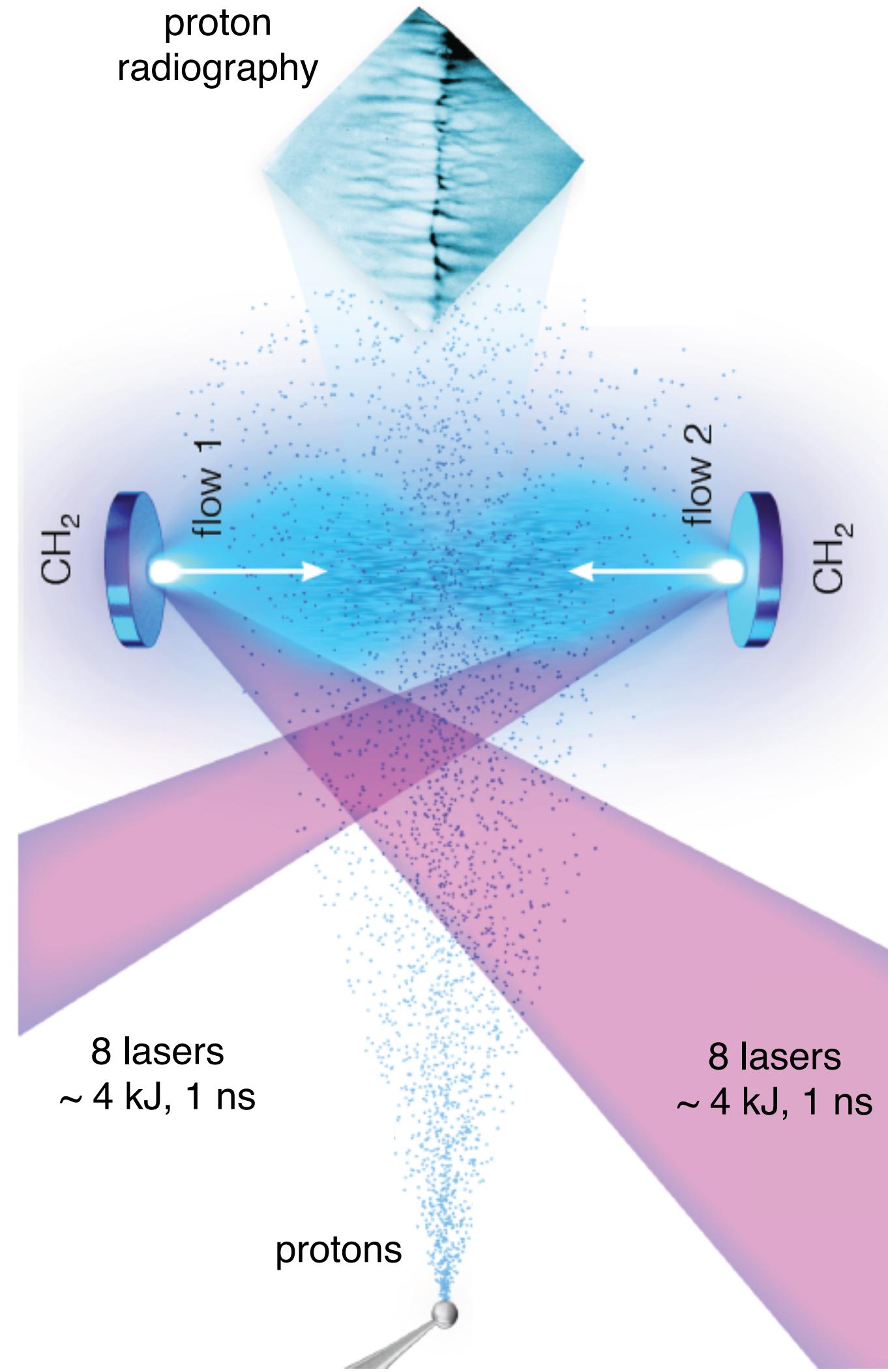
B-field amplification by the ion Weibel instability observed

SLAC



B-field amplification by the ion Weibel instability observed

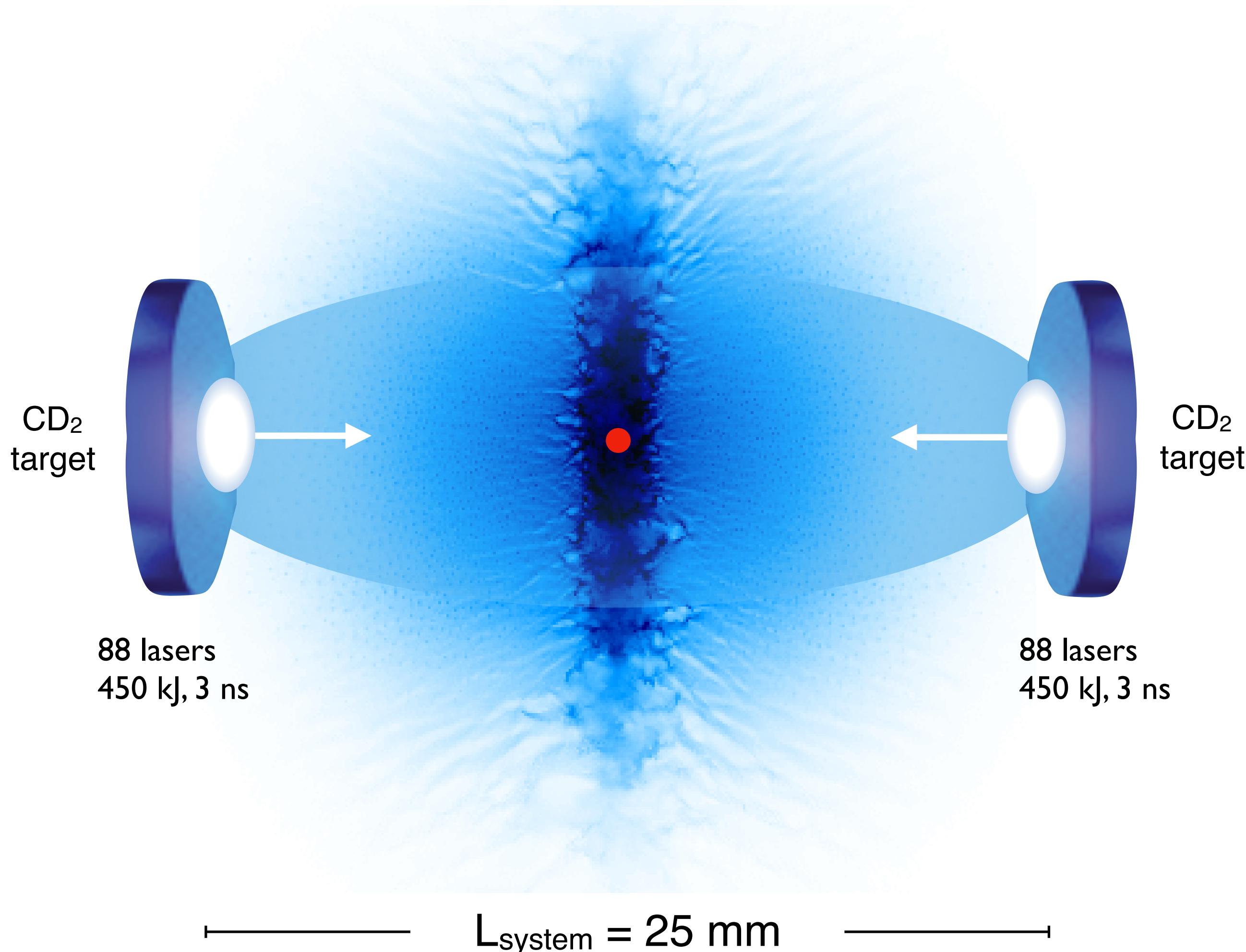
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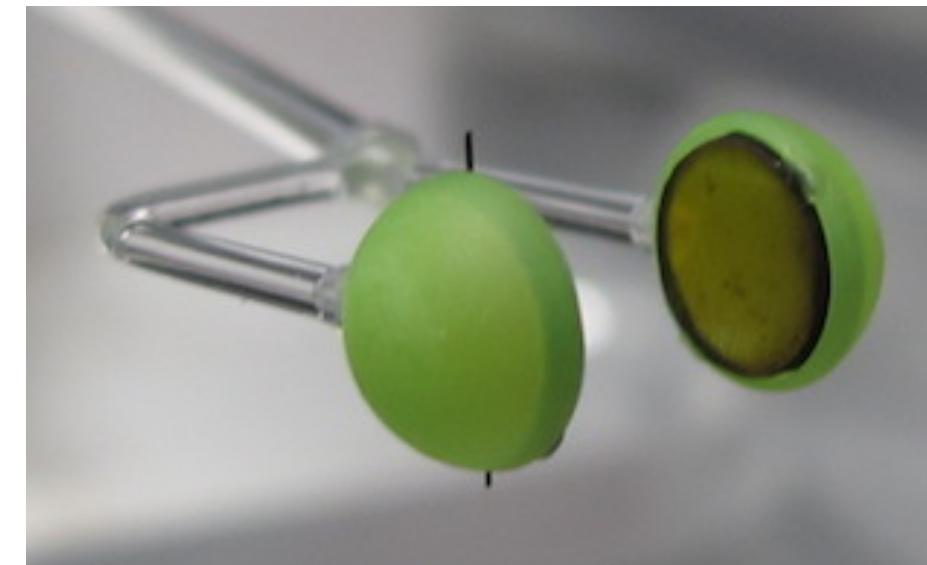
Platform to study shock formation and particle acceleration at NIF

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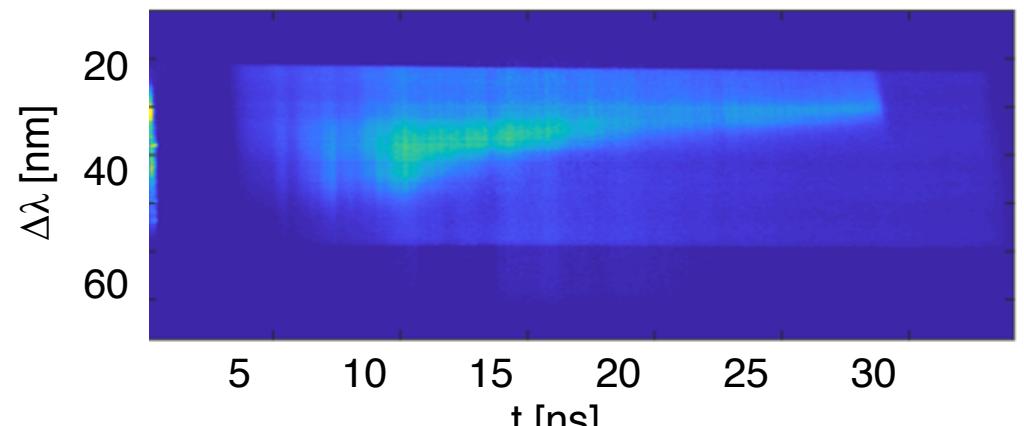
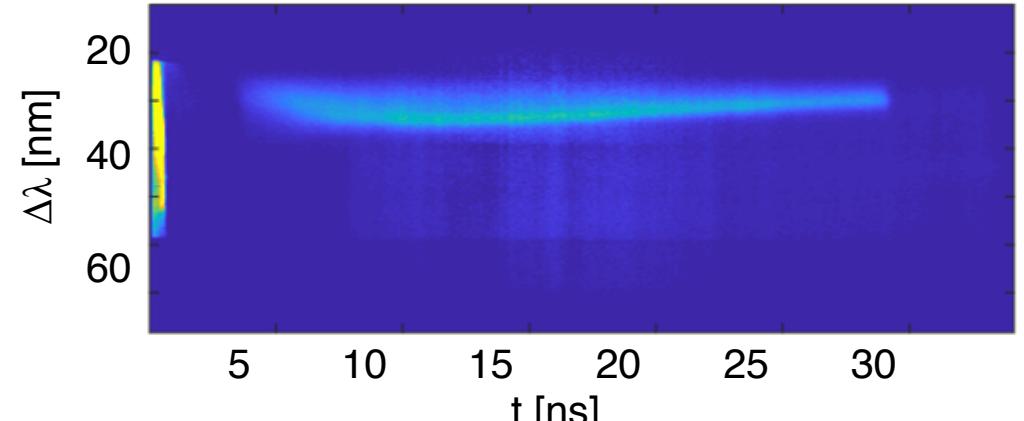
NIF laser system delivers $\sim 1\text{MJ}$ in 190 beams



