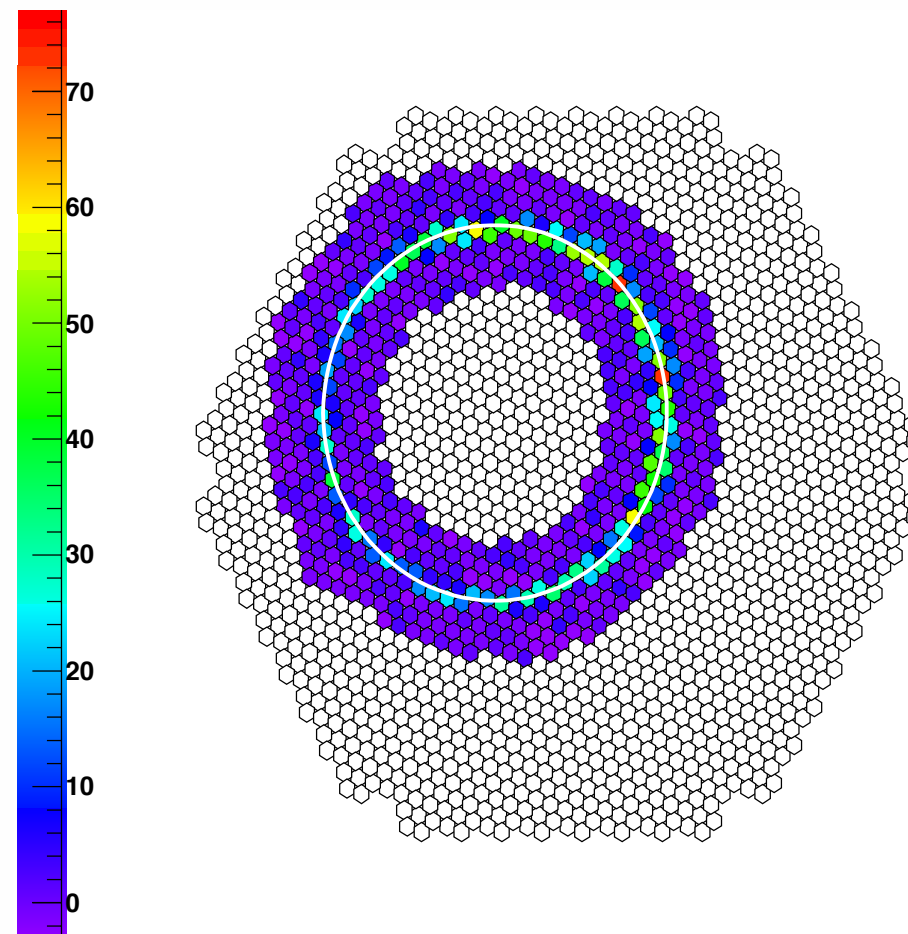


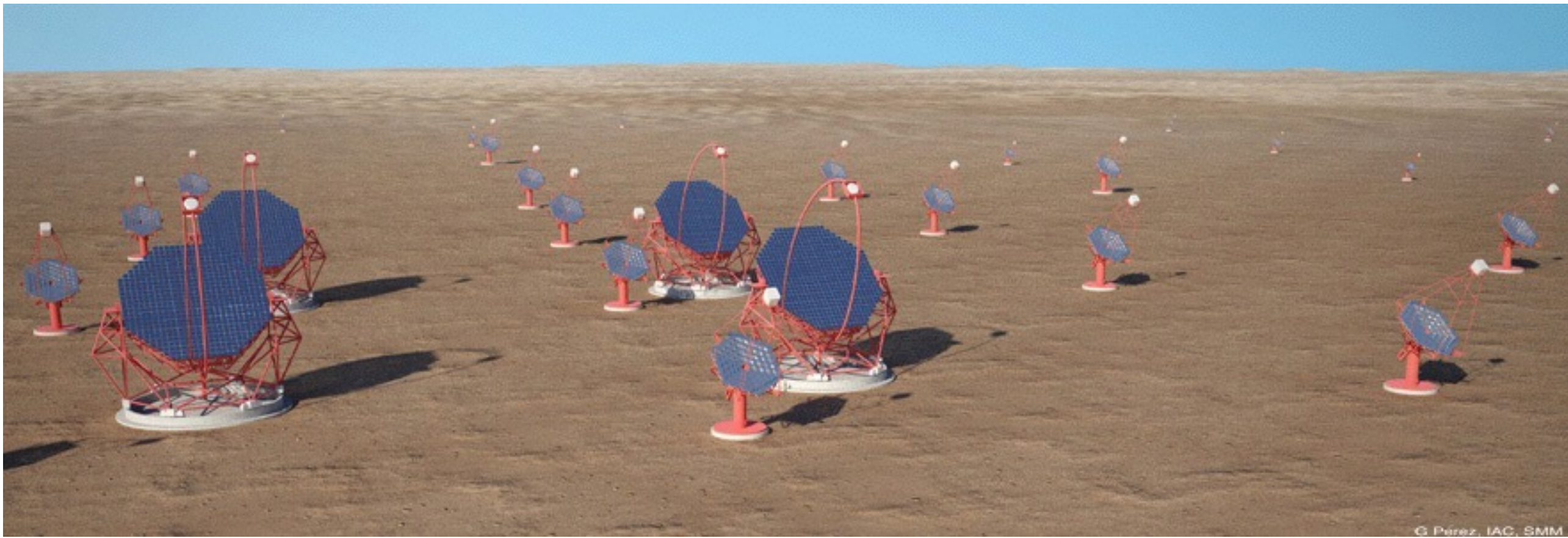
# Reconstructing Muons in CTA



CCF Meeting, 23/06/16  
A. Mitchell

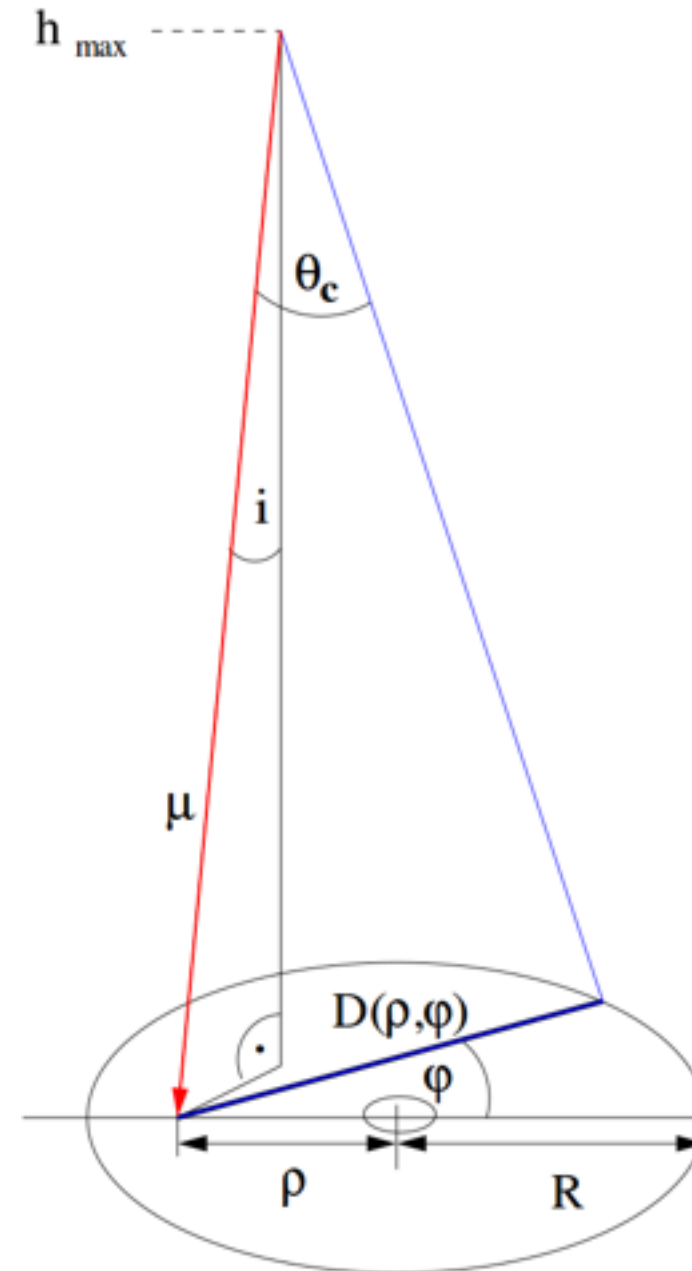
# Need for Generic Algorithms

- CTA will comprise a variety of telescopes and cameras
- Don't want every camera/telescope team to have a separate reconstruction algorithm
- Ideally a single, generic algorithm in the pipeline, which can be applied to all
- —> Need flexible/generalised approach



# H.E.S.S. II Approach

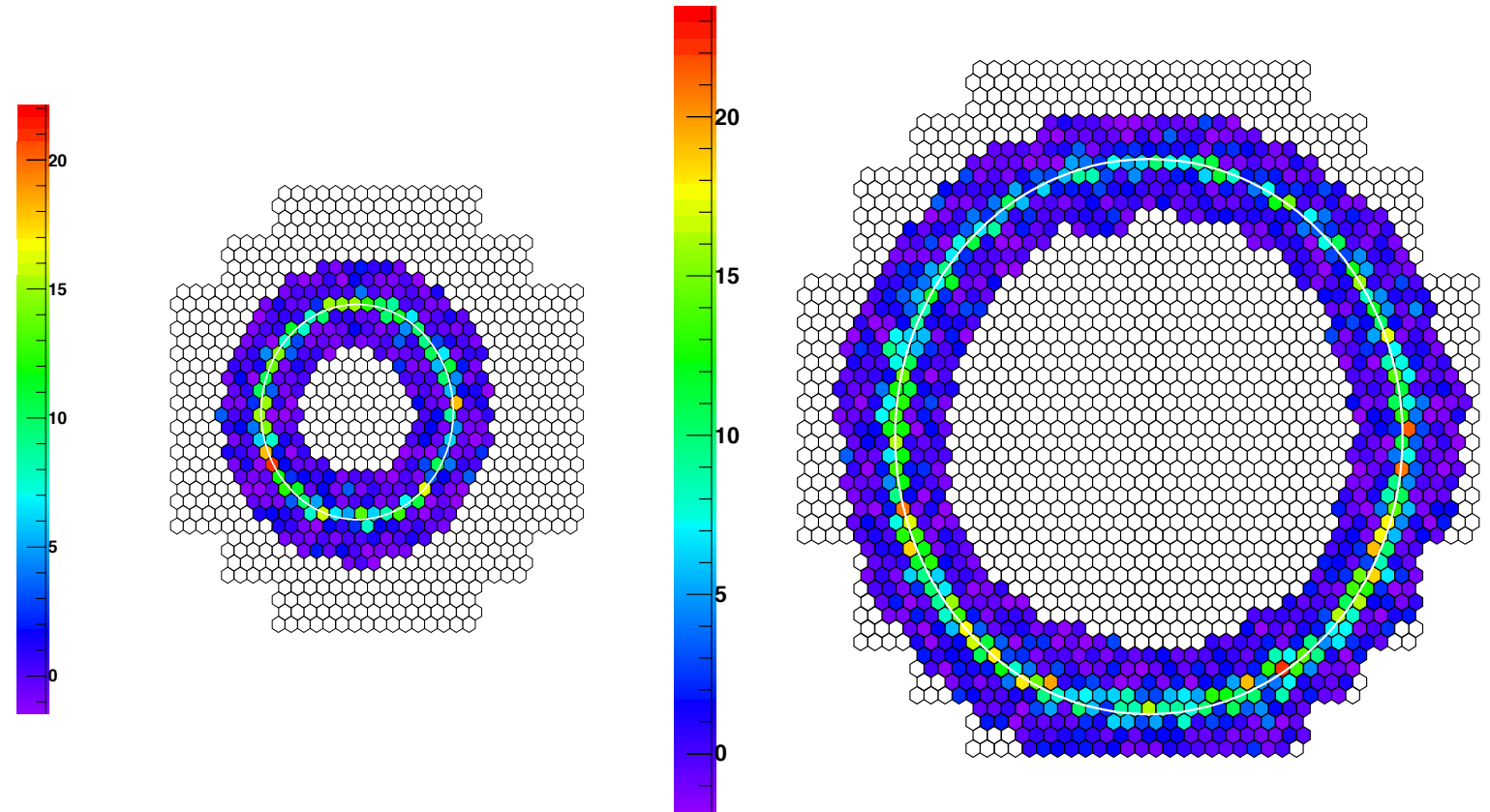
- H.E.S.S. II is the only currently operational multi-sized IACT array
- Needed to rework the muon calibration code for use on both telescope types
- Amount of light from muon in one pixel depends on telescope geometry



$$I_{pe} = \varepsilon_{\mu} I(\theta_c, \rho, \phi, \omega) = \varepsilon_{\mu} \frac{\alpha}{2} \frac{\omega}{\theta_c} I \sin(2\theta_c) D(\rho, \phi)$$

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- Change from chi-squared fit to 2D pixel-wise log likelihood

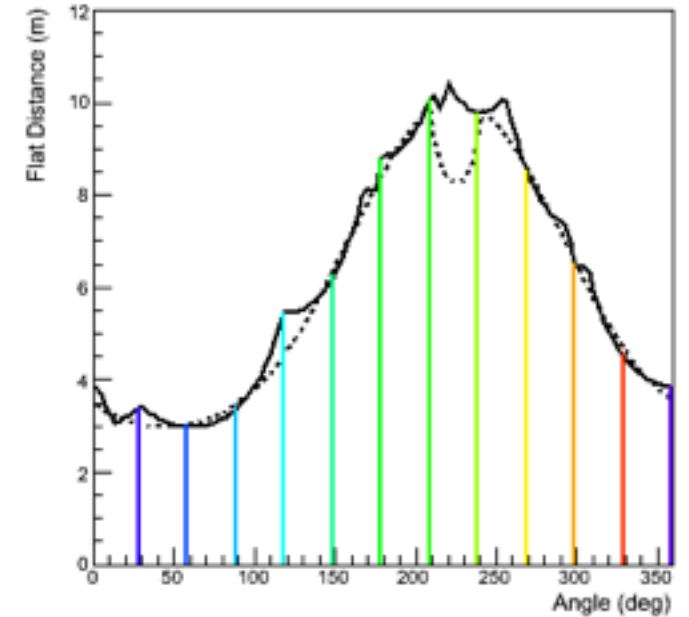
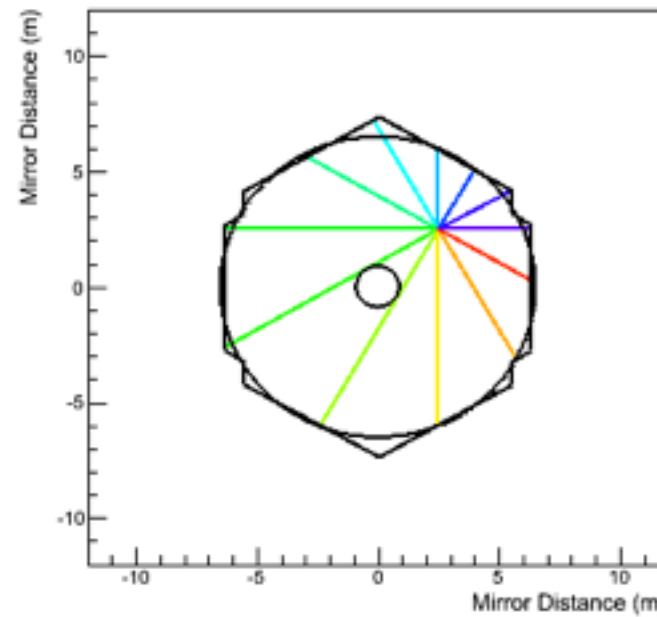


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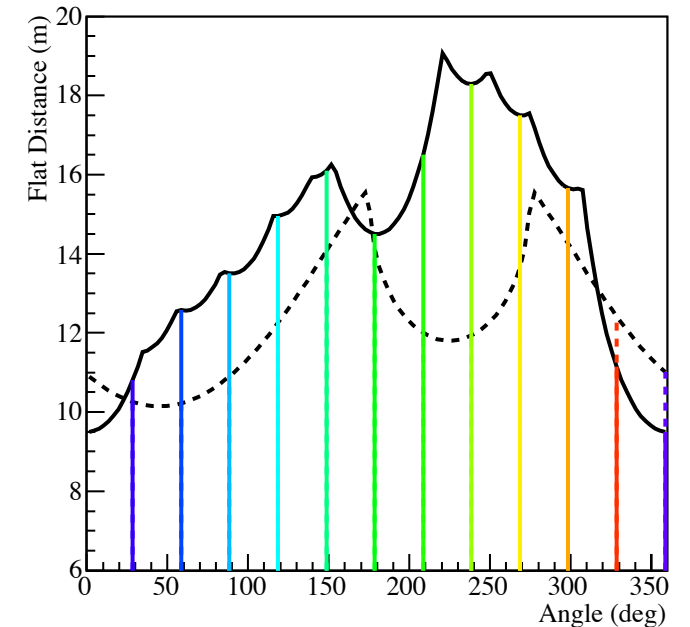
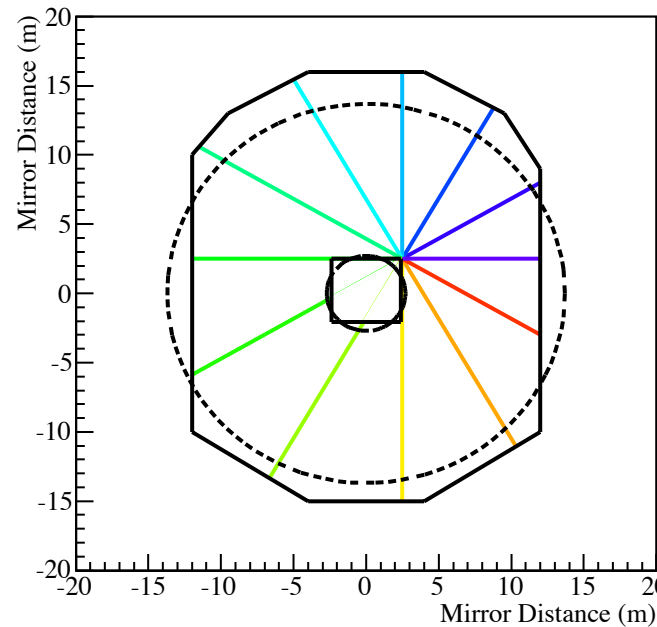
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- Mirror interpolation vs circle approximation



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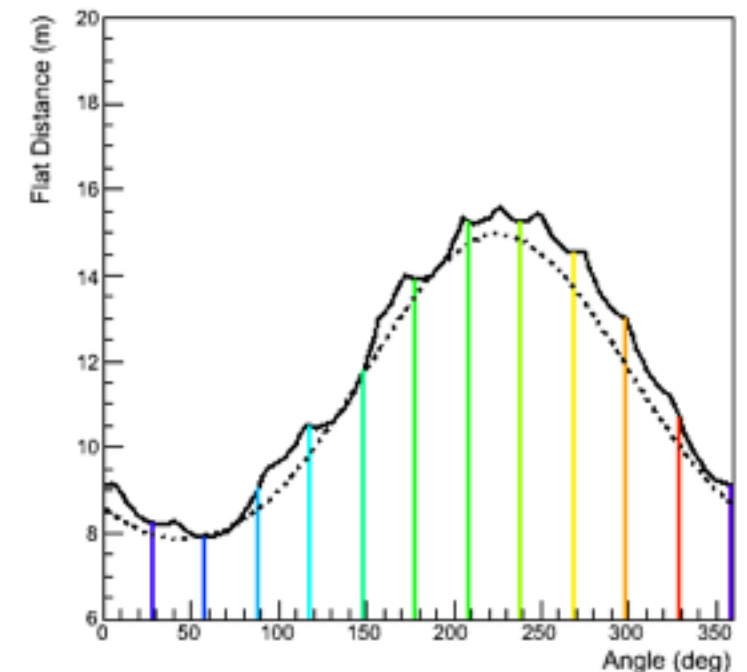
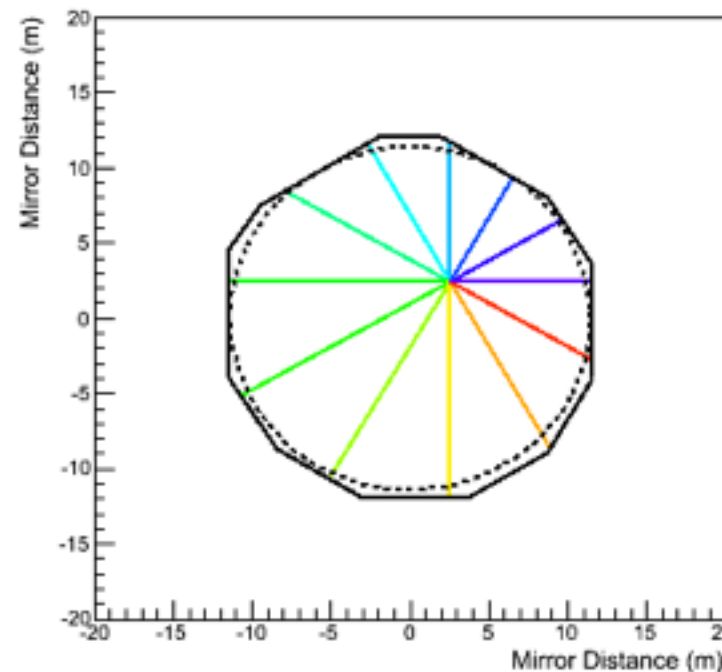
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- Mirror interpolation vs circle approximation
- Same code now used for all HESS telescopes; telescope configuration passed as input