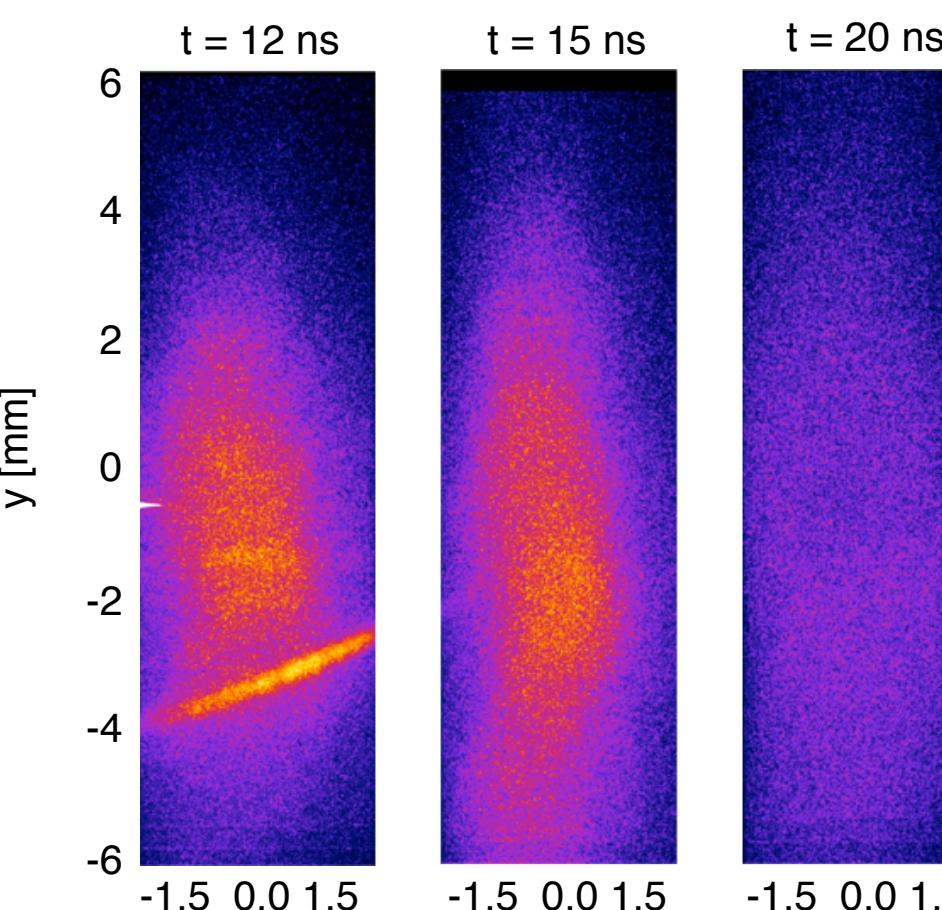
CD₂ targets



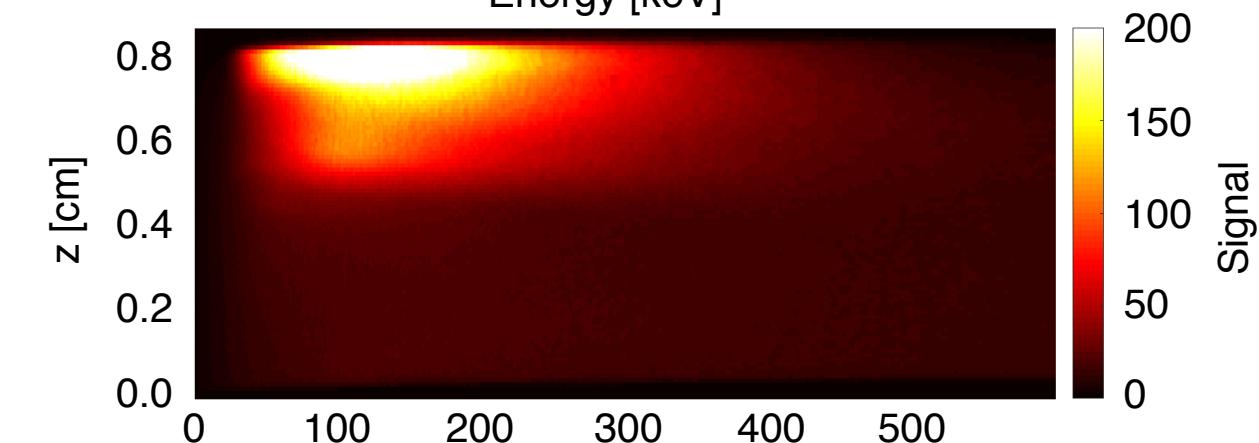
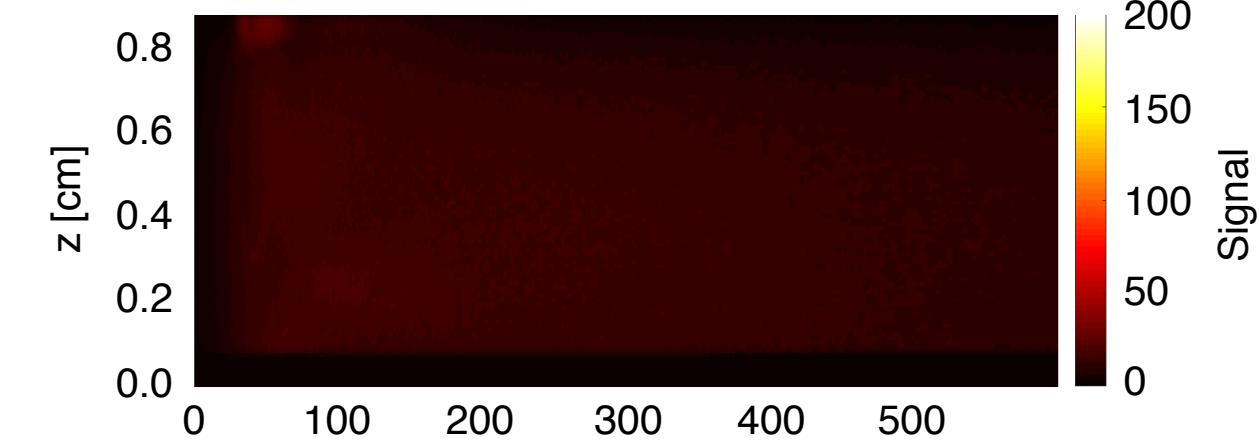
Thomson scattering



Plasma X-ray self emission



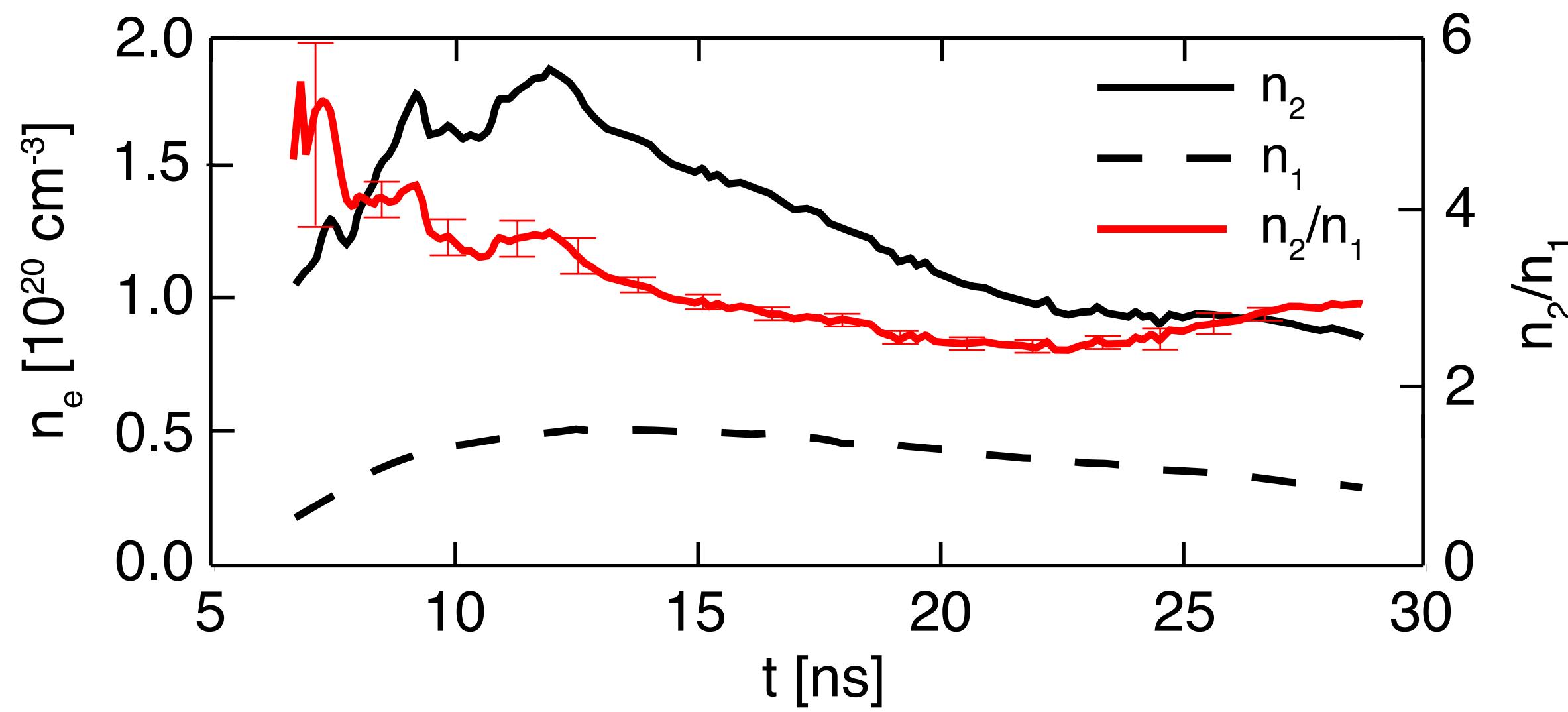
Electron magnetic spectrometer



Experimental observation of collisionless shock formation

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Density evolution of shocked plasma



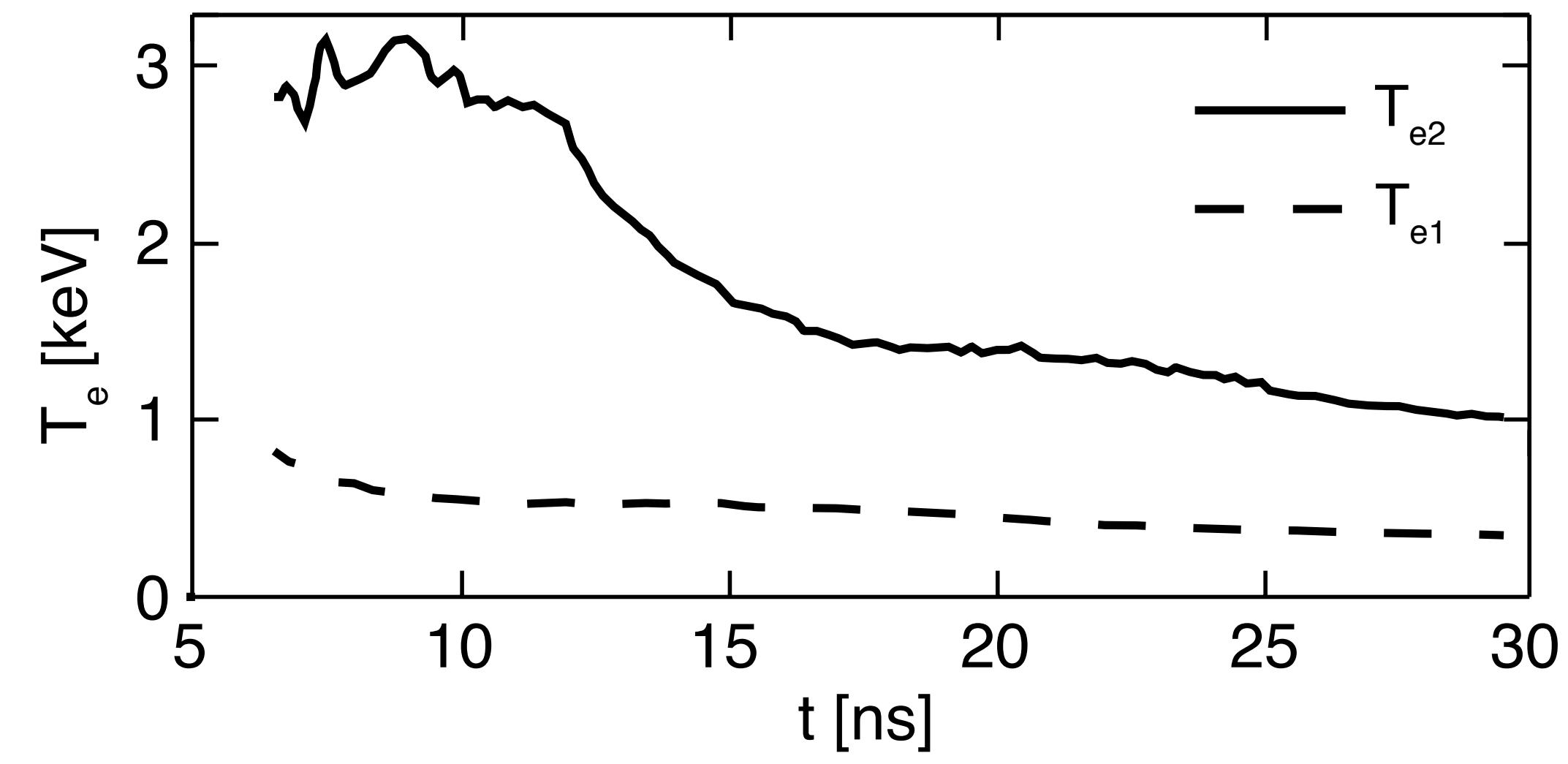
$$v_{\text{flow}} = c_{S1} + \frac{1}{2} \frac{L_{\text{system}}}{t} \simeq 1750 \text{ km/s}$$

$$\frac{n_2}{n_1} = \frac{(\gamma+1)M^2}{2+(\gamma-1)M^2} \sim 4 \quad M_{sh} \sim 15$$

$$L_{m.f.p.} \simeq 10^{-12} \frac{A^2 v_{\text{flow}}^4}{Z^4 n_i} \simeq 21 \text{ cm} \gg L_{\text{system}}$$

Observed shock is collisionless!