# CTA simulations

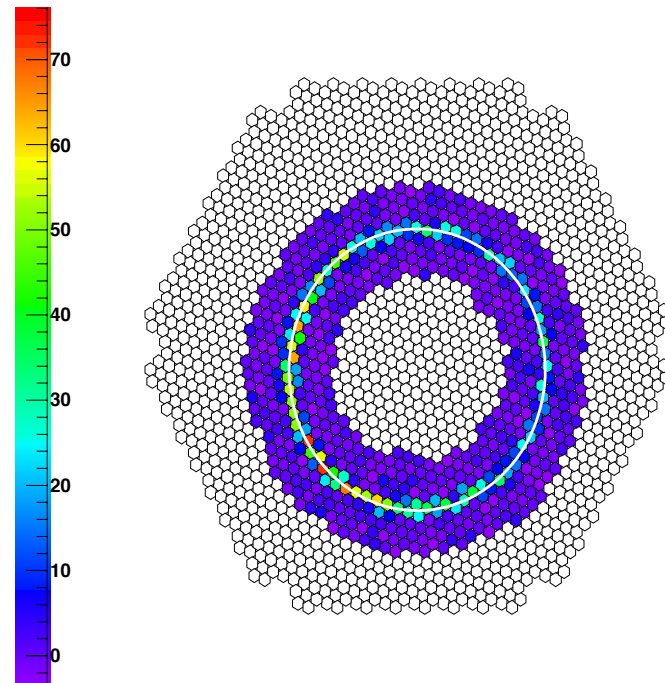
- Simulated muons for all telescopes with prod-3
- Converted output into HESS readable format
- New mirror descriptions (within the muon code) required for CTA telescopes
- Cuts required optimising
- Same code now used for all HESS **and CTA** telescopes; telescope configuration passed as input

LST

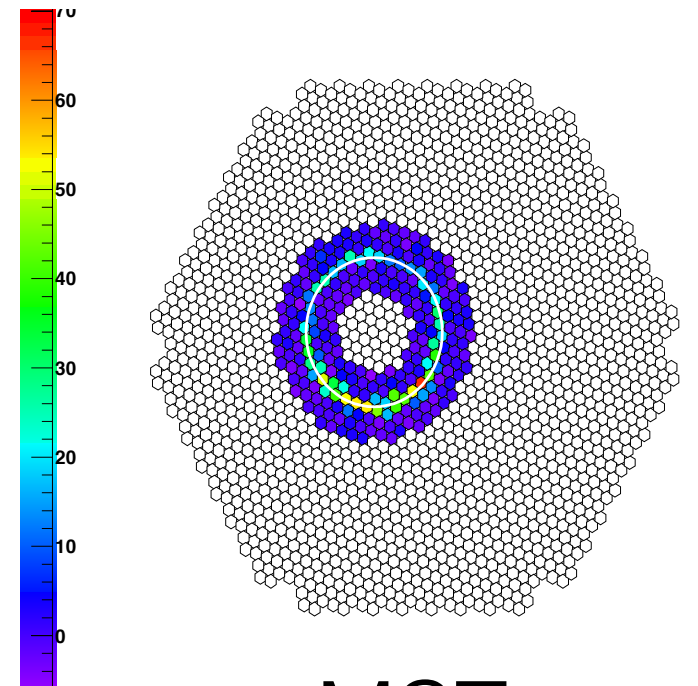


# CTA Muon Events

- Muon events are fitted with a circle
- A 2D analytical expectation is calculated
- A 2D pixel log-likelihood fit of the event to the expectation is performed
- Muon Efficiency is a free parameter of the fit
- $\omega$  - angular pixel size



LST

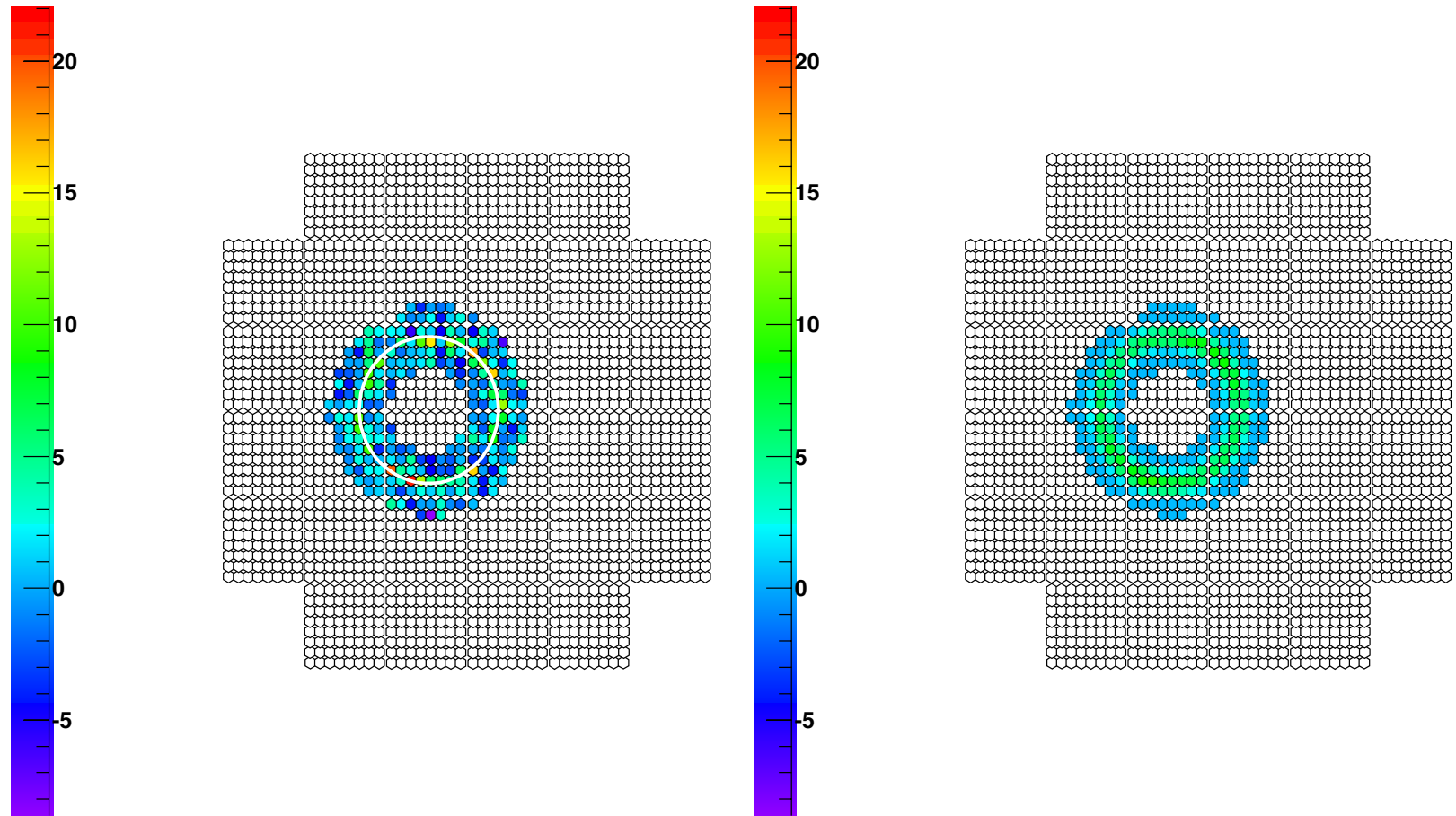


MST

$$I_{pe} = \varepsilon_{\mu} I(\theta_c, \rho, \phi, \omega) = \varepsilon_{\mu} \frac{\alpha}{2} \frac{\omega}{\theta_c} I \sin(2\theta_c) D(\rho, \phi)$$

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SST-GCT

$$I_{pe} = \varepsilon_{\mu} I(\theta_c, \rho, \phi, \omega) = \varepsilon_{\mu} \frac{\alpha}{2} \frac{\omega}{\theta_c} I \sin(2\theta_c) D(\rho, \phi)$$