Temperature evolution of shocked plasma



$$\frac{1}{2} m_i v_{\text{flow}}^2 \simeq \frac{3}{2} k_B (T_i + Z T_e)$$

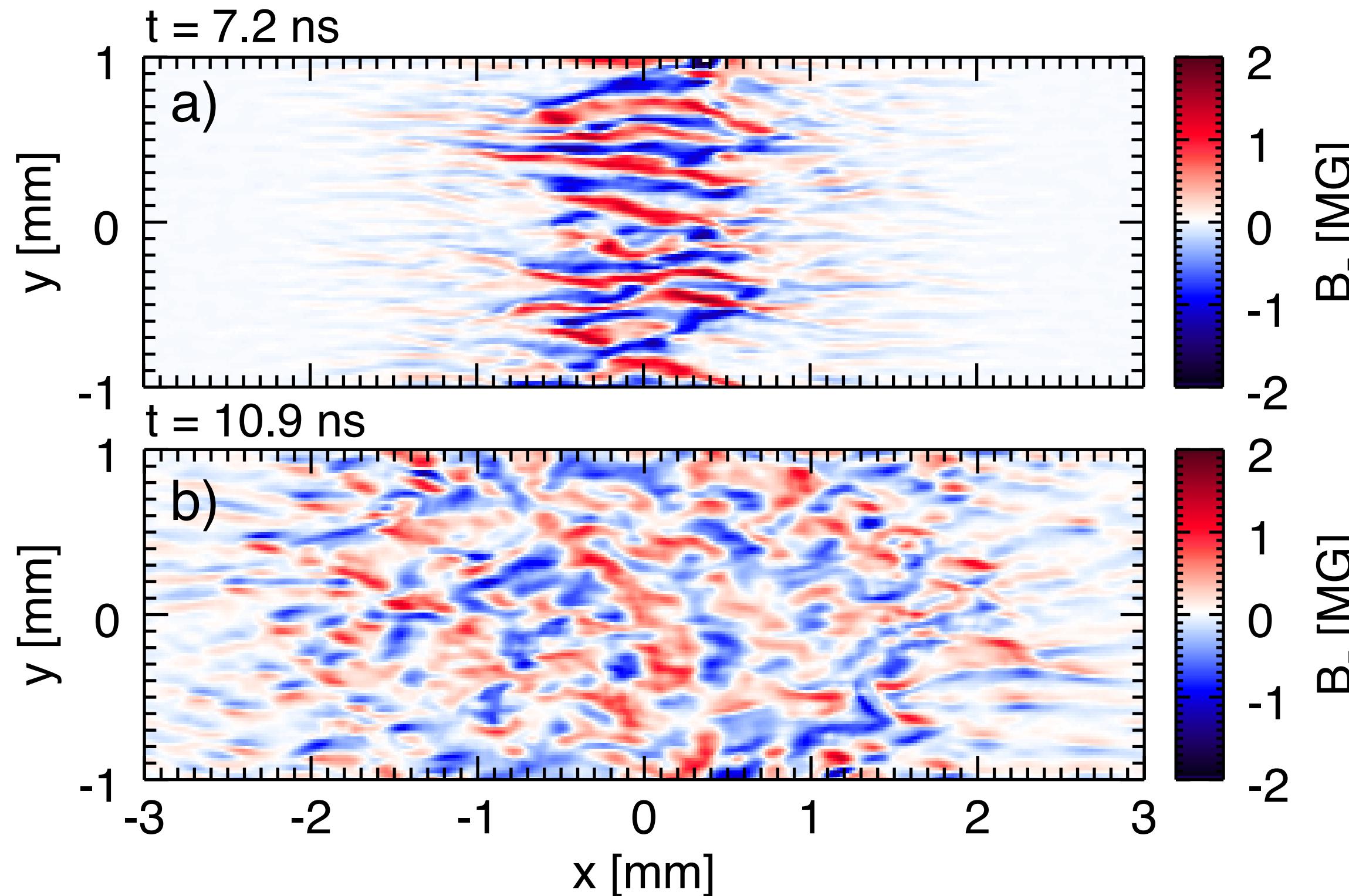
$$\frac{T_e}{T_i} = \frac{0.34}{A}$$

Temperature ratio consistent with previous observations of SNR shocks (Rakowski 2003, 2006)

Simulations show consistent Weibel-mediated shock structure

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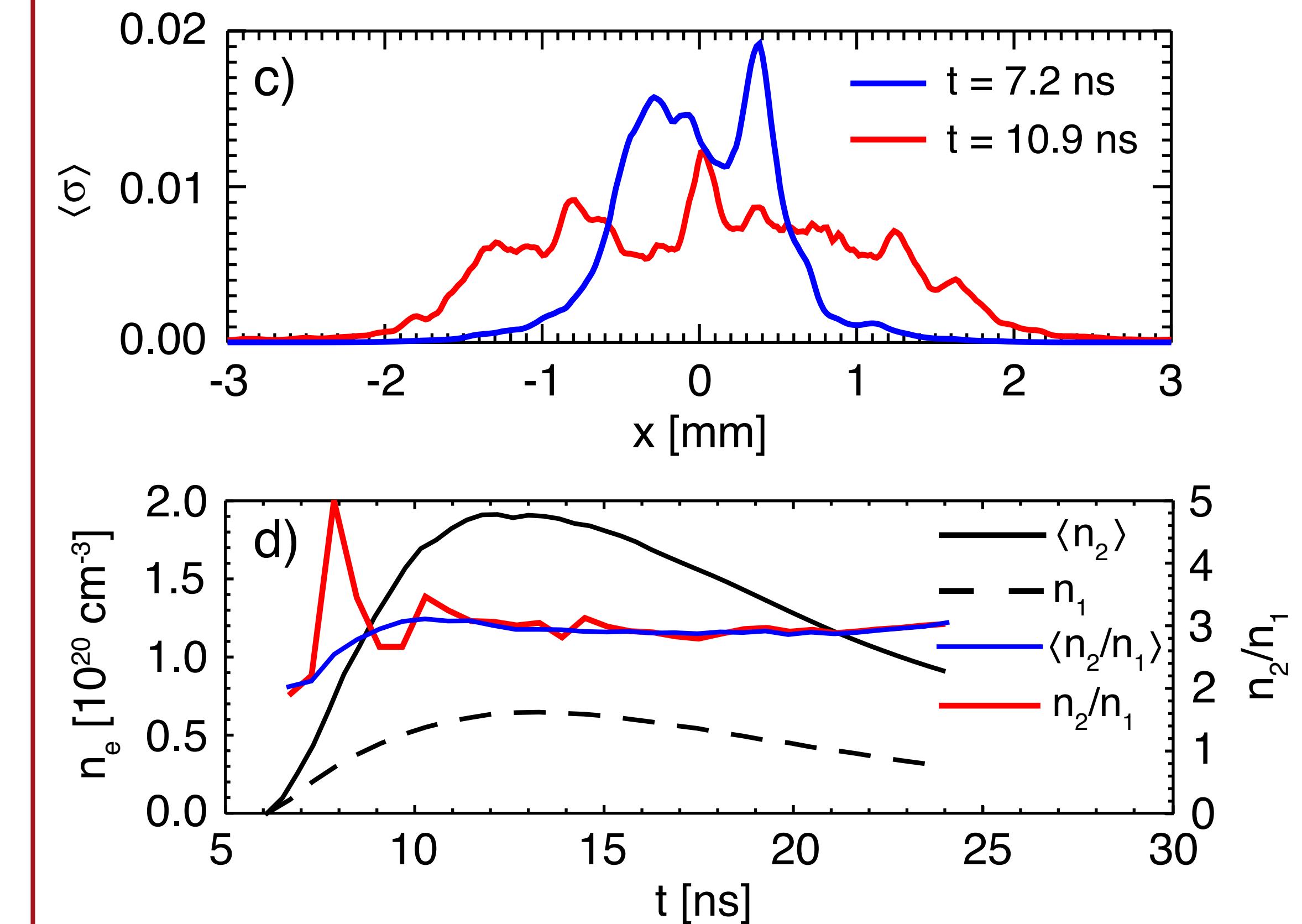
Onset of magnetic turbulence from Weibel instability



Turbulence scale $L_B \sim 200\mu\text{m}$ comparable to ion gyroradius $r_i \sim 300\mu\text{m}^*$