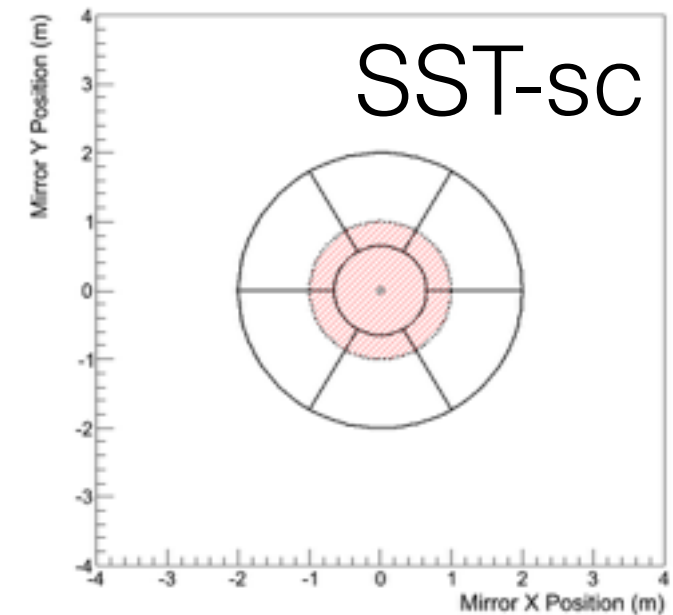
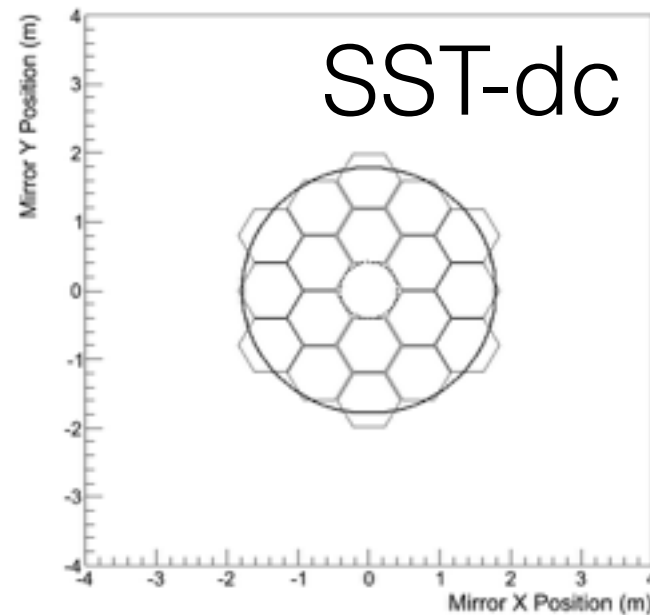
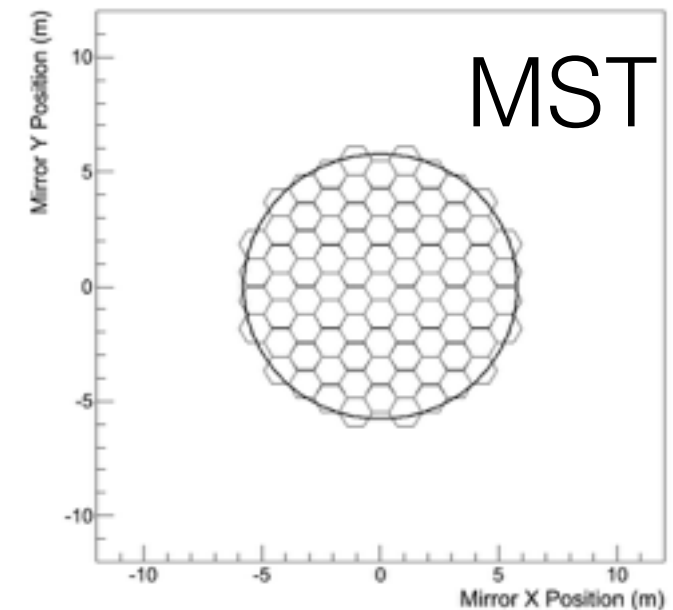
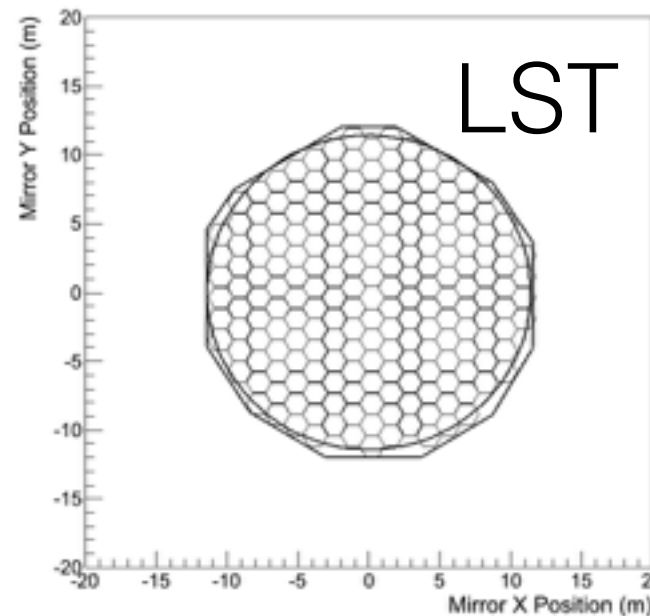
# CTA Mirror Descriptions

CTA Mirrors generally well approximated by a circle

Interpolation more precise, but small corrections

Dual Mirror SSTs more complex

N.B. SST-dc ~ SST-1M, and SST-sc ~ SST-GCT, but some minor differences



# Dual-Mirror telescopes

1.  $\rho > R$  and  $\rho \sin \phi > R'$

$$C = D$$

$$D(\rho, \phi) = 2R \sqrt{1 - \left(\frac{\rho}{R}\right)^2 \sin^2 \phi}$$

2.  $\rho > R$  and  $\rho \sin \phi < R'$

$$C = D - D'$$

$$D'(\rho, \phi) = 2R' \sqrt{1 - \left(\frac{\rho}{R'}\right)^2 \sin^2 \phi}$$

3.  $\rho < R$  and  $\rho \sin \phi > R'$

$$C = D$$

$$D(\rho, \phi) = R \left[ \sqrt{1 - \left(\frac{\rho}{R}\right)^2 \sin^2 \phi} + \frac{\rho}{R} \cos \phi \right]$$

4.  $\rho < R$  and  $\rho \sin \phi < R'$

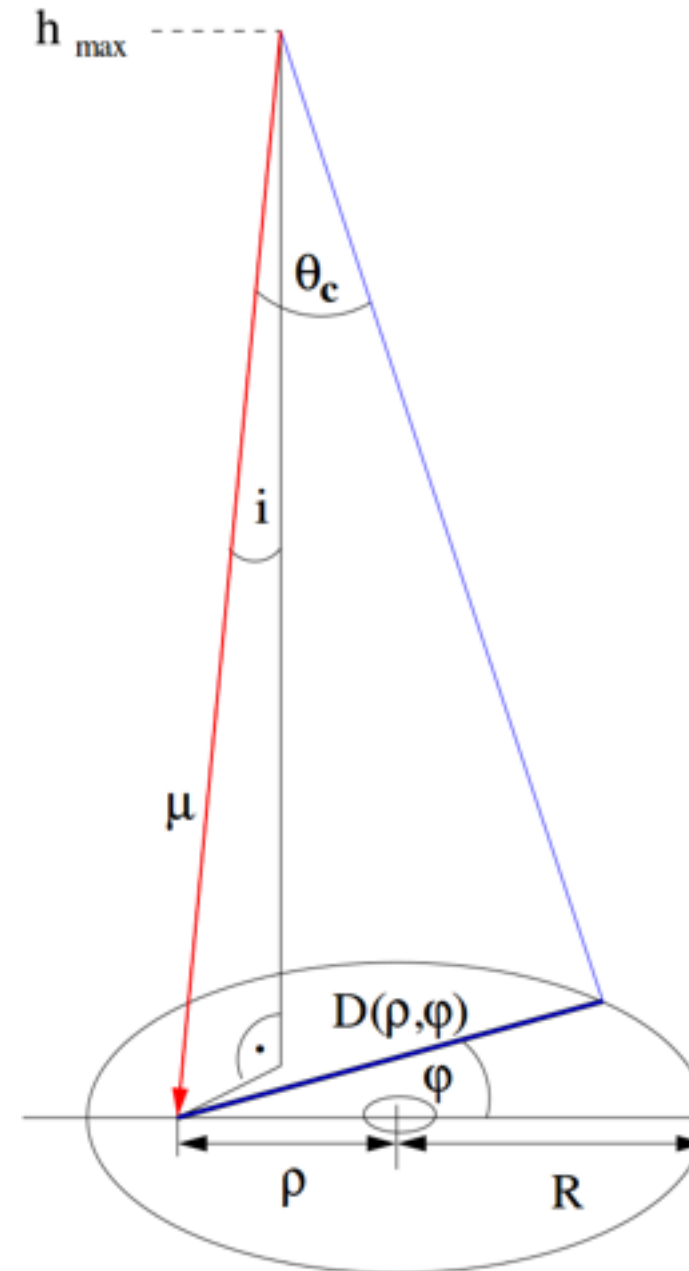
- (a)  $\rho > R'$

$$C = D - D' \text{ (3.,2.)}$$

- (b)  $\rho < R'$

$$C = D - D' \text{ (3.,4.)}$$

$$D'(\rho, \phi) = R' \left[ \sqrt{1 - \left(\frac{\rho}{R'}\right)^2 \sin^2 \phi} + \frac{\rho}{R'} \cos \phi \right]$$



- How to treat secondary mirror?
- Same as hole in centre of HESS mirrors? Or like shadowing?
- Efficiency of mirrors separately, or telescope as a whole?

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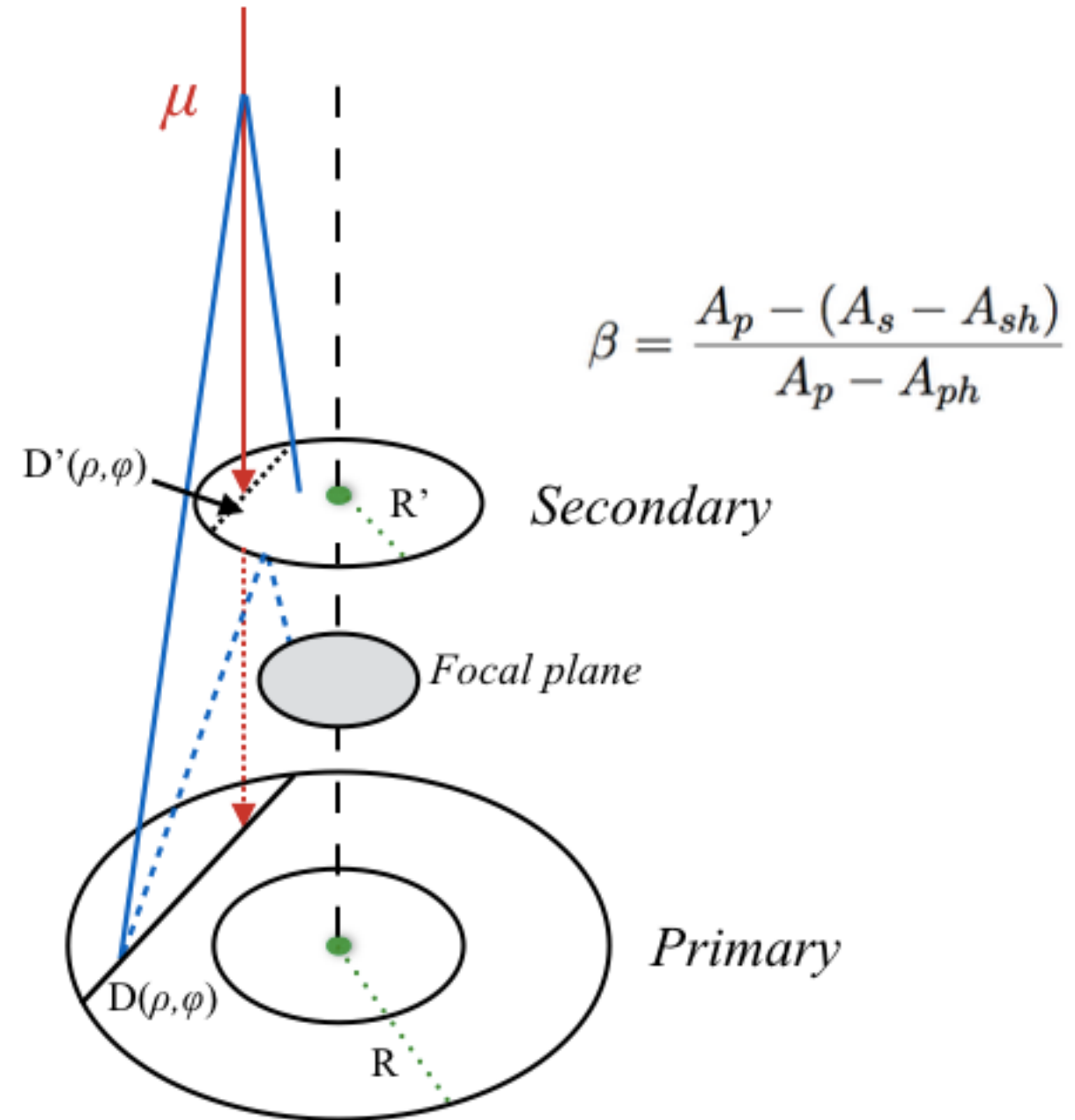
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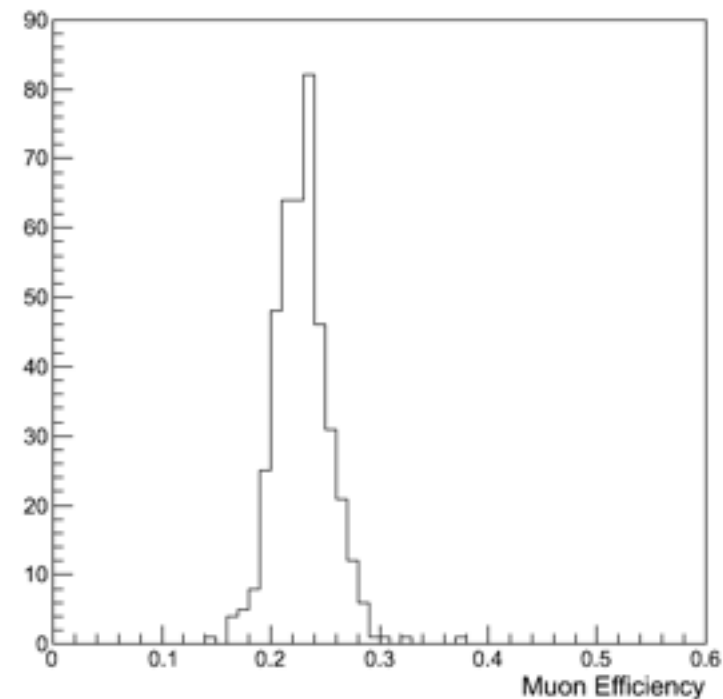
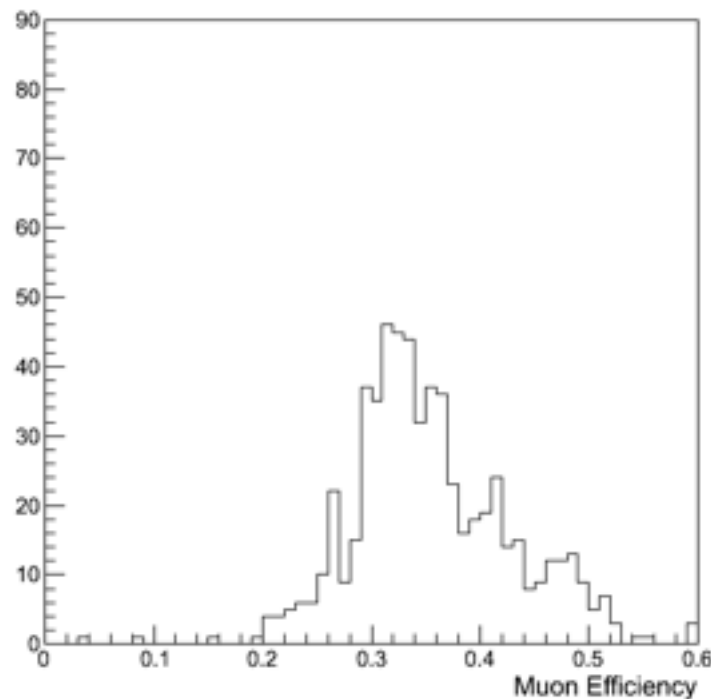
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# Dual-Mirror telescopes

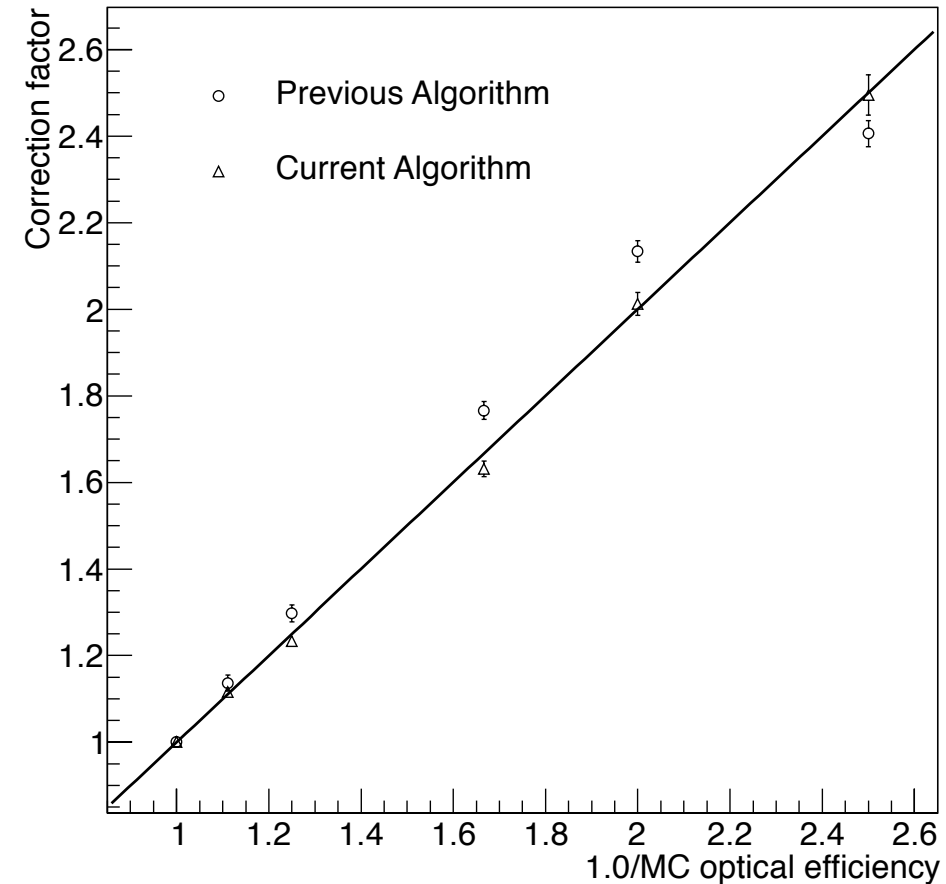
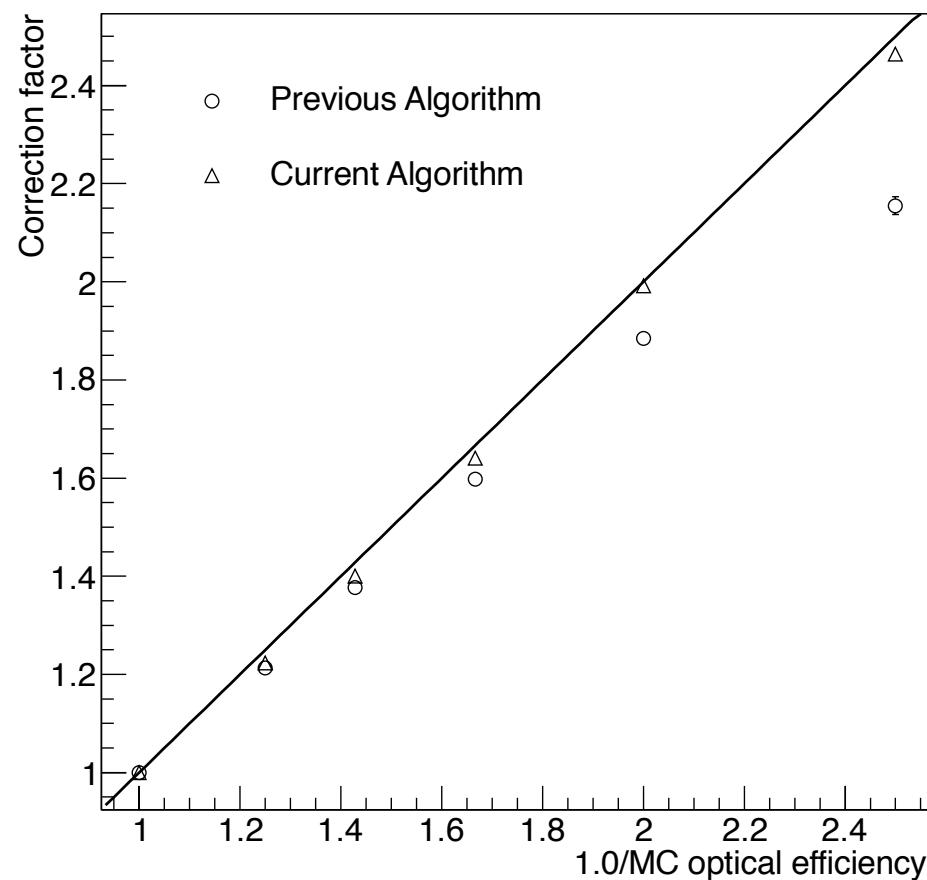
- Find poor distribution when treating the secondary mirror as a hole/loss of light (left)
- Improved by adding contributions to the chord across both mirrors (right)
- However, need to scale to account for the overall shadowing

$$\beta = \frac{A_p - (A_s - A_{sh})}{A_p - A_{ph}}$$

- N.B. —> Seems to work; not the final word!