Effective magnetization $\sigma \sim 0.01$

Density evolution consistent with experiments

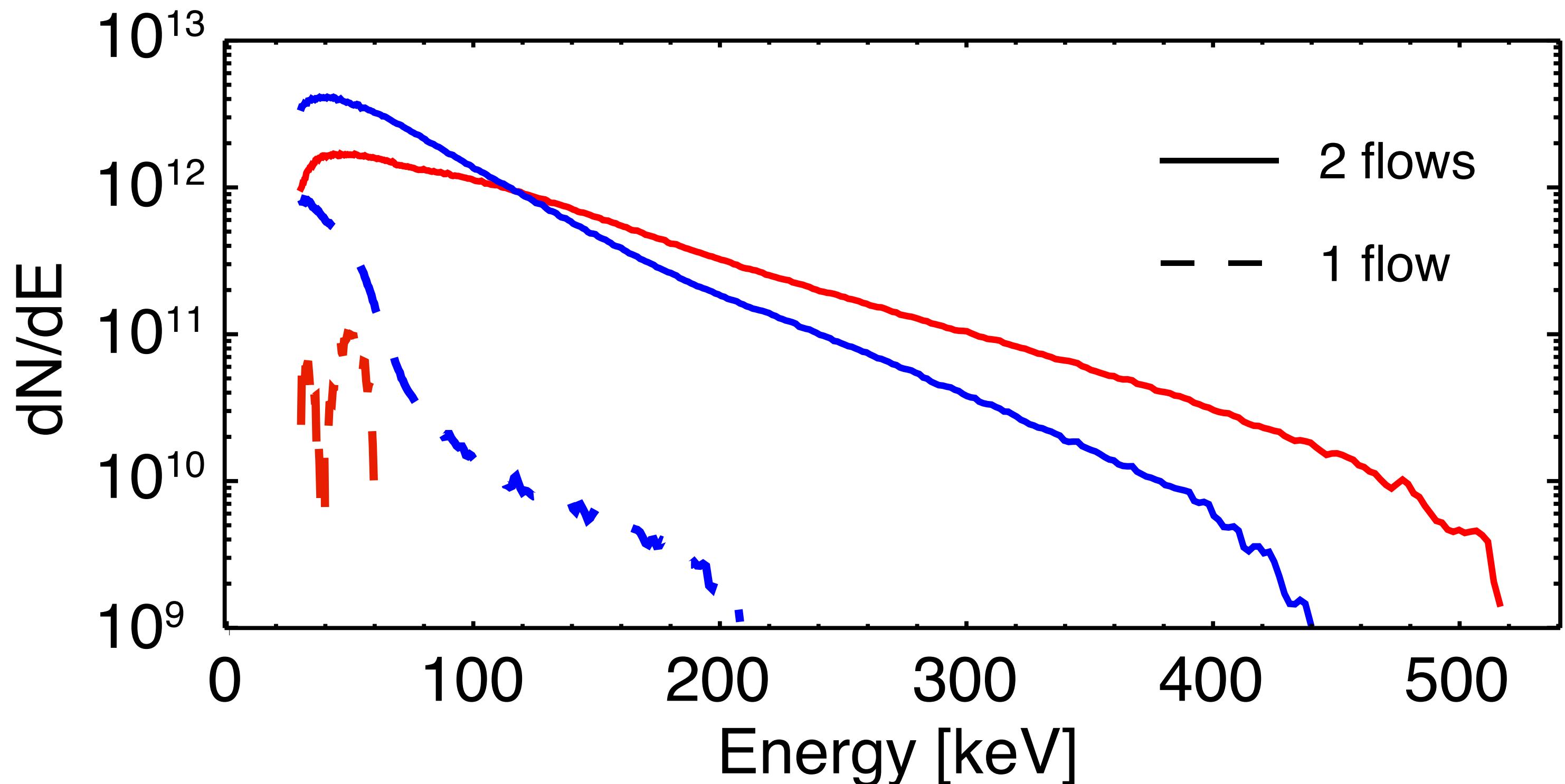


Shock formation at $\sim 9 \text{ ns}$ consistent with experiments

Experiments show clear evidence of nonthermal electron acceleration

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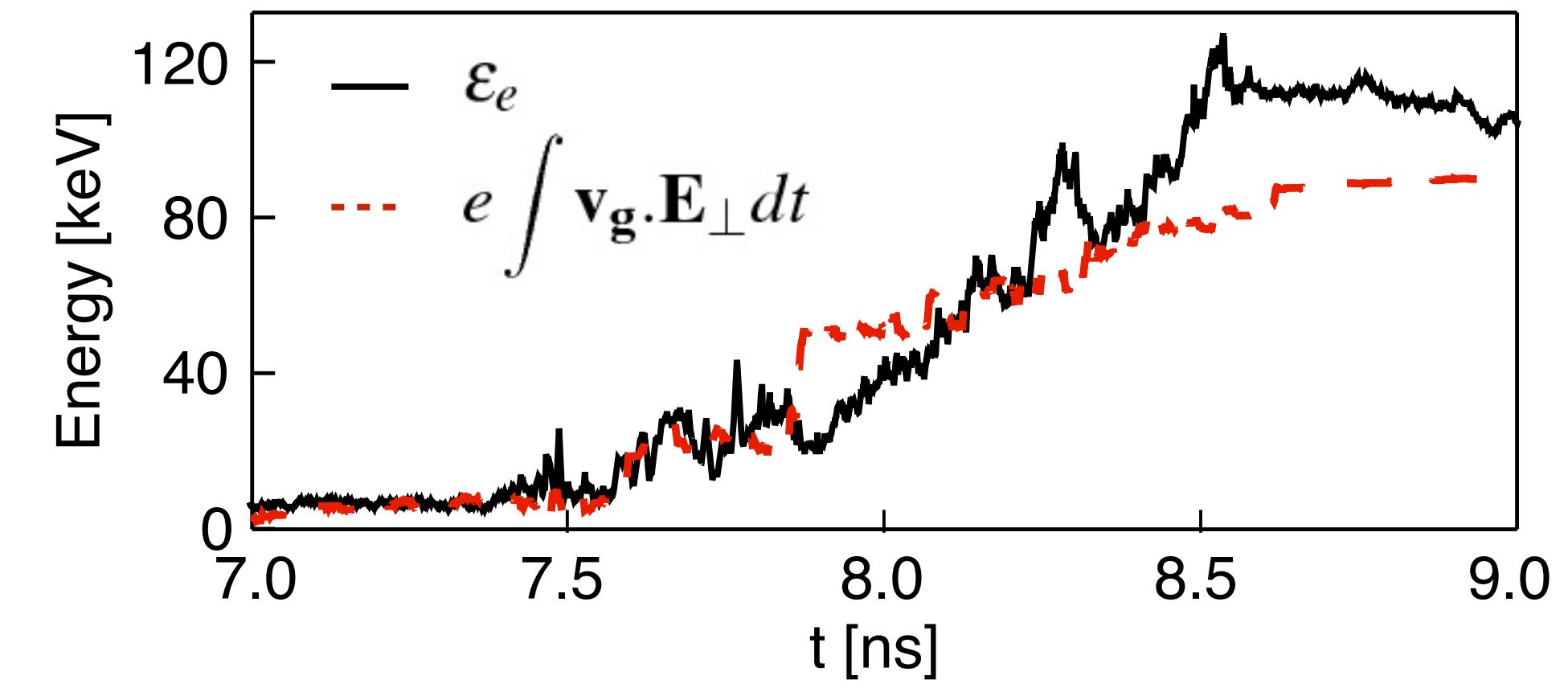
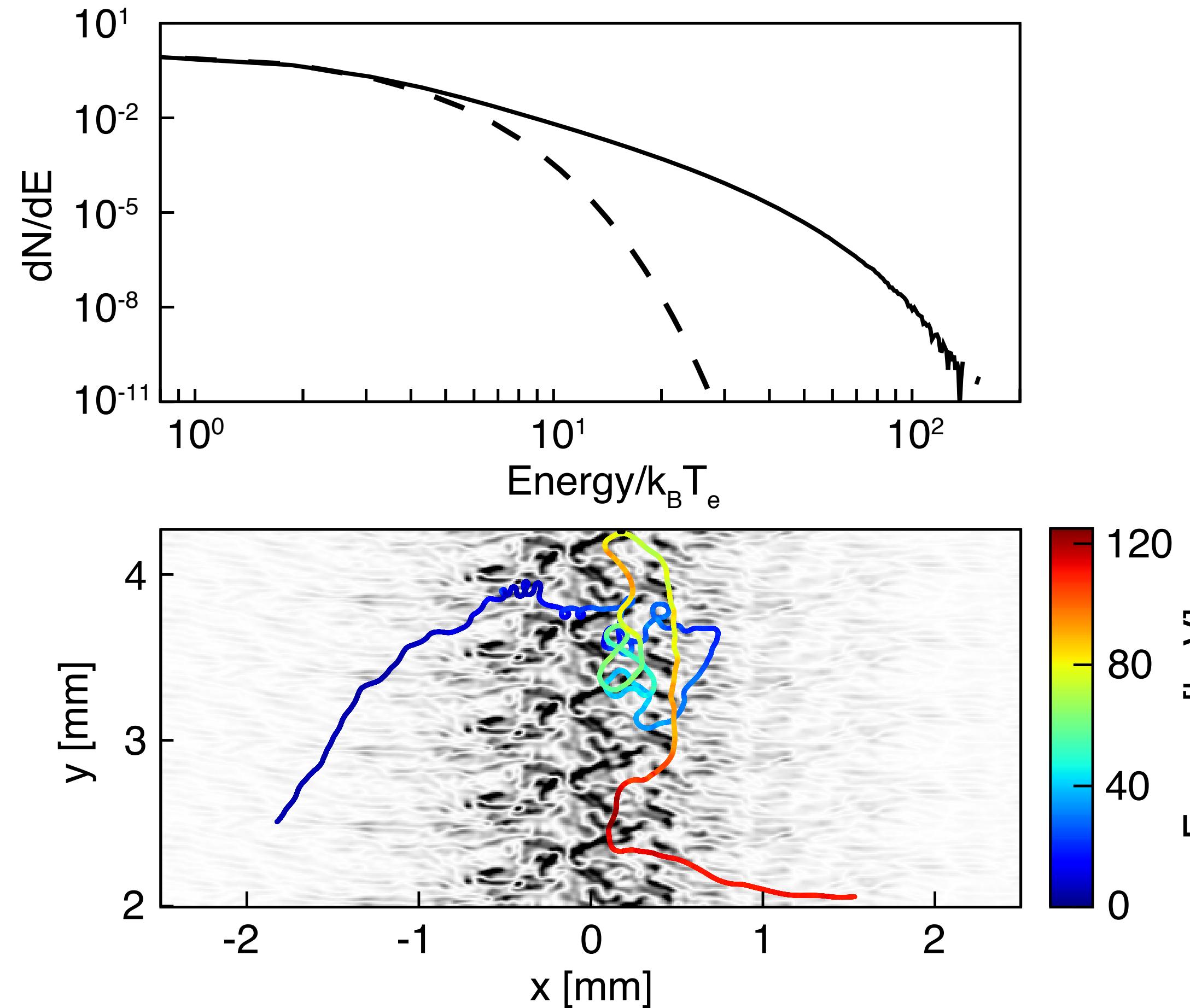
Electrons accelerated to relativistic energies $> 100 T_e$



- Fast electrons from individual plasma flows are produced by the lasers and escape system before flow interaction (< 0.3 ns)
- **Electrons must then be injected from 3 keV shocked plasma!**
- **Nonthermal electrons exceed kinetic energy of the flow ions (~ 250 keV) and can access DSA!**
- $\varepsilon_e / \varepsilon_{\text{flow}} \sim 10^{-4}$ similar to Tycho observations (Morlino & Caprioli 2012)

Simulations reveal that injection is associated with scattering in magnetic turbulence

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Stochastic interaction of electrons with magnetic turbulence allow for significant energization in ns time scale*:

$$t_{\text{acc}} \sim \frac{K(\varepsilon)}{v_{\text{turb}}^2} \sim \text{ns}$$

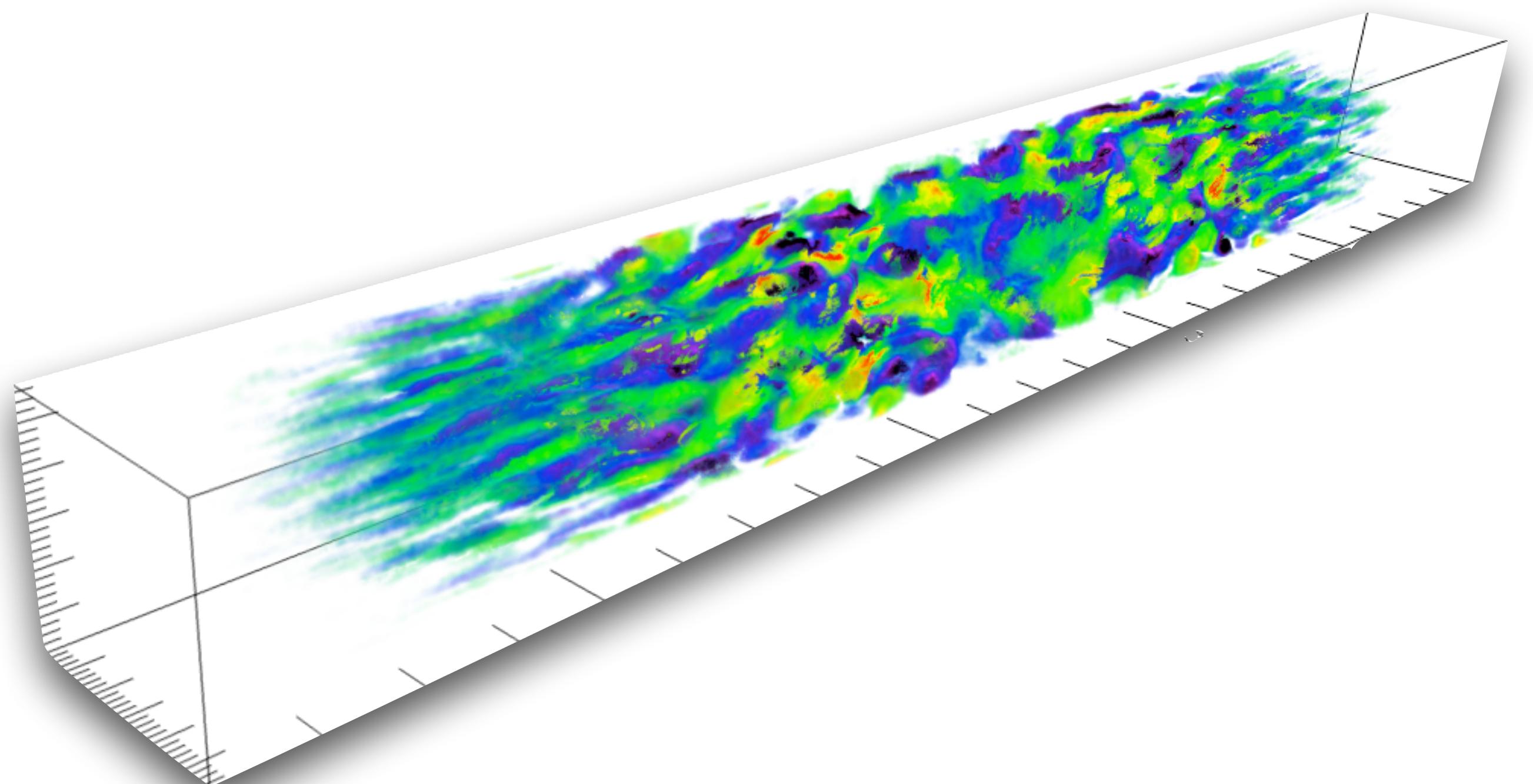
$$\varepsilon_{\text{max}} = |e|(u_{sh}/c)BR_{sh} \sim 500 \text{ keV}$$

Conclusions and future perspectives



- Important progress in experiments of collisionless plasmas led to first laboratory measurements of:
 - **the amplification of magnetic fields by the ion Weibel instability**
 - **the formation of electromagnetic collisionless shocks**
 - **nonthermal electron acceleration in these shocks**
- Experiments provide important **benchmark of numerical codes and injection models** and can **complement spacecraft measurements and astrophysical observations**
- Existing platforms can be extended to study relative acceleration efficiency of protons and electrons, magnetized shocks, different B-field amplification mechanisms (e.g. Bell instability). Stay tuned!

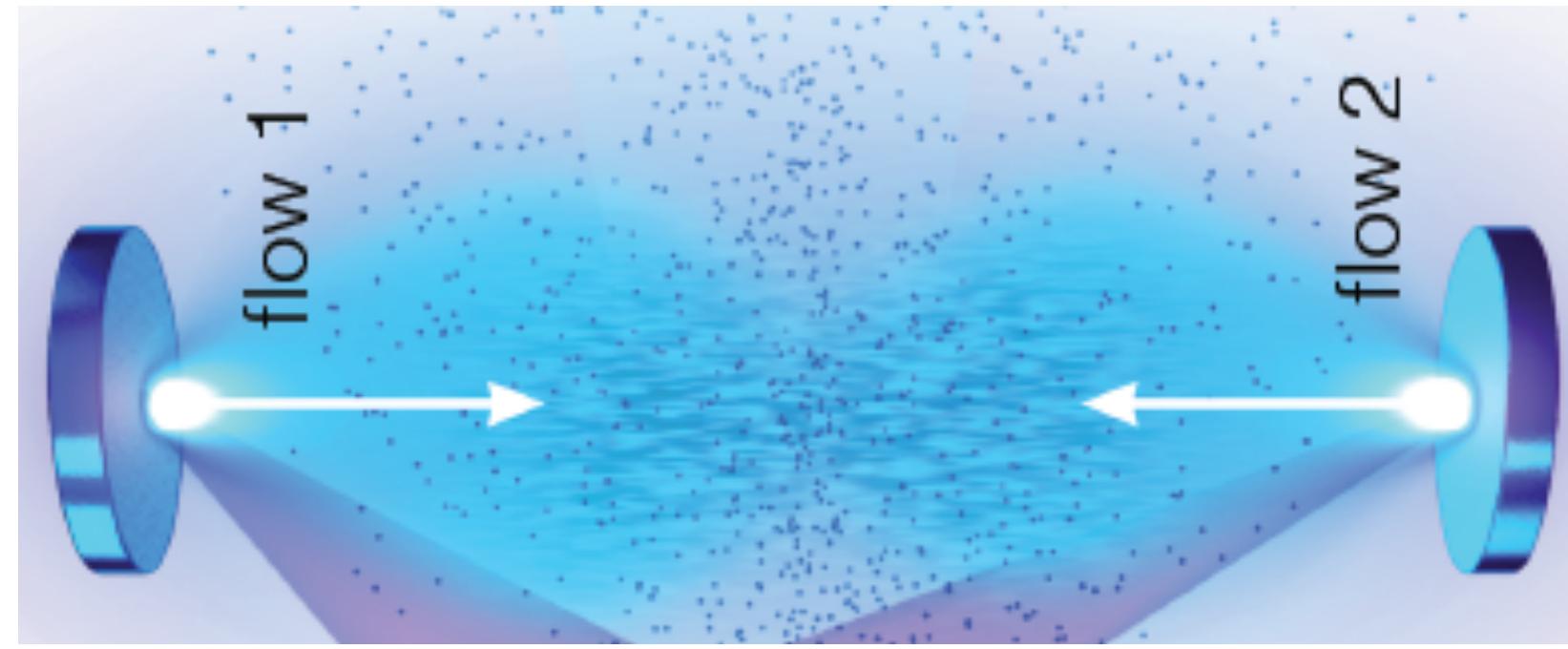
Extra slides



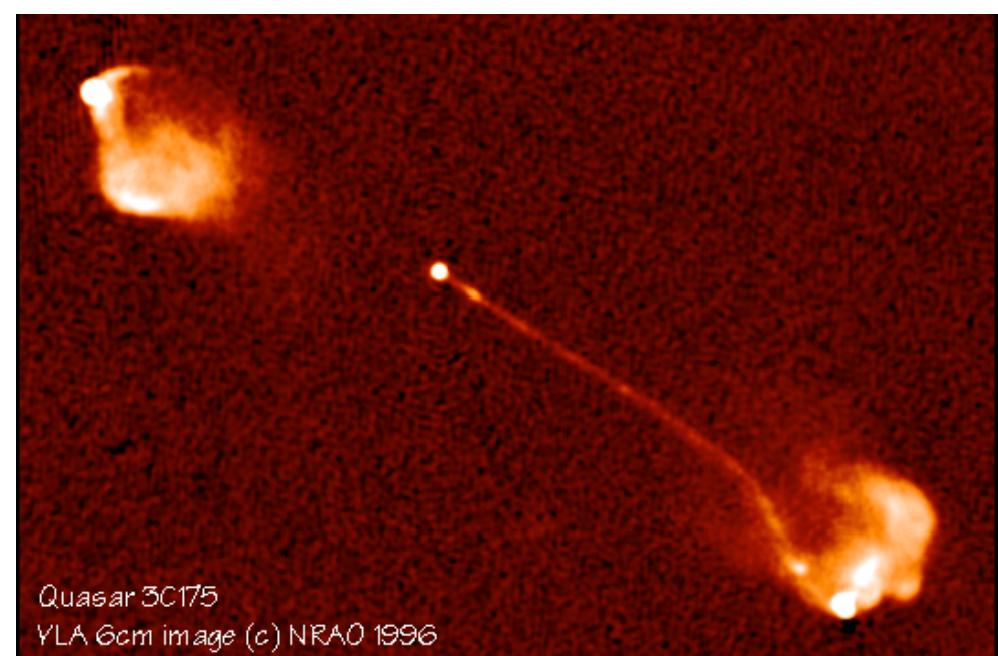
Shock microphysics can be scaled from lab to astrophysical plasmas