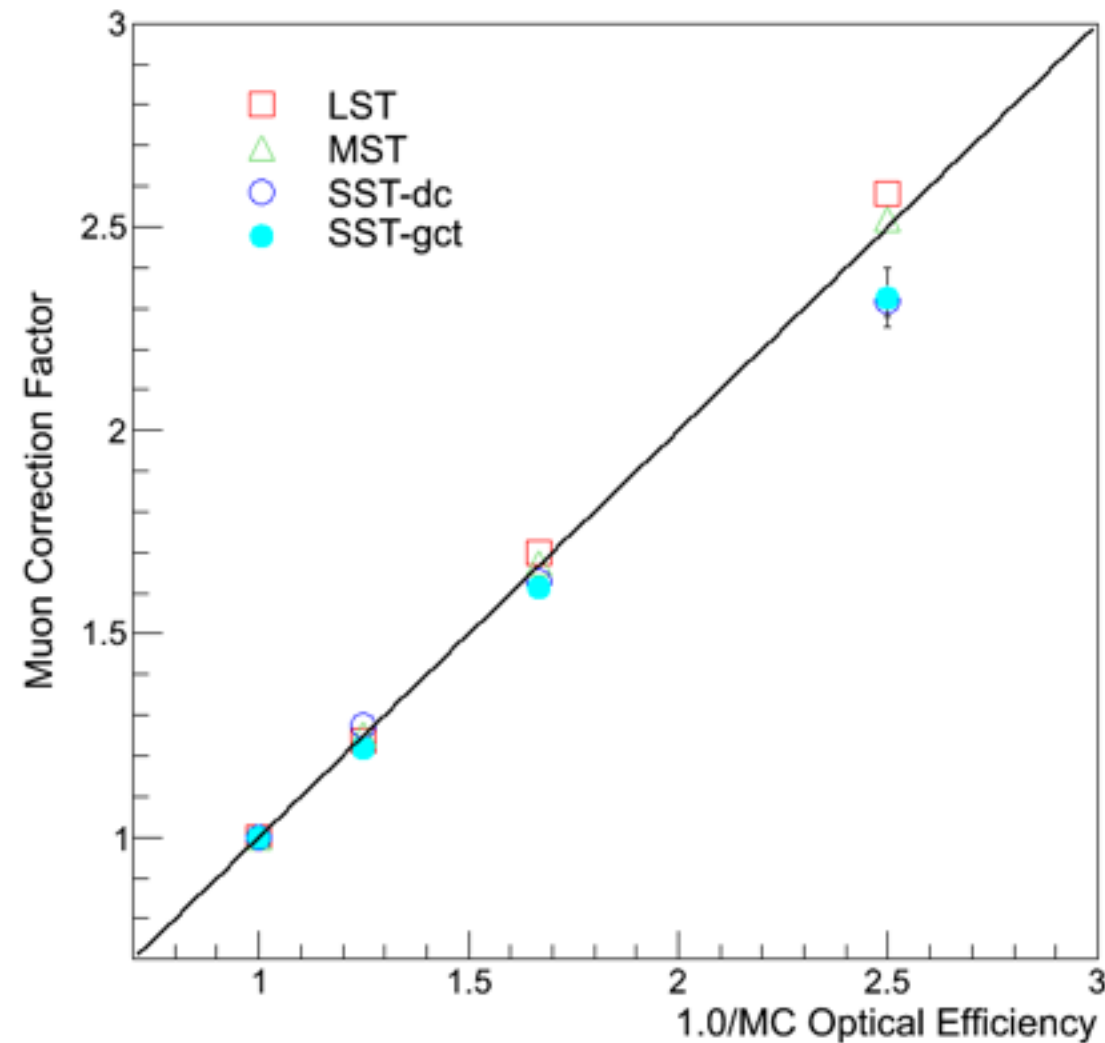
# H.E.S.S. II $\mu$ Performance



- Linearity of correction factor with degradation is improved over previous algorithm
- Shown on MC (linearity always assumed in application to data)

$$c = \varepsilon_{\mu}(\text{degraded MC}) / \varepsilon_{\mu}(\text{nominal MC})$$

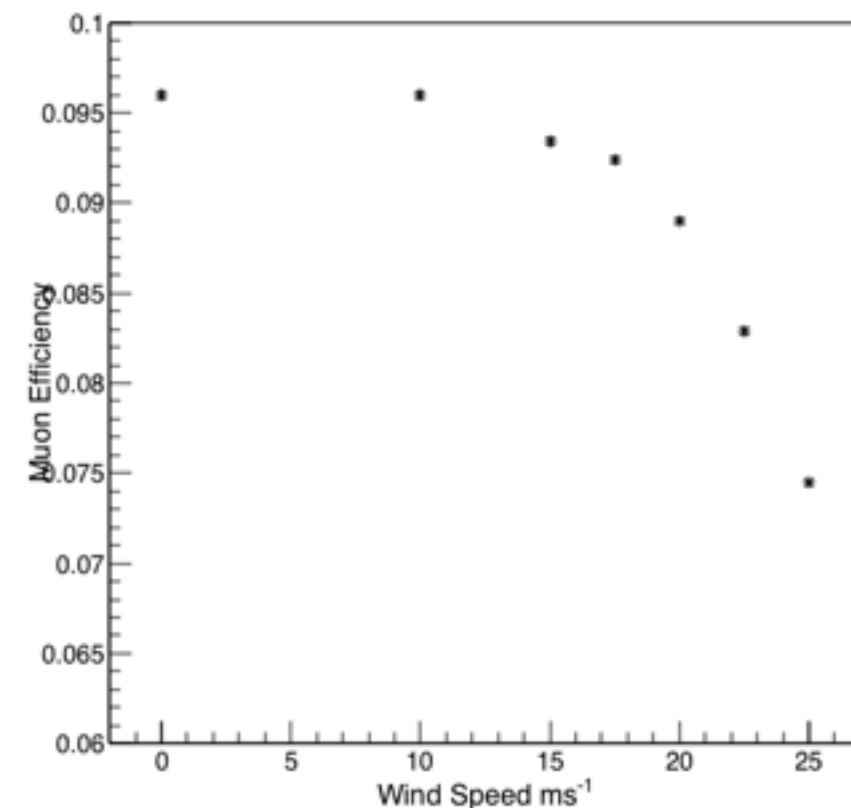
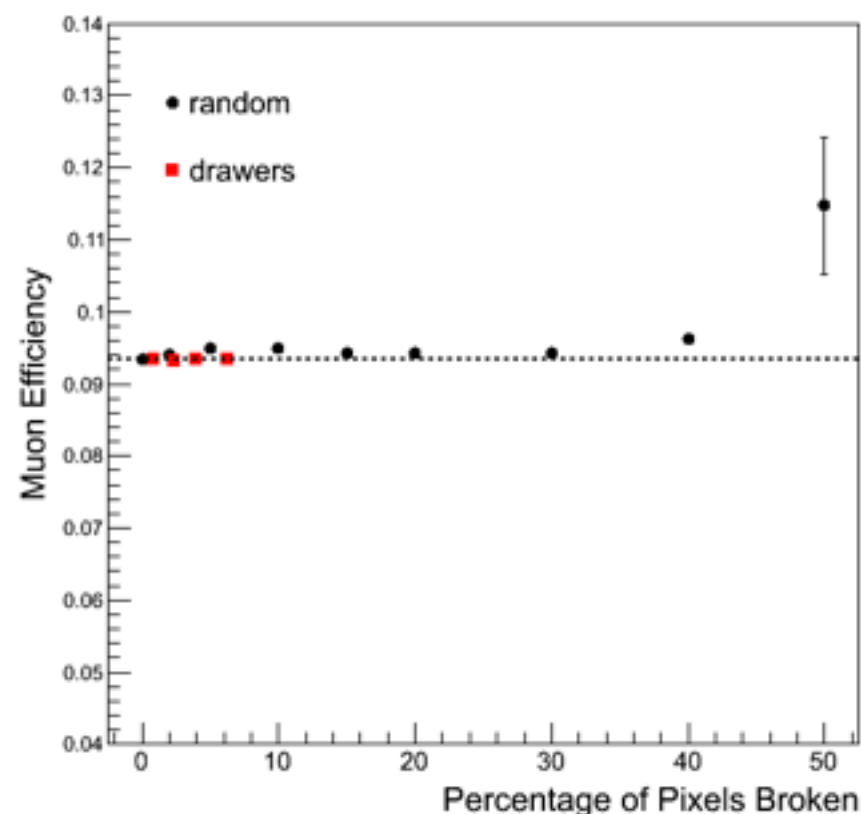
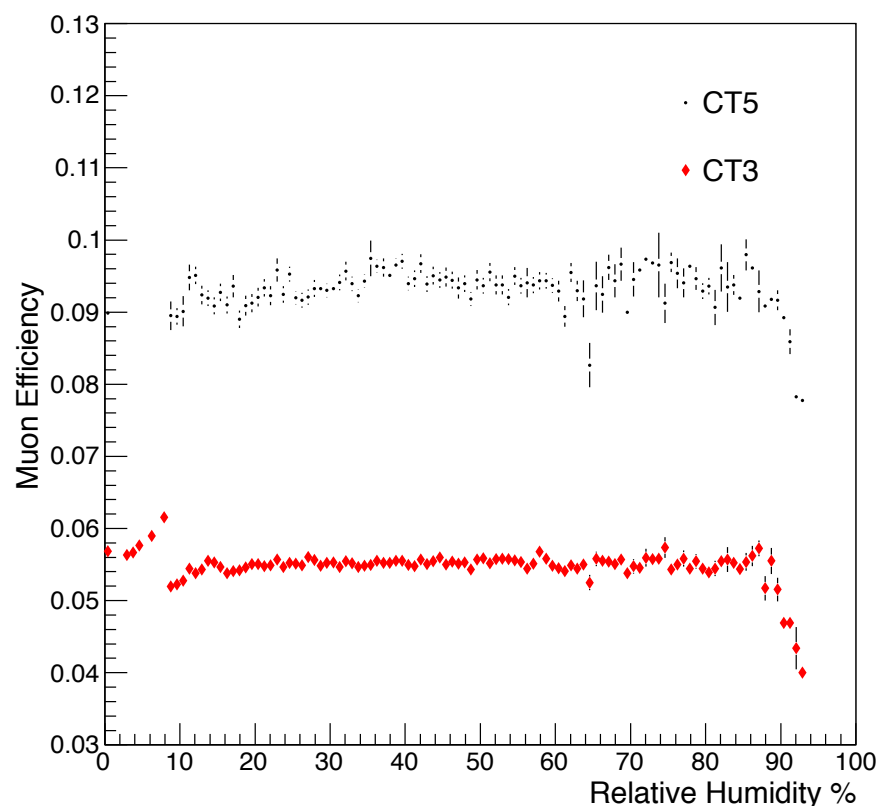
# CTA $\mu$ Performance