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Laboratory system 1



Astrophysical system 2



Main assumptions: collisionless system ($\lambda_{\text{mfp}} \gg L_{\text{system}}$), weakly magnetized ($\sigma \ll 1$), $v_{\text{flow}} \gg v_{\text{th}}$, electromagnetic instabilities are dominant ($\text{Div. } E \sim 0$)

Normalized Vlasov-Maxwell equations:

$$\frac{\partial f'_i}{\partial t'} + \mathbf{v}' \cdot \frac{\partial f'_i}{\partial \mathbf{r}'} + \left(-\frac{\partial \mathbf{A}'}{\partial t'} + \mathbf{v}' \times \nabla' \times \mathbf{A}' \right) \cdot \frac{\partial f'_i}{\partial \mathbf{v}'} = 0,$$

$$\frac{\partial f'_e}{\partial t'} + \mathbf{v}' \cdot \frac{\partial f'_e}{\partial \mathbf{r}'} + \frac{1}{\mu} \left(-\frac{\partial \mathbf{A}'}{\partial t'} + \mathbf{v}' \times \nabla' \times \mathbf{A}' \right) \cdot \frac{\partial f'_e}{\partial \mathbf{v}'} = 0$$

$$\nabla'^2 \mathbf{A}' = \left(\int f'_e \mathbf{v}' d^3 \mathbf{v}' - \int f'_i \mathbf{v}' d\mathbf{v}'^3 \right). \quad \mu \equiv \frac{Z m_e}{A m_p}$$

Scaling relations between both systems:

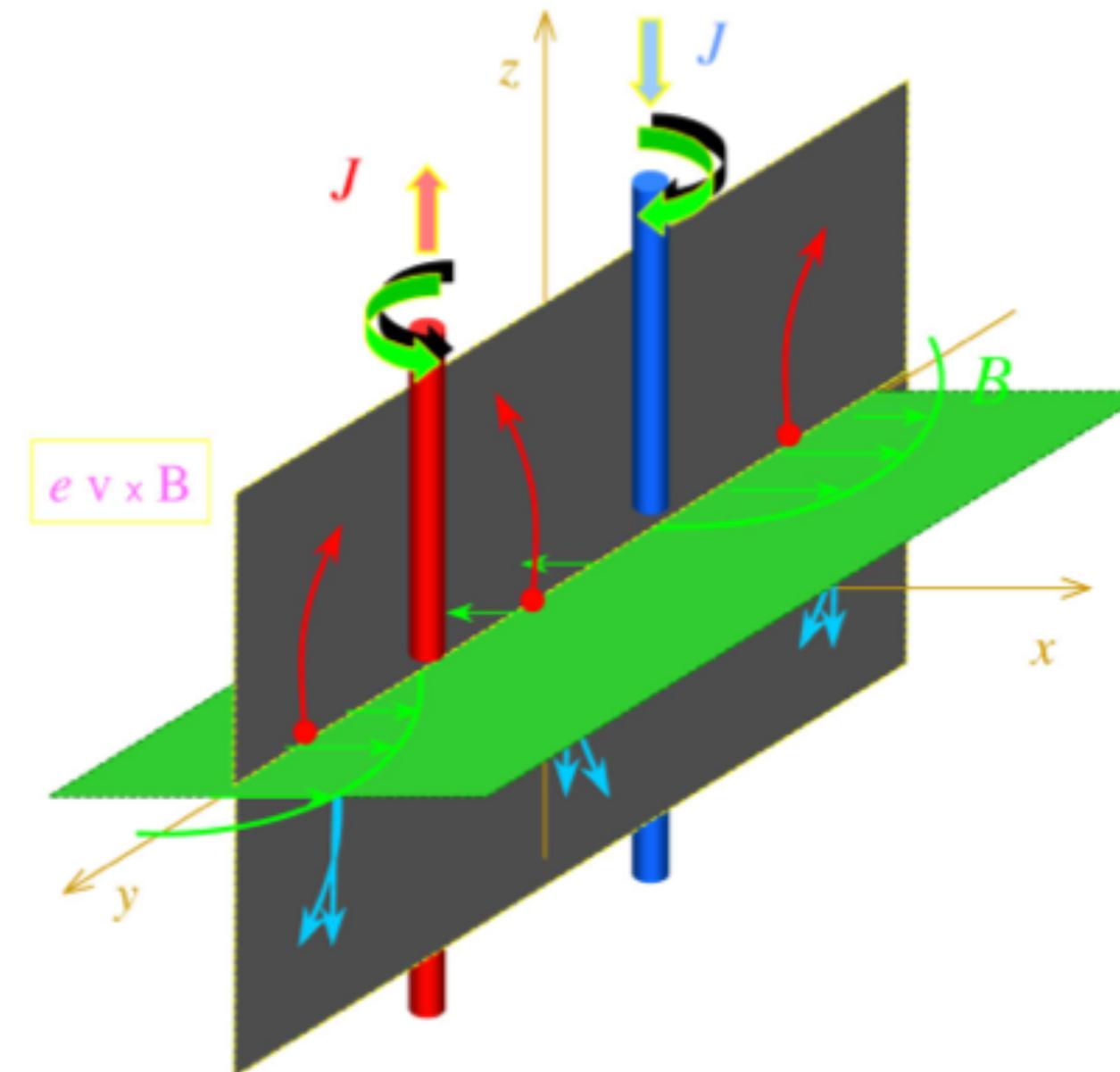
$$L_2 = L_1 \sqrt{\frac{n_1}{n_2}} \quad t_2 = t_1 \frac{u_1}{u_2} \sqrt{\frac{n_1}{n_2}} \quad T_{i2} = \frac{A_2 u_2^2}{A_1 u_1^2} T_{i1}$$

$$\tilde{E}_2 = \tilde{E}_1 \frac{u_2^2}{u_1^2} \sqrt{\frac{n_2}{n_1}} \quad \tilde{B}_2 = \tilde{B}_1 \frac{u_2}{u_1} \sqrt{\frac{n_2}{n_1}}$$

Weibel instability can amplify B-fields in weakly magnetized plasmas

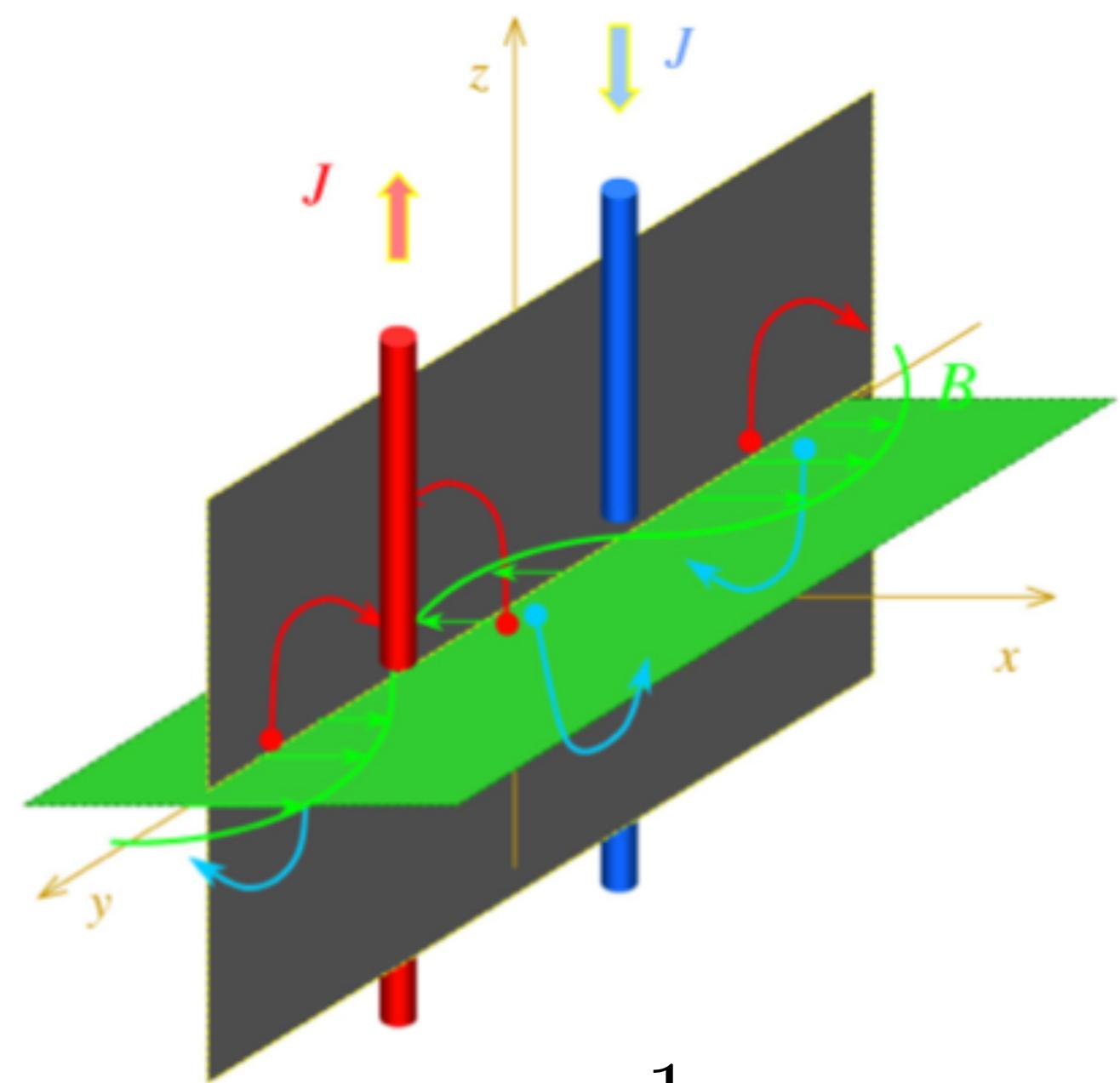
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Linear regime



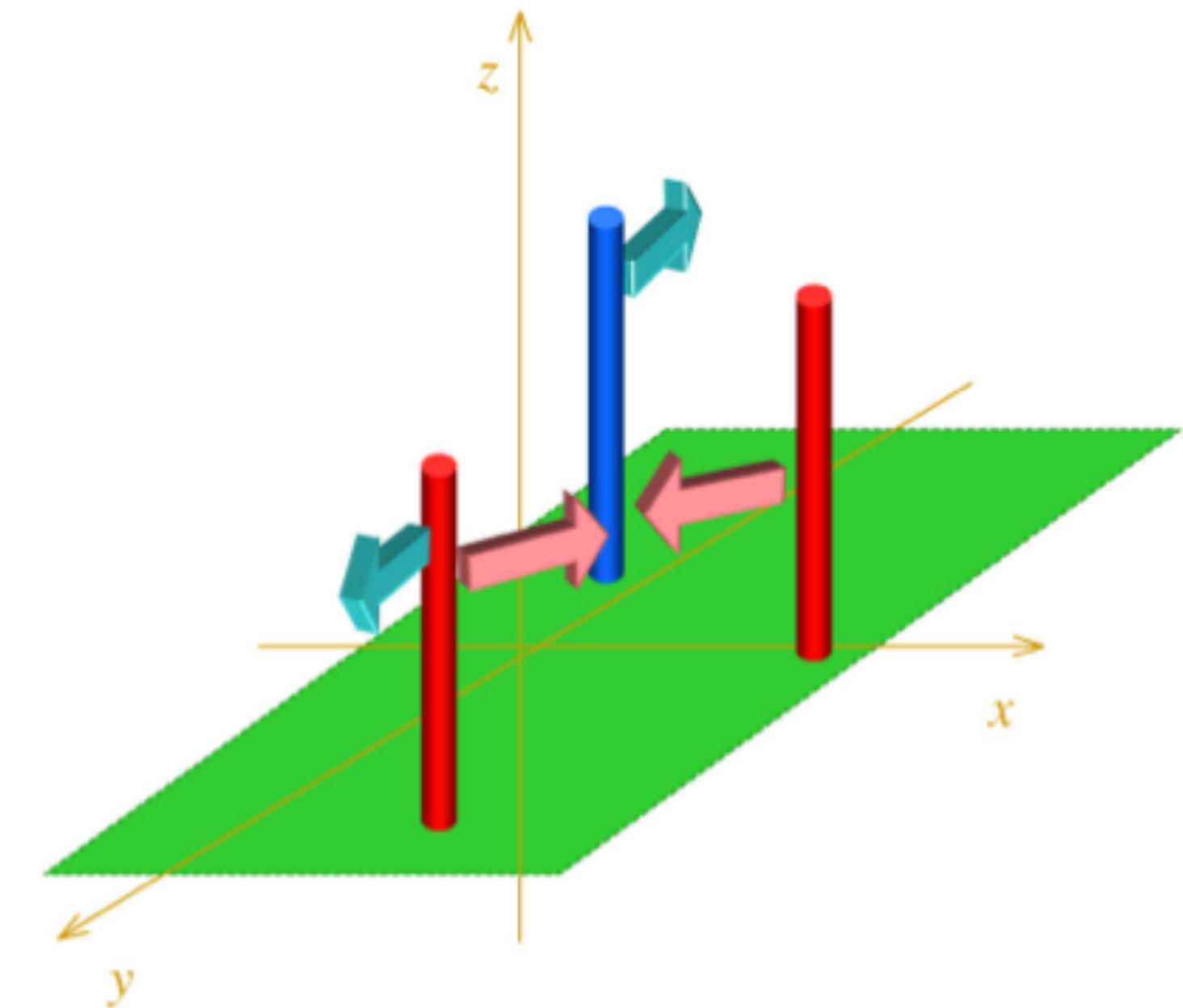
$$\Gamma_W = \frac{v_0}{c} \frac{\omega_{pi}}{\gamma_0^{1/2}}$$