- Correction factor mostly linear with optical efficiency degradation
- Treatment of secondary mirror needs more thought
- Cut optimisation still needed

$$c = \varepsilon_{\mu}(\text{degraded MC}) / \varepsilon_{\mu}(\text{nominal MC})$$

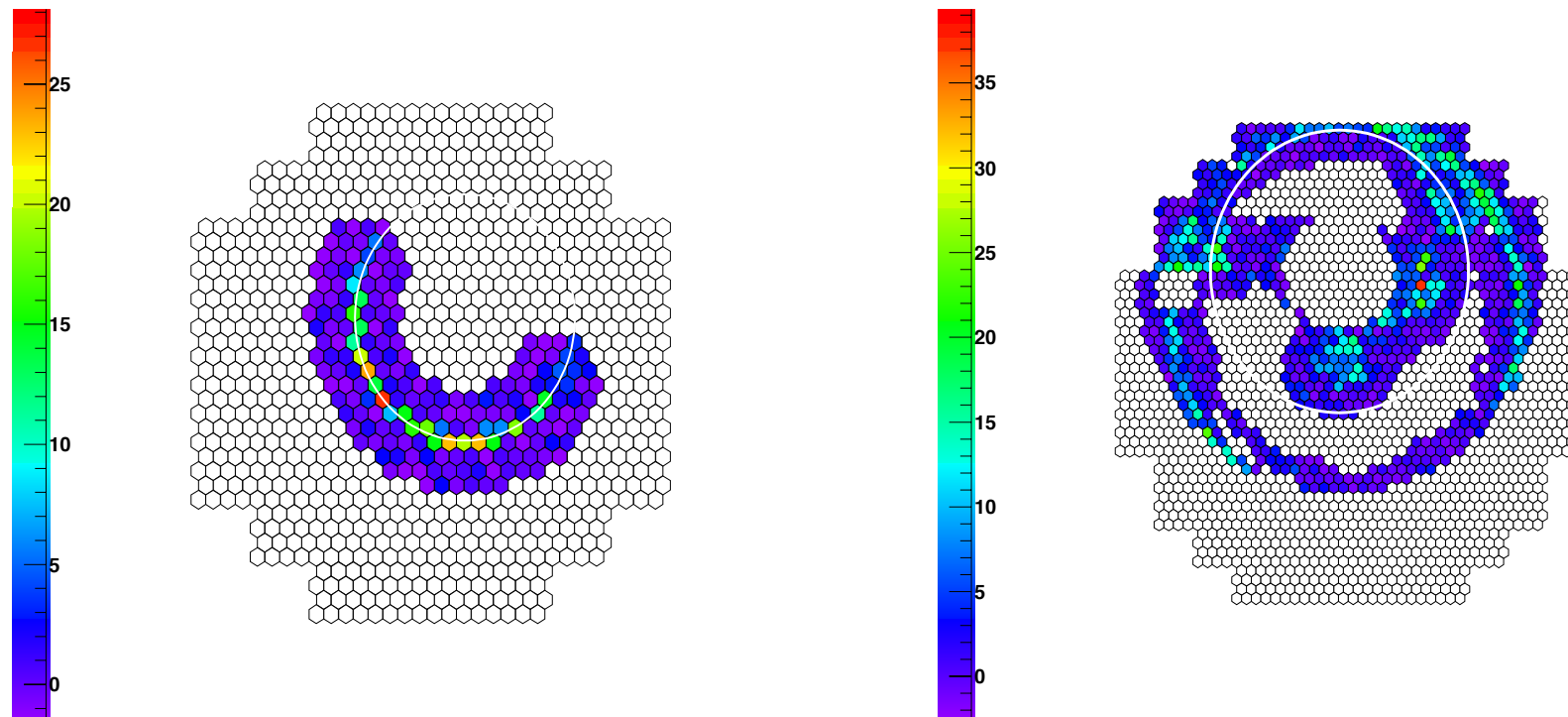
# Other factors affecting muon calibration



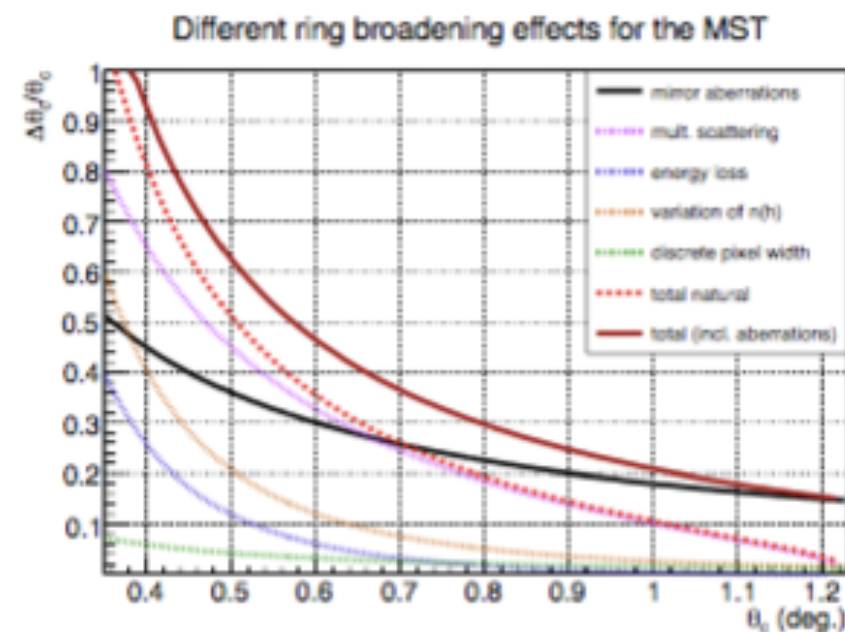
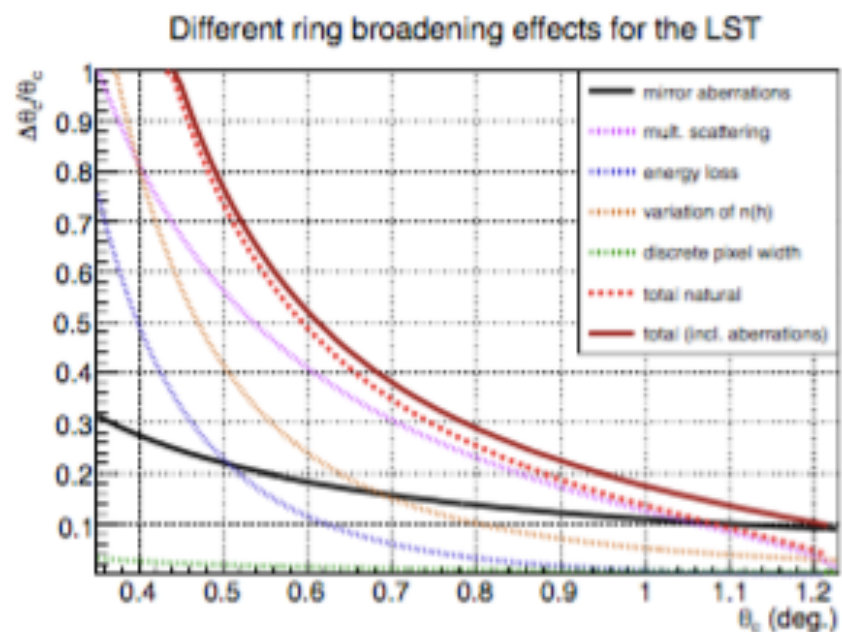
HESS

- Quality cuts based on environment and hardware:
  - Reject data with large number of broken pixels
  - Reject data with high humidity
  - (Wind speed  $\Leftrightarrow$  aerosol content in simulations)
- Cherenkov angle depends on atmosphere & altitude