Saturation



$$k_{max} = \frac{\omega_{pi}}{c} \frac{1}{\gamma_0^{1/2}}$$

Non-linear regime



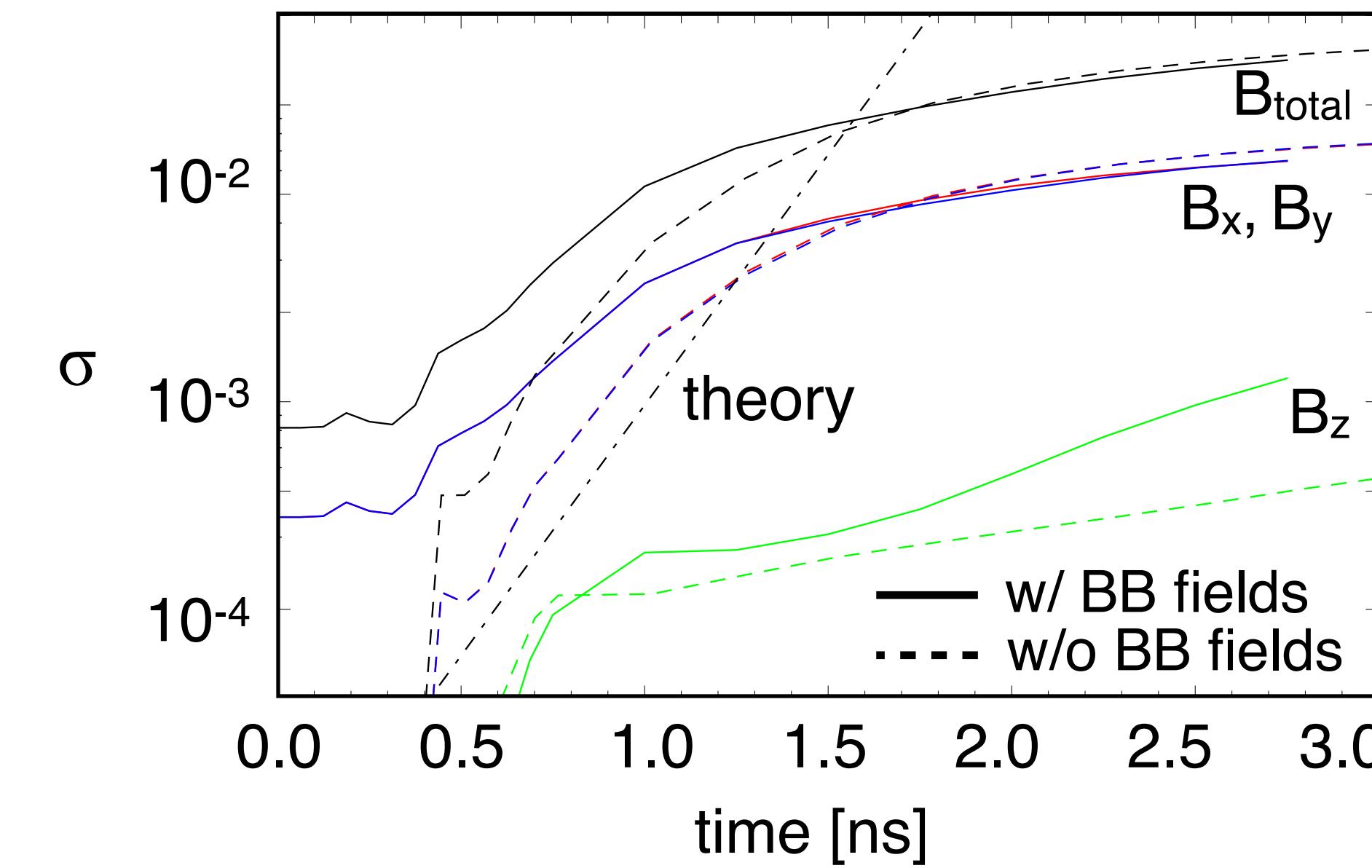
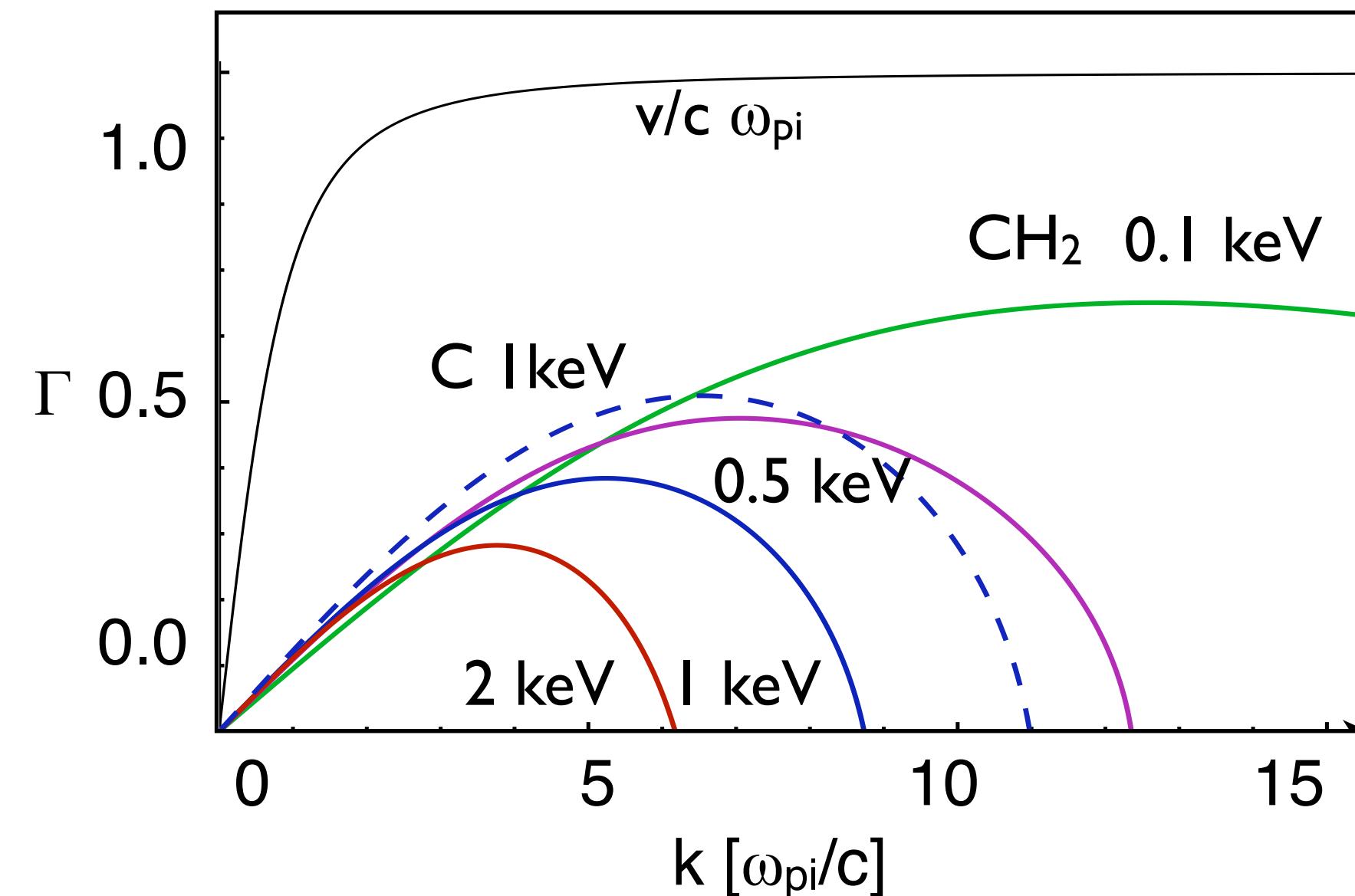
Instability can transfer $\sim 10\%$ of kinetic energy of plasma flows into magnetic energy

Good agreement between linear theory, simulations, and experiments

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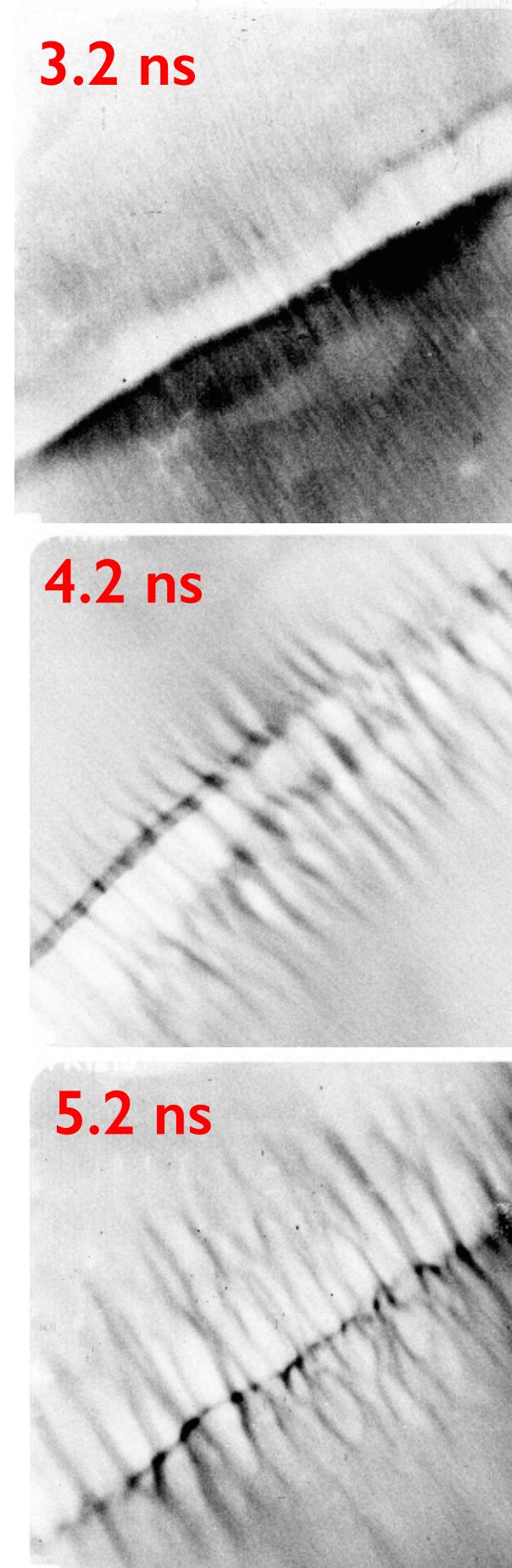
Dispersion relation for plasma with several ion components

$$\tilde{k}^2 + \frac{a_1}{1 + \sqrt{\frac{a_2}{\pi}} \frac{|\tilde{k}|}{\tilde{\Gamma}}} + \sum C_Z \left[G_1 \left(\frac{a_{3\alpha} \tilde{\Gamma}^2}{\tilde{k}^2} \right) - \frac{\tilde{k}^2}{\tilde{\Gamma}^2} G_2 \left(\frac{a_{3\alpha} \tilde{\Gamma}^2}{\tilde{k}^2} \right) \right] = 0.$$
$$a_1 = \frac{\omega_{pe}^2}{\omega_{pi}^2} \quad a_2 = \frac{2T_e}{m_e v^2} \quad a_{3\alpha} = \frac{2T_\alpha}{A_\alpha m_p v^2} \quad G_1(y) = \frac{1}{\sqrt{\pi}} \int_{-\infty}^{+\infty} \frac{ye^{-x^2}}{x^2 + y} dx \quad G_2(y) = \frac{2y}{\sqrt{\pi}} \int_{-\infty}^{+\infty} \frac{x^2 e^{-x^2}}{x^2 + y} dx$$



Our measurements probe early non-linear development of instability

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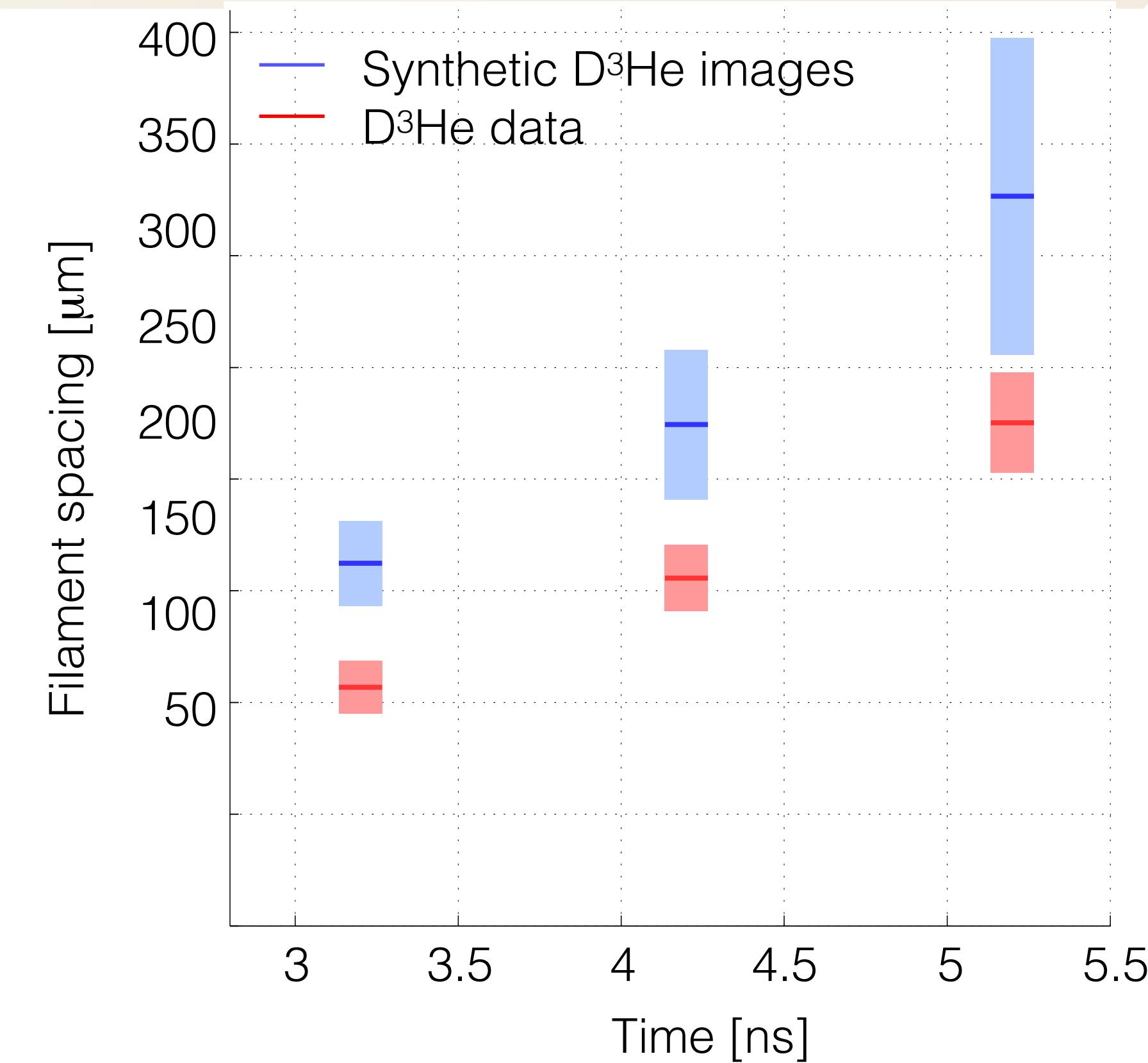


Early time interaction

Bulk flow interpenetration

Development of Weibel instability

Non-linear development of Weibel instability

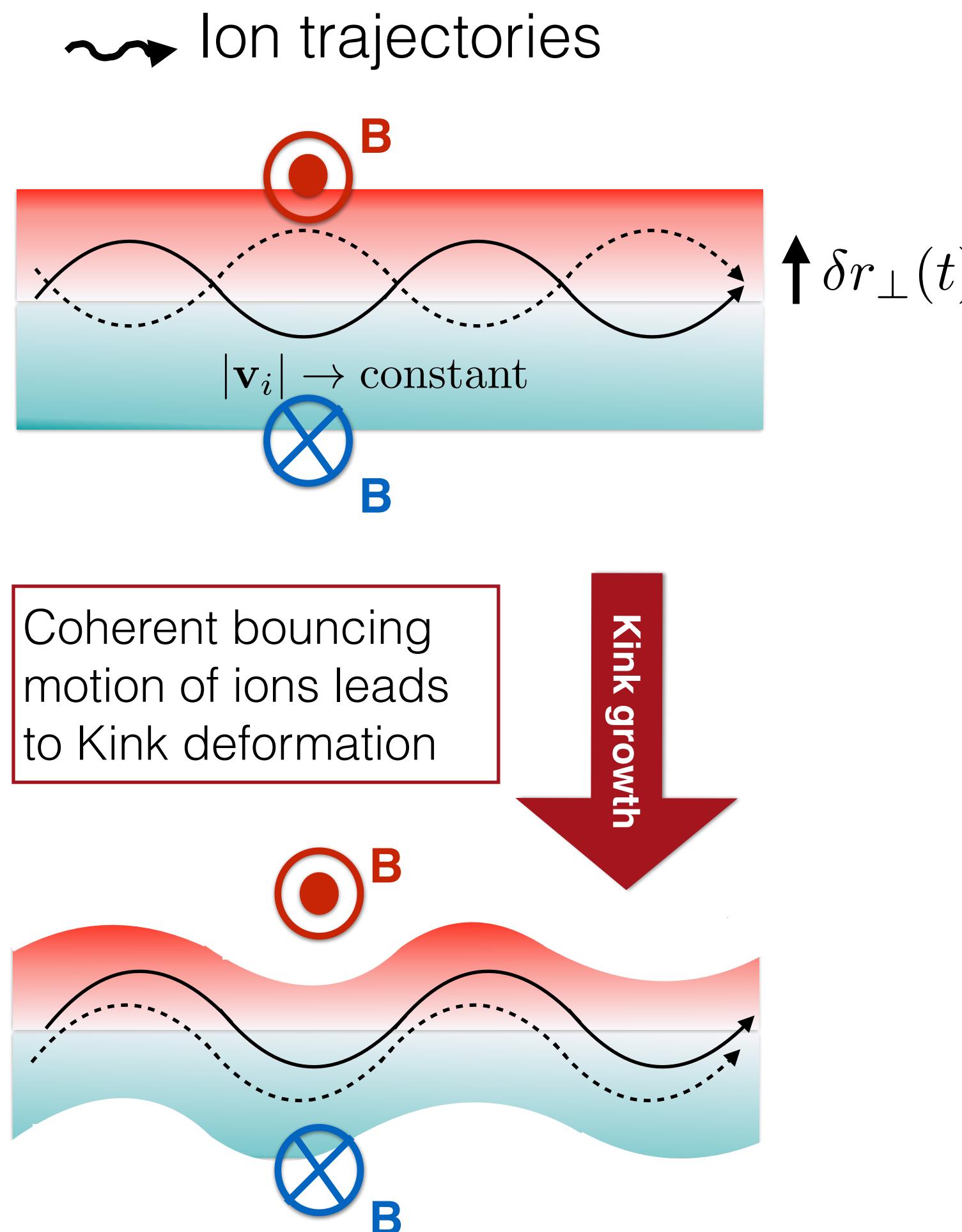


Simulations and experimental measurements indicate magnetization of 1%, consistent with astrophysical shocks

Shock formation requires larger interpenetration regions/higher density flows

Kink deformation of filaments is due to resonant bouncing of ions

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Proton trajectory to leading order in $\delta r_{\perp}/\lambda_B$

$$\frac{d^2 \delta r_{\perp}}{dt^2} + \omega_B^2 \delta r_{\perp} = 0$$

Bouncing frequency: $\omega_{\text{bounce}}^2 \simeq \frac{eBv_i}{\gamma_i m_i (\lambda_{\text{sat}}/2\pi)}$

- Most unstable $\lambda_{\text{kink}}/2\pi \approx v_i/\omega_B$
- Growth rate given by typical attraction-time between bouncing ions

$$\Gamma_{\text{kink}} \simeq \frac{\omega_{pi}\lambda_B}{4c} \frac{v_i}{\lambda_{\text{kink}}} \simeq \frac{\omega_{pi}\lambda_B}{4c} \omega_{\text{bounce}}$$

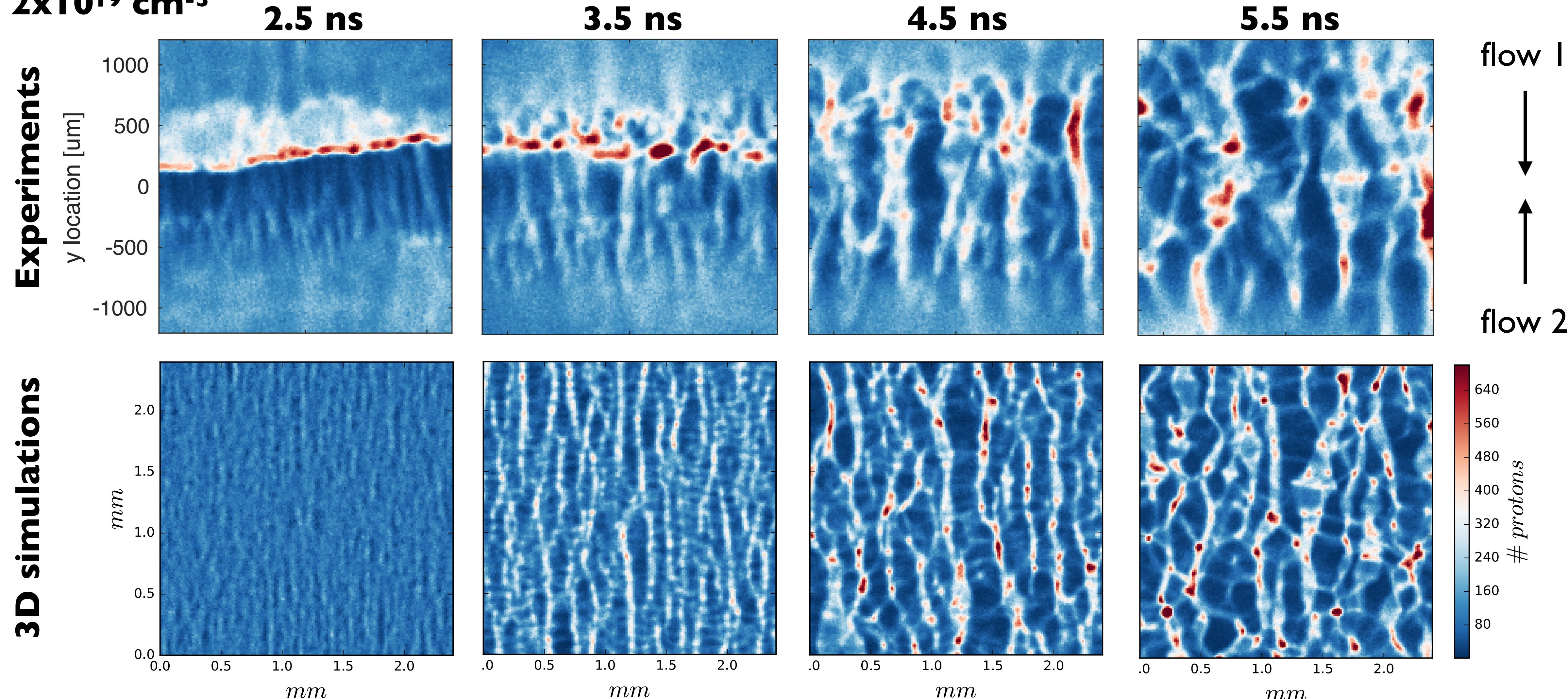
- Saturation when transverse kinetic ion pressure exceed magnetic pressure

$$n_i m_i (\delta r_{\perp}^{\text{sat}} \omega_{\text{bounce}} / \pi)^2 \sim B^2 / 2\mu_0 \Rightarrow \delta r_{\perp}^{\text{sat}} \simeq \pi \lambda_B / 4$$

Proton radiography data is consistent with 3D PIC simulations

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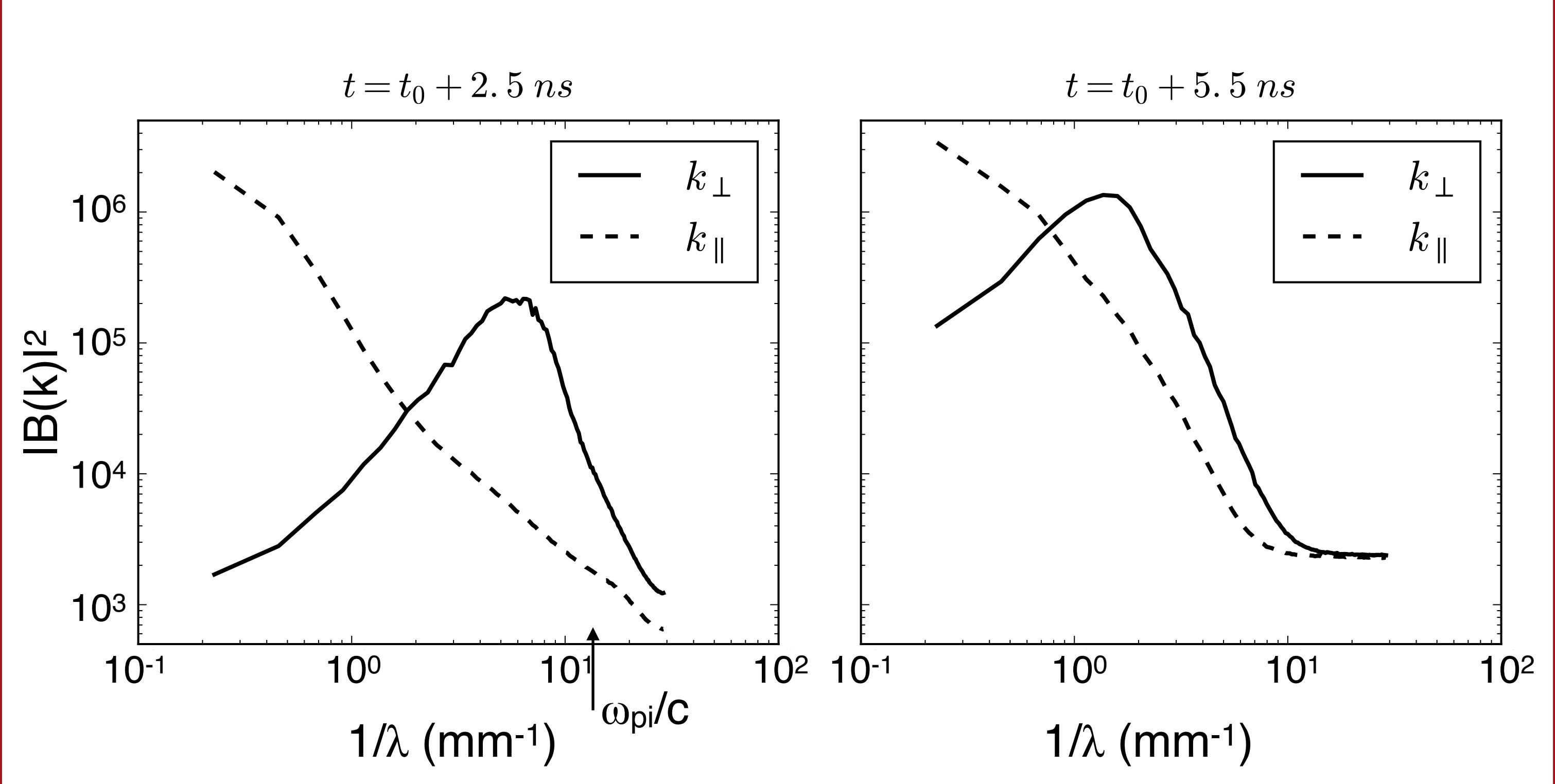
$$n = 2 \times 10^{19} \text{ cm}^{-3}$$



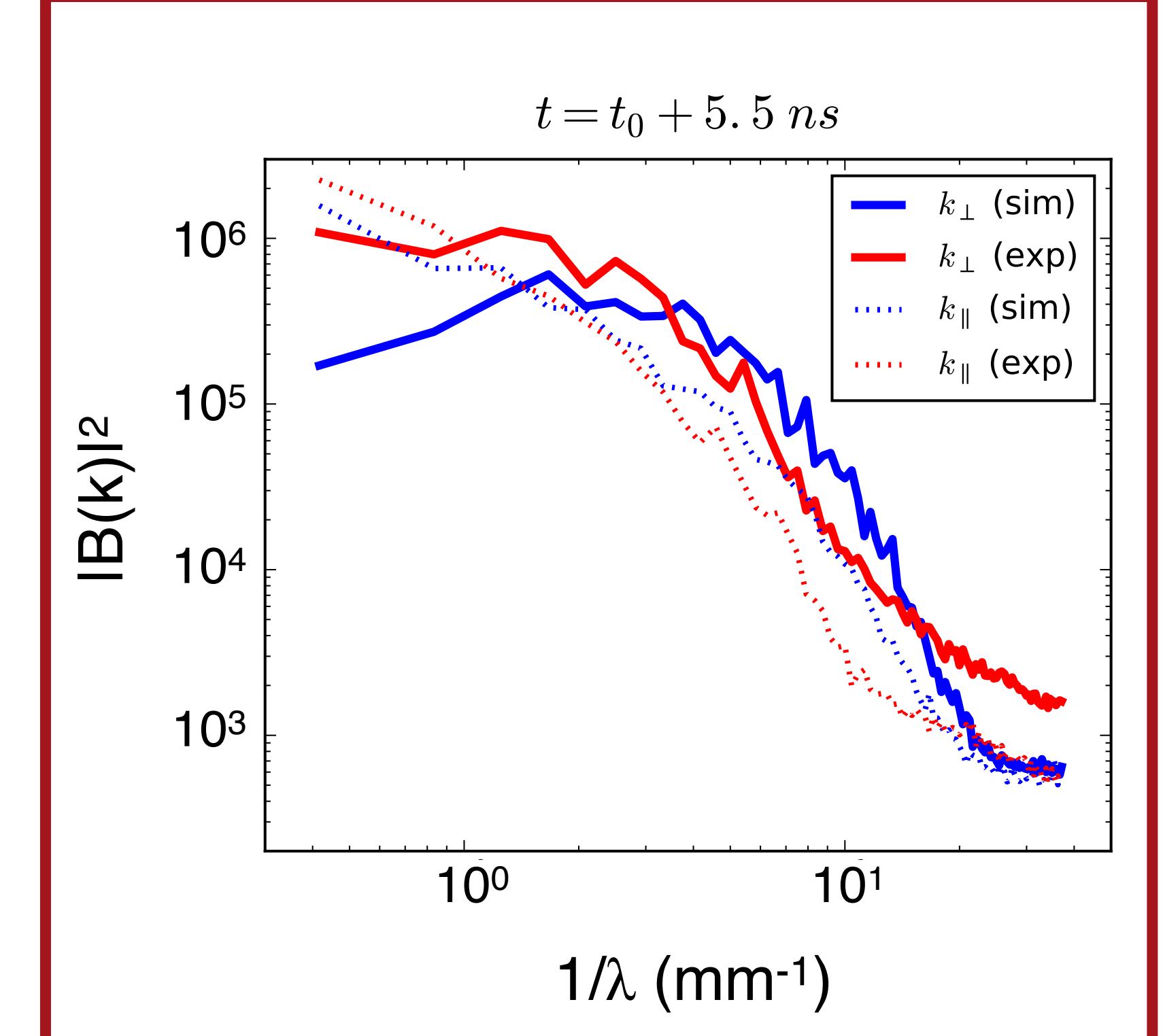
Initial analysis indicates isotropization of B-field energy at late times

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3D PIC simulation shows isotropization of B-field energy



Experiment vs 3D simulation



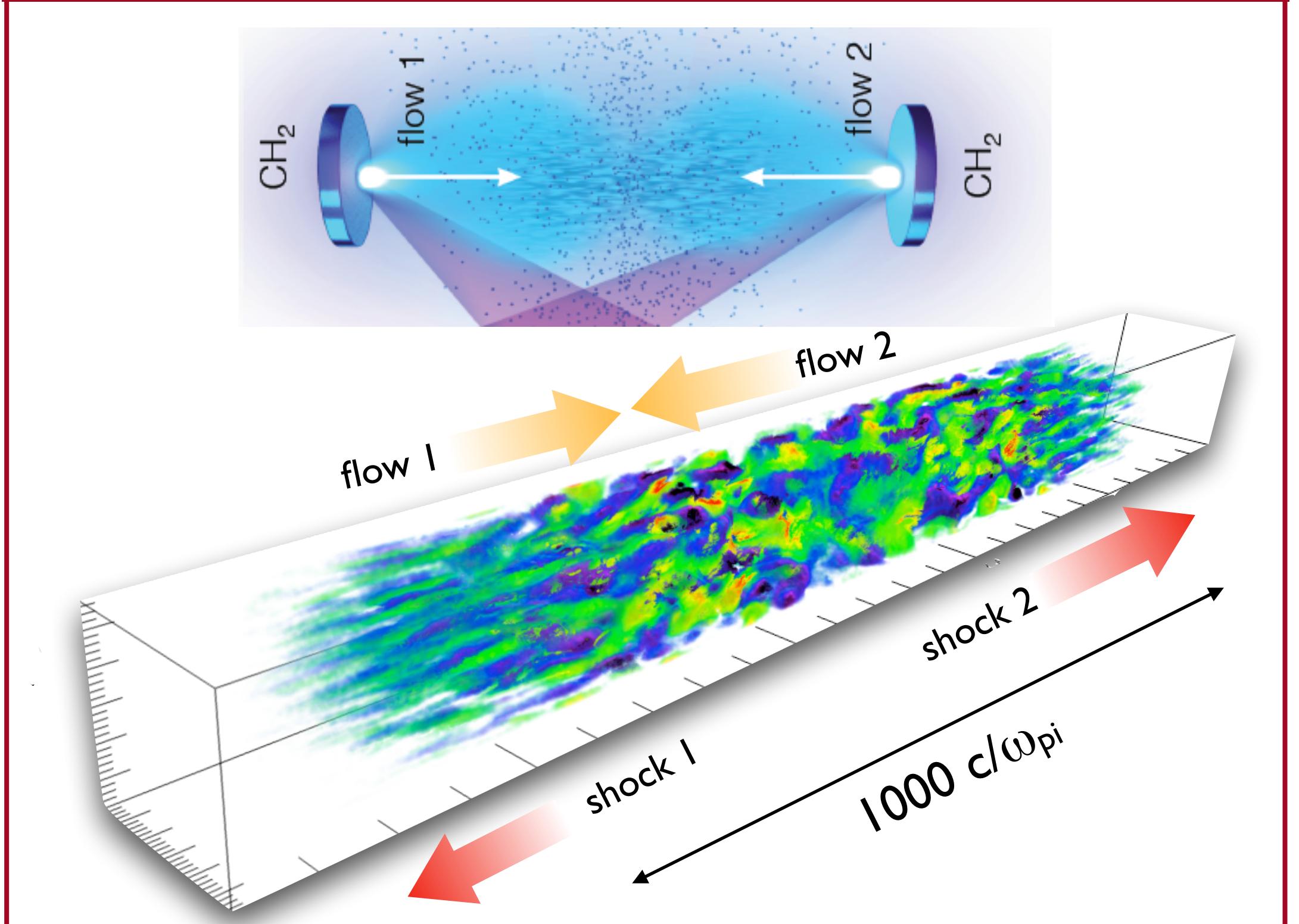
More detailed analysis is needed to benchmark ion resonance model with experiments

NIF experiments will study shock formation and particle acceleration

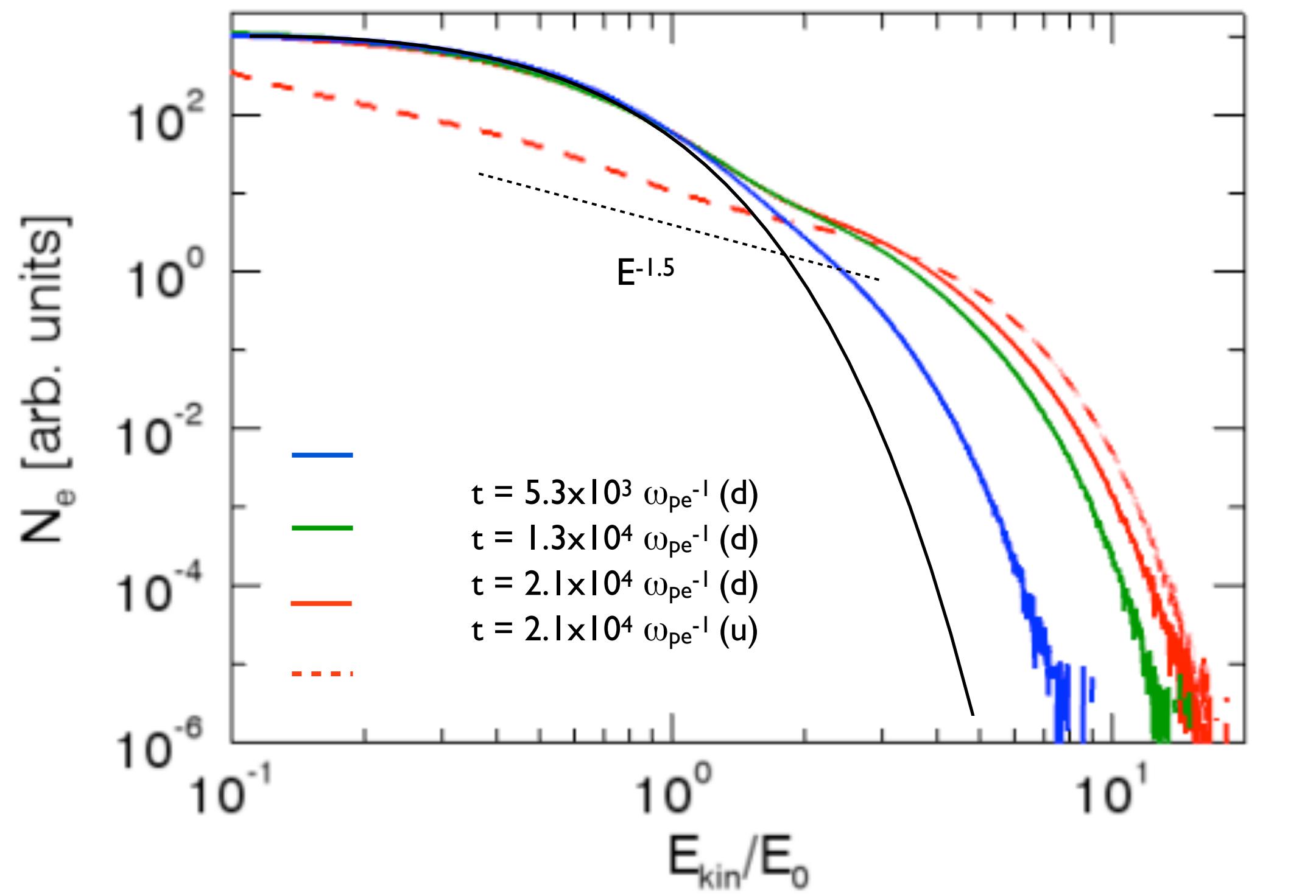
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PI: F. Fiuzza

500 kJ/target at NIF can generate large system size



Evidence of Fermi acceleration (cosmic rays)



These experiments can validate current models for shocks formation and particle injection