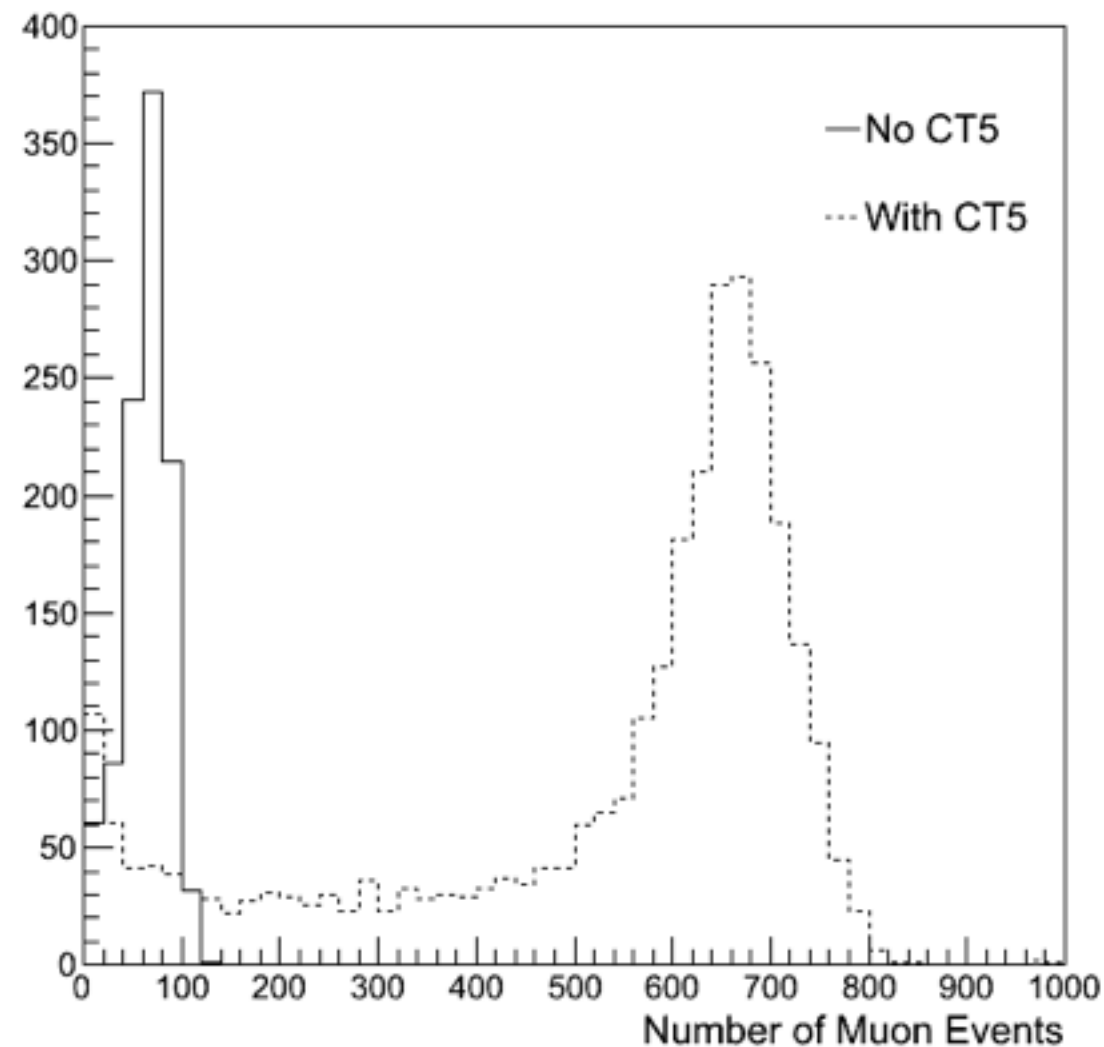
# Other factors affecting muon calibration



- Partial Muon Rings
- Background from hadronic shower
- Ring Broadening effects...



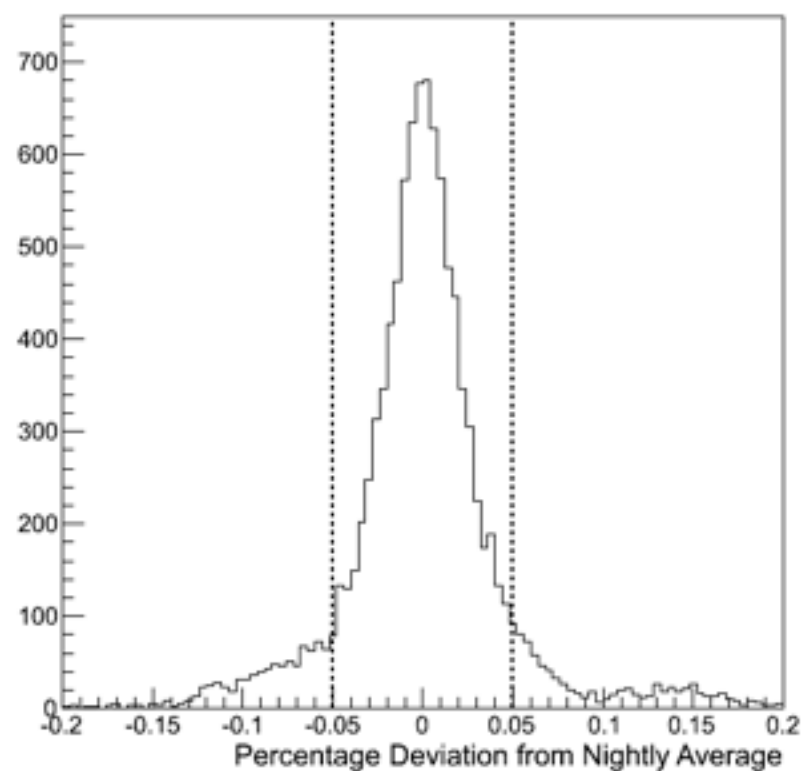
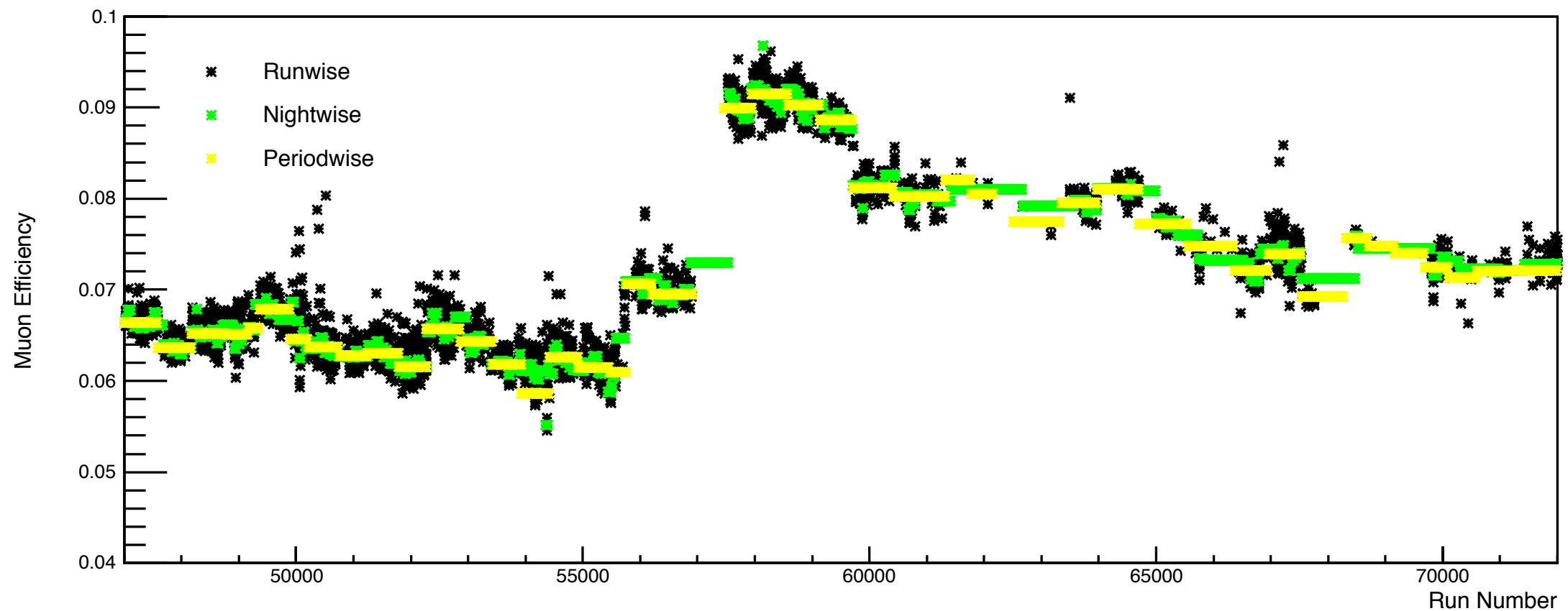
# Number of muons



Number of muons detected depends on telescopes taking data  
—> depends on array location  
Mono muon trigger for MSTs?

# Variation over time

HESS



- Should the muon calibration be implemented per “run”, per night, or per month?
- All three currently available in HESS

# How to apply muon calibration to data?

- In HESS: currently, take ratio of muon efficiency to a reference value from Monte Carlo - gives a correction factor
- Correction is applied directly to **reconstructed energy** estimates rather than **image size**
- Alternatively; interpolate between lookup tables rather than applying a correction
- Also affects the **effective area** of the array
- Two schools of thought within HESS:
  - Reproduce Monte Carlo when efficiencies deviate significantly ( $\sim 10\%$ ) from current set
  - Continue with same Monte Carlo, adjusting by correction factor
- Other approaches?
  - MAGIC use a conversion efficiency ratio as a correction to the **MC ADC counts - photons conversion factor**
  - MAGIC also measure the **PSF** from the width of the Gaussian fit
  - VERITAS - no corrections directly applied (?)
  - **Run-wise simulations**: no correction (factor = 1.0) - monitoring only?
- **Which to adopt?** (at array level and at telescope/camera level)

# “Shopping list” for input needed :

- Need to know from telescope/camera specifics:
  - Material of PMs/PMTs & mirrors —> which dominate degradation? ✓
  - Mirror and camera configuration (optics...) ✓
  - PSF - which effects dominate broadening? ✓
  - Can muon candidates be identified at trigger level? If so, how? (✓)
- Need to know wrt CTA pipeline/Monte Carlo:
  - Format of data arriving/framework of reconstruction
  - How often to simulate/reproduce MC? (per run? Muon input?)
  - *Over what time period should efficiency be averaged?*
  - *How is it foreseen to be applied in the reconstruction?*
- Need to know from CCF:
  - Which parameters to obtain? (timing, efficiency, psf...) ✓
  - Input from muons to atmospheric calibration or vice versa?
  - *Over what time period should efficiency be averaged? (OVERLAP)*
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# Thank you for your attention

Any Questions